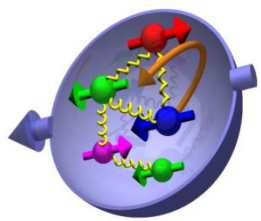


GPDs

-- status of measurements --

- a very brief introduction
- prerequisites and methods
- DVCS & DVMP: *selected* results
- on the way to an *EIC*

→ see additional slides for results not covered

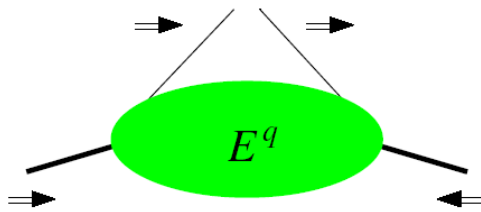


why GPDs ?

'spin puzzle'

$$s_z = \frac{1}{2} = J^q + J^g = \frac{1}{2} \sum_q \Delta q + L_z^q + \Delta g + L_z^g$$

\uparrow $\approx 30\%$ \uparrow $\approx \text{zero}$

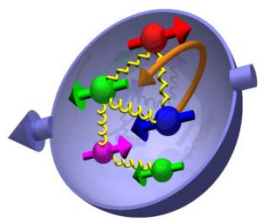


proton helicity flipped while
quark helicity is conserved

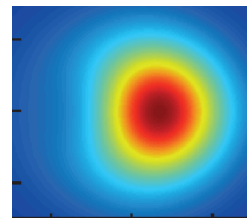
$E^q \neq 0$ requires orbital angular momentum

$$J^q = \frac{1}{2} \int_{-1}^1 x dx \left[H^q(x, \xi, t) + E^q(x, \xi, t) \right]_{t=0}$$

[X. Ji (1996)]



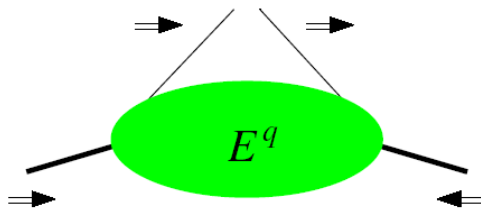
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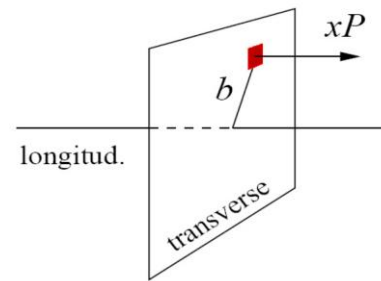
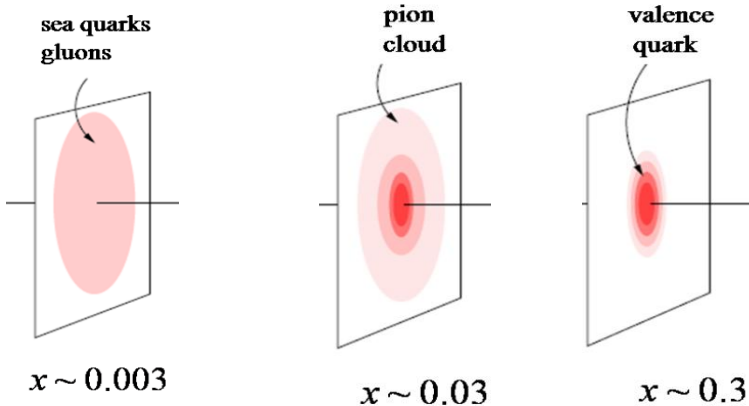
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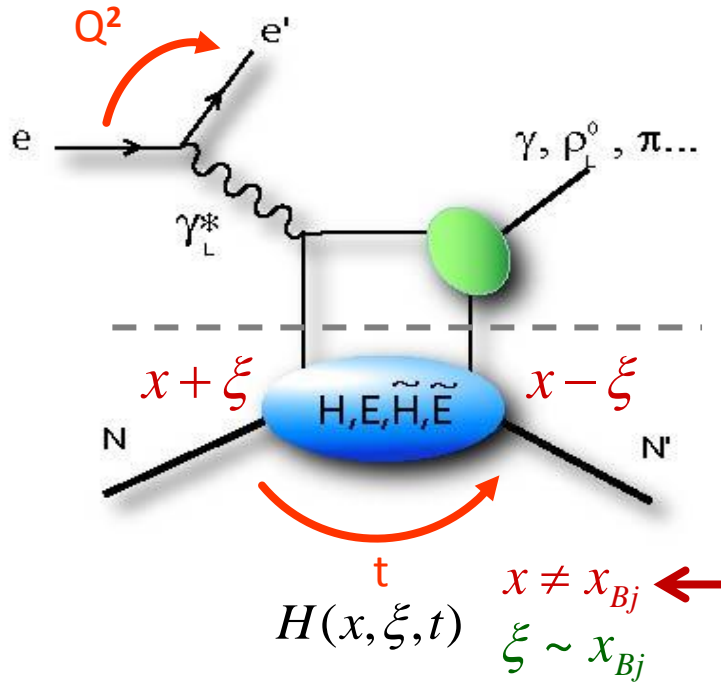
nucleon imaging: $FT(\text{GPD}) \rightarrow$ impact parameter space b_\perp : spatial distribution in transverse plane



