TMD Theory Overview

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"PHYSICS OPPORTUNITIES AT AN ELECTRON-ION COLLIDER", POETIC, BLOOMINGTON, AUG 20, 2012

TMD vs. collinear factorization

Collinear factorization in pQCD

□ applicable to one-scale processes, e.g. 1-particle inclusive processes



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□ Cross sections at high energies → (hard part) × (soft parts)

□ hard part → pQCD (NLO, NNLO,...); soft parts → universal, 1-dim

collinear parton distributions

 $q(x,\mu),\,\Delta q(x,\mu),\,\delta q(x,\mu)$

$$G(x,\mu), \, \Delta G(x,\mu)$$

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 $q(x,\mu), \, \Delta q(x,\mu), \, \delta q(x,\mu)$

 $G(x,\mu), \, \Delta G(x,\mu)$

 $d\sigma$

 $dx \, dQ^2$

□ also for higher twist observables → Single-Spin Asymmetries (ETQS)



+



hard scale Q

two scales:

final state transverse momentum $\, q_T \,$

 $\wedge \wedge \wedge$

Collinear factorization: 2 (or more...)-particle inclusive processes

SIDIS



two scales: hard scale Q +

 \rightarrow integrated observables



final state transverse momentum q_T $\int d^2 \mathbf{q_T} \, w(\mathbf{q_T}) \, \frac{d\sigma}{dx \, dQ^2 \, d\mathbf{q_T}} \equiv \langle w(q_T) \rangle$

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\Box q_T-dependence:



one scale → collinear factorization ok, transverse momentum generated perturbatively in hard part



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large logs in the hard part (gluon radiation) $\log^n(q_T/Q)$ \rightarrow CSS-resummation \rightarrow coll. fact. still applicable



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→ Transverse momentum dependent (TMD) factorization!

Idea of TMDs:

transverse momentum q₊ from "intrinsic" transverse parton momentum k₊ → different kind of factorization → additional degree of freedom of partonic motion → study different aspects of hadron spin structure (e.g. 3-d momentum structure, spin-orbit correlations, etc.)



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All-order factorization theorem for, e.g., Drell-Yan





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All-order factorization theorem for, e.g., Drell-Yan

$$\frac{W^{\mu\nu} \sim \int d^2 k_{aT} d^2 k_{bT} \,\delta^{(2)}(\vec{k}_{aT} + \vec{k}_{bT} - \vec{q}_T) \operatorname{Tr}[\hat{M}^{\mu} \Phi(x_a, \vec{k}_{aT})(\hat{M}^{\nu})^{\dagger} \bar{\Phi}(x_b, \vec{k}_{bT})] + Y^{\mu\nu}}{q_T \ll Q}$$

$$q_T \ll Q$$

proven for SIDIS + pp - collisions with color singlet final states ICollins; ji, Ma, Yuan; Qiu; Rogers, Mulders; ...]







→ Wilson line: initial/final state interactions (sign change, color entanglement, etc.)

(Naive) definition of the quark TMD correlator

$$\Phi^{[\Gamma]}(x,k_T) = \int \frac{dz^- d^2 z_T}{2(2\pi)^3} e^{ik \cdot z} \langle P, S | \bar{q}(0) \Gamma \mathcal{W}[0,z] q(z) | P, S \rangle \Big|_{z^+=z^+}$$

→ Wilson line: initial/final state interactions (sign change, color entanglement, etc.)

All-order definition beyond tree-level

[Aybat, Rogers, PRD83, 114042; Collins' "Foundations of pQCD"]

→ Wilson lines off the lightcone

→ regulator ξ → "unsubtracted" "subtract" soft factor

$$\Phi_{ij}(x,\vec{k}_T;S;\boldsymbol{\xi},\boldsymbol{\mu})$$

Collins-Soper evolution equations for ξ , μ



Implements Subtractions/Cancellations







Gluon TMDs

$$\Gamma^{ij}(x,\vec{k}_T) = \frac{1}{xP^+} \int \frac{dz^- d^2 z_T}{(2\pi)^3} e^{ik \cdot z} \langle P, S | F^{+i}(0) \mathcal{W}[0;z] F^{+j}(z) | P, S \rangle \Big|_{z^+=0}$$

$\Gamma^{[T-even]}(x,\vec{k}_T)$			$\Gamma^{[T-odd]}(x,\vec{k}_T)$	
		flip		flip
И	f_1^g	$h_1^{\perp g}$		
L	$g_{1L}^{\perp g}$			$h_{1L}^{\perp g}$
Ŧ	$g_{1T}^{\perp g}$		$f_{1T}^{\perp g}$	$h_1^g \ h_{1T}^{\perp g}$

[Mulders, Rodrínes, PRD 63,094021]



- * gluonic correspondence to "Boer-Mulders": T-even
- * unpolarized gluons in transversely pol. proton: gluon Sivers function
 * gluonic transversity / pretzelosity / wormgears: T-odd
 * no chirality
 * two collinear PDFs

Gluon TMDs do not appear in Drell-Yan or SIDIS

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Heavy Quark production in e + p - collisions

[Boer, Brodsky, Mulders, Písano, PRL 106, 132001]

 $e + p^{(\uparrow)} \rightarrow e' + \operatorname{jet}(c, b) + \operatorname{jet}(\overline{c}, \overline{b}) + X$

TMD factorization ok!

Spin dependent (+independent...) gluon TMDs: EIC would be ideal!