(transverse distance from proton center of momentum)

[M. Burkardt(2001), M. Diehl(2002)]

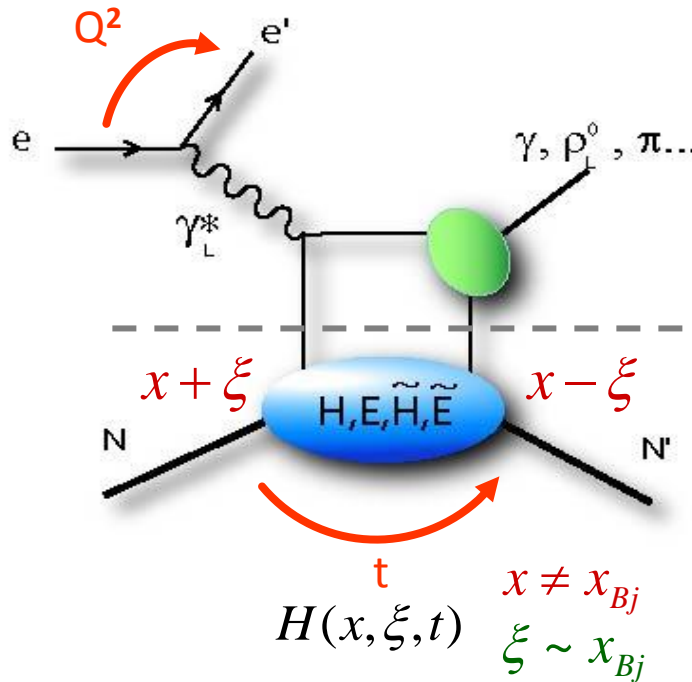
how to constrain GPDs ?



$$Q^2 \gg t, t \ll$$

appear in factorisation theorem for *hard exclusive* processes

how to constrain GPDs ?



$$Q^2 \gg, t \ll$$

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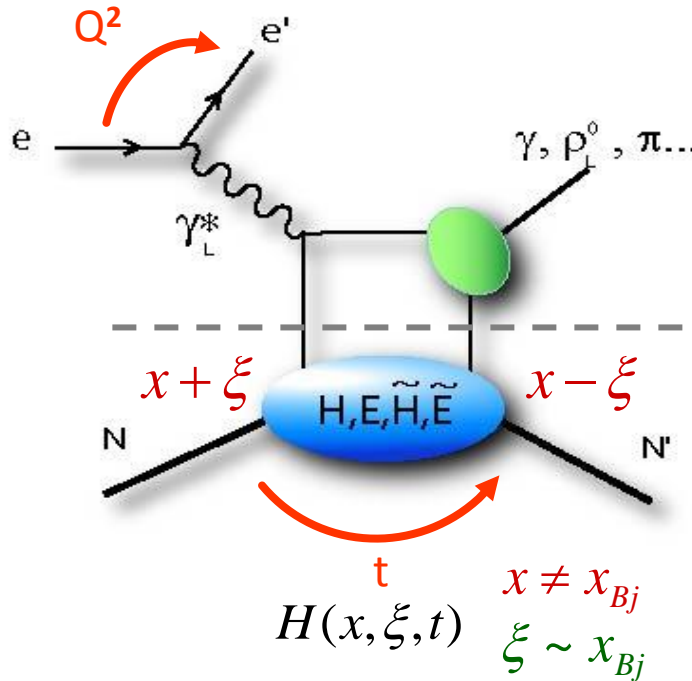
- spin 1/2 target:

4 leading-tw, chiral even q & g GPDs: H, \tilde{H} conserve nucleon helicity
 E, \tilde{E} involve nucleon helicity flip

+ 4 chiral odd ('transversity') GPDs, which flip the parton helicity

$H_T \rightarrow$ related to transversity

how to constrain GPDs ?