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unpolarízed cross section:

$$\frac{d\sigma_{UU}}{dq_T} \propto \left(F_1 + F_2\cos(2\phi)\right)$$

azímuthally independent term: I azímuthally dependent term: I

 $F_1 \propto f_1^g(x, q_T) \rightarrow unpol.$ gluon distribution $F_2 \propto h_1^{\perp g}(x, q_T) \rightarrow linearly pol.$ gluons

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p PDF Heavy Quark production in e + p - collisions [Boer, Brodsky, Mulders, Pisano, PRL 106, 132001]

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→ unpol. gluon distribution azimuthally independent term: $F_1 \propto f_1^g(x, \mathbf{q_T})$ $F_2 \propto h_1^{\perp g}(x, \mathbf{q_T})$ → línearly pol. gluons azimuthally dependent term:

Heavy "back-to-back" díjet production in pp - collisions: TMD factorization problematic!

pp - collisions

Gluon TMDs measurable in pp-collisions with color singlet final states $p + p \rightarrow ((\bar{N}), (\gamma \gamma), (\gamma l\bar{l}), (l'\bar{l}')(l\bar{l}), ...) + X$ (RHIC / LHC)

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Photon Pair production

[Qín, M.S., Vogelsang, PRL 107, 062001 (2011)]

quark TMDs



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Other leptonic final states (218, 41)

[Qín, M.S., Vogelsang, PRL 107, 062001 (2011)]

quark TMDs



gluon TMDs at $O(\alpha_s^2)$



[Boer, den Dunnen, Písano, M.S., Vogelsang, in prep.]





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quark TMDs







no colored final state \Rightarrow TMD factorization ok

Initial state interactions only, past-pointing Wilson lines

- $\Box \qquad gauge invariance \Rightarrow box finite \Rightarrow effectively tree-level$
 - potentially large gluon distributions

[Boer, den Dunnen, Písano, M.S., Vogelsang, in prep.]

Other leptonic final states (217, 41)





quark contributions -> almost identical to DY



gluon contributions \rightarrow absent in DY



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 $\left| + \left(\frac{\alpha_s}{2\pi}\right)^2 \left(\mathcal{F}_1[f_1^g \otimes f_1^g] + \mathcal{F}_2[h_1^{\perp g} \otimes h_1^{\perp g}] + \cos(2\phi)\mathcal{F}_3[h_1^{\perp g} \otimes f_1^g + f_1^g \otimes h_1^{\perp g}] + \cos(4\phi)\mathcal{F}_4[h_1^{\perp g} \otimes h_1^{\perp g}] \right) \right|$

gluon contributions -> absent in DY

 $\mathcal{F}_i(\theta) \rightarrow \text{non-trivial functions of } \cos(\theta)$ and $\sin(\theta)$ (Logarithms from quark loop)



→ gluon TMDs in YY

Can gluoníc TMDs be useful for the LHC?

[Boer, den Dunnen, Písano, M.S., Vogelsang, PRL 108, 032002 (2012)]

Maín Híggs production mechanism: gluon fusion Once a scalar particle (Híggs!?) is found... want to determine its spin, parity, etc.



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pure Higgs production



línearly polarízed gluons sensitive to Híggs parity $rac{d\sigma}{d^3q} \propto [f_1^g \otimes f_1^g] \pm [h_1^{\perp g} \otimes h_1^{\perp g}]$

+: scalar Higgs -: pseudoscalar Higgs

→ precise q_ measurement may offer a way to determine Higgs parity

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<u>Numerical estimate:</u> Gaussian ansatz + saturation of positivity bounds $< p_T^2 > = 7 \text{ GeV}^2$

CS evolution of unpol./lin. pol. gluons studied in [Sun, Xiao, Yuan, PRD 84, 094005]

Higgs decay into photon pairs: gg -> H/A -> YY + < + () 2 + $\int d\phi rac{d\sigma^{gg}}{d^4 q \, d\Omega} \propto ar{\mathcal{F}}_1 \left[f_1^g \otimes f_1^g
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 $Q \neq m_{H}: \quad \bar{\mathcal{F}}_{1} \gg \bar{\mathcal{F}}_{2}$

box dominant

Higgs dominant (pole of the propagator)

Sign signature preserved at the pole! small total Higgs width → good Q resolution

Higgs decay into 4 leptons: gg → H/A → 4l

[Boer, den Dunnen, Písano, M.S., Vogelsang, in prep.]

Different decay channels for scalar and pseudoscalar Higgs:

SM Higgs: tree-level vertex



Beyond SM pseudoscalar Higgs: top-loop



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one on-shell $Z: gg \rightarrow ZZ^*$



Beyond SM pseudoscalar Higgs: top-loop



two on-shell $Z: gg \rightarrow ZZ$



→ more difficult w.r.t. parity distinction, clean process experimentally Warning: multi-parton scattering!

May use also azimuthal cos (2φ) modulation... [Boer, den Dunnen, Pisano, MS, Vogelsang, in prep.]

$$\langle q_T^2 \cos(2\phi) \rangle = \int d^2 q_T d\phi \, q_T^2 \cos(2\phi) \frac{d\sigma}{d^4 q \, d\Omega} \sim \bar{\mathcal{F}}_3(\theta, Q^2) \left[f_1^g \otimes h_1^{\perp g} + h_1^{\perp g} \otimes f_1^g \right]$$

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Summary

Important progress on evolution of TMDs -> can be studied at EIC

Gluon TMDs can be studies at EIC

•Gluon TMDs from pp - collisions with leptonic final states at RHIC / LHC

Gluon Boer-Mulders effect may offer a way to determine parity of the Higgs boson at LHC