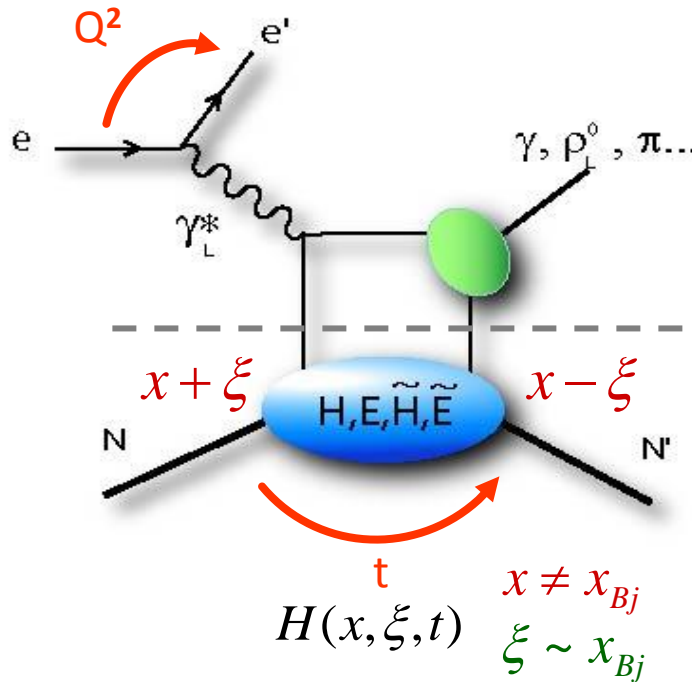
$$Q^2 \gg t, t \ll \Lambda^2$$

appear in factorisation theorem for *hard exclusive* processes

- **DVCS**: most clean process, (some) flavour dependent information from p & n target OR: *evolution*

→ $H, \tilde{H}, E, \tilde{E}$

how to constrain GPDs ?



$$Q^2 \gg, t \ll$$

appear in factorisation theorem for *hard exclusive* processes

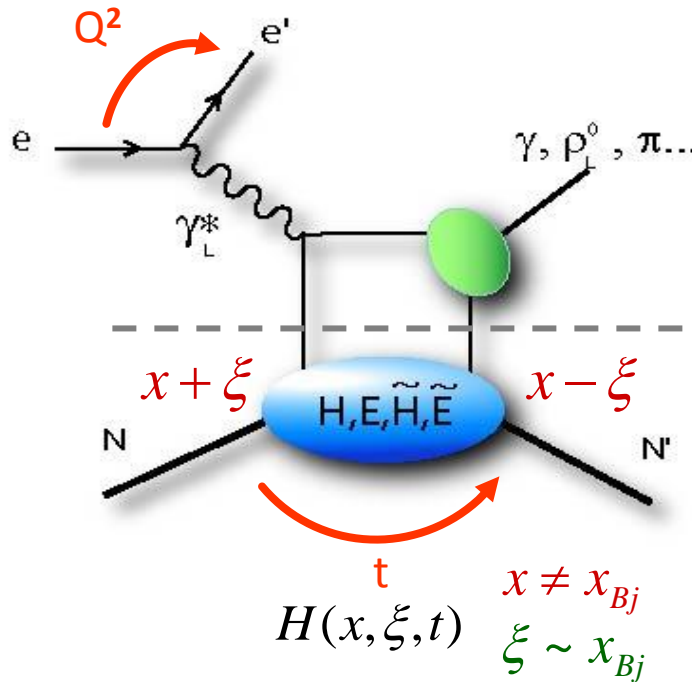
- **DVCS**: most clean process, (some) flavour dependent information from p & n target OR: *evolution*
- **DVMP**: flavour decomposition & gluons

$$\rightarrow H, \tilde{H}, E, \tilde{E}$$

$$VM \rightarrow H, E$$

$$PS \rightarrow \tilde{H}, \tilde{E}, \tilde{H}_T, \tilde{E}_T$$

how to constrain GPDs ?



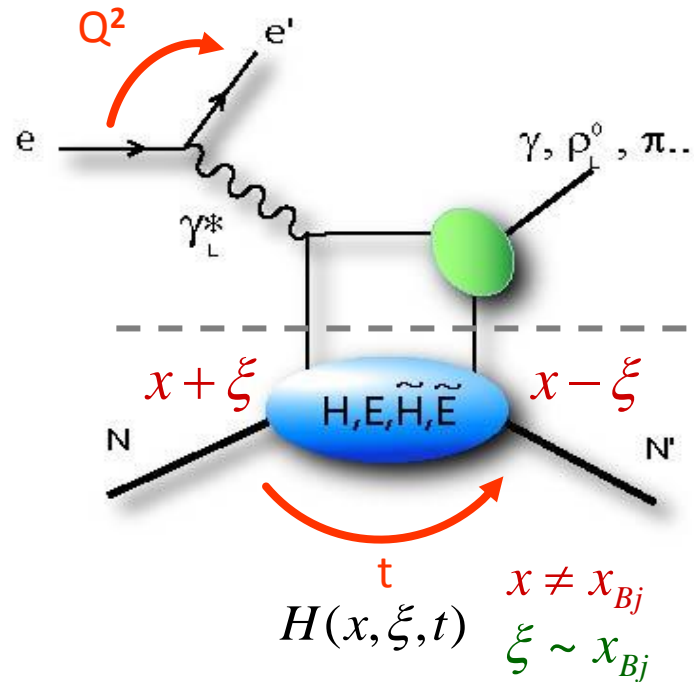
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ρ^0	$2u+d, 9g/4$
ω	$2u-d, 3g/4$
ϕ	s, g
ρ^+	$u-d$
J/ψ	g

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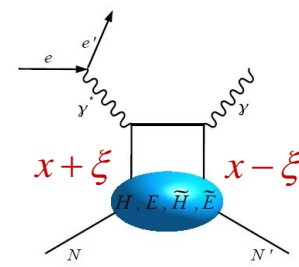
- **DVCS**: most clean process, (some) flavour dependent information from p & n target OR: *evolution*
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BUT

- factorisation only for σ_L
- meson distribution amplitude needed
- large NLO & power corrections

ρ^0	$2u+d, 9g/4$
ω	$2u-d, 3g/4$
ϕ	s, g
ρ^+	$u-d$
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link GPDs & observables

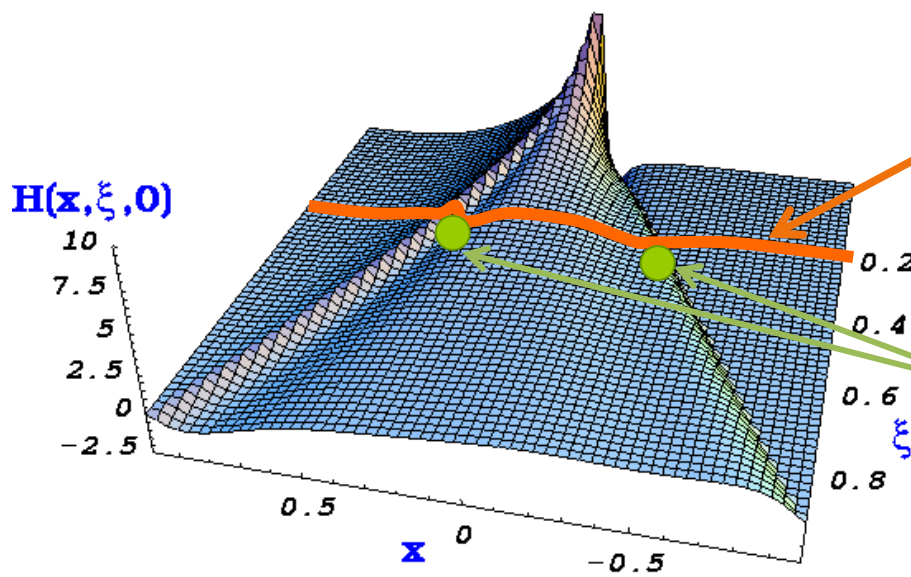


$$T_{\mu\nu} = [\mathcal{H}, \mathcal{E}, \tilde{\mathcal{H}}, \tilde{\mathcal{E}}](\xi, t, Q^2), \quad \mathcal{F}(\xi, t, Q^2) = \int_{-1}^1 dx C^-(\xi, x) F(x, \xi, t, Q^2),$$

complex DVCS amplitude

Compton Form Factor (CFF)

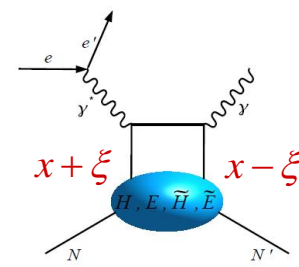
- x is mute variable (integrated over), needs deconvolution
 - apart from 'cross over' trajectory ($x = \pm \xi$) GPDs not directly accessible
- extrapolation $t \rightarrow 0$ model dependent



cross section & beam charge asymmetry
 $\sim \text{Re}(T^{\text{DVCS}})$:
integral of GPDs over x

beam or target spin asymmetries
 $\sim \text{Im}(T^{\text{DVCS}})$,
 i.e., GPDs @ $x = \pm \xi$

link GPDs & observables

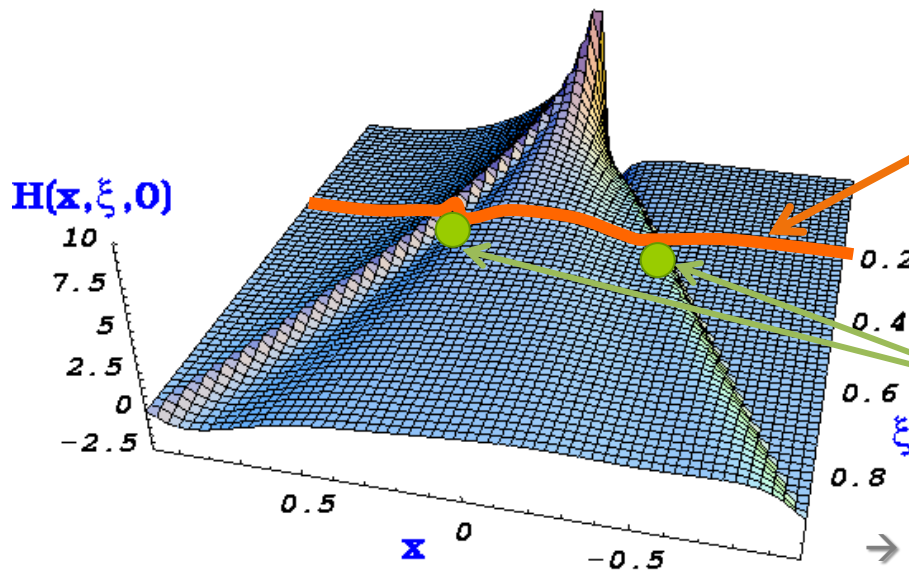


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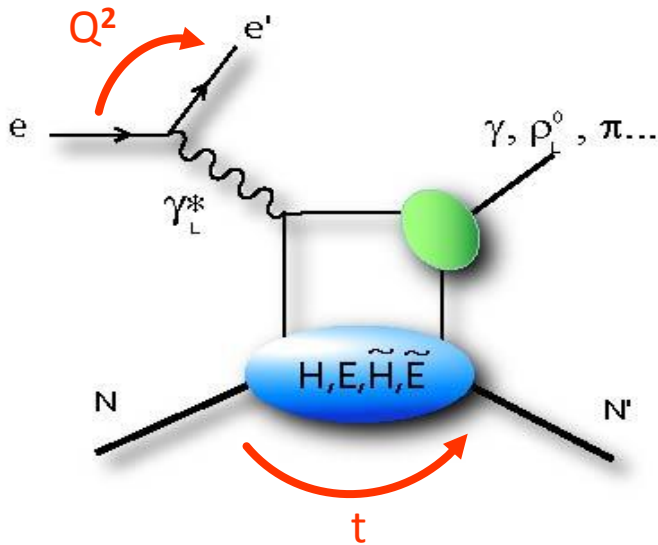
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 $\sim \text{Im}(T^{\text{DVCS}})$,
 i.e., *GPDs @ $x = \pm \xi$*

- x scan of GPDs:
- ‘double’DVCS: *JLab12 (?)*
 - Q2 evolution: *EIC*

the ideal experiment for measuring hard exclusive processes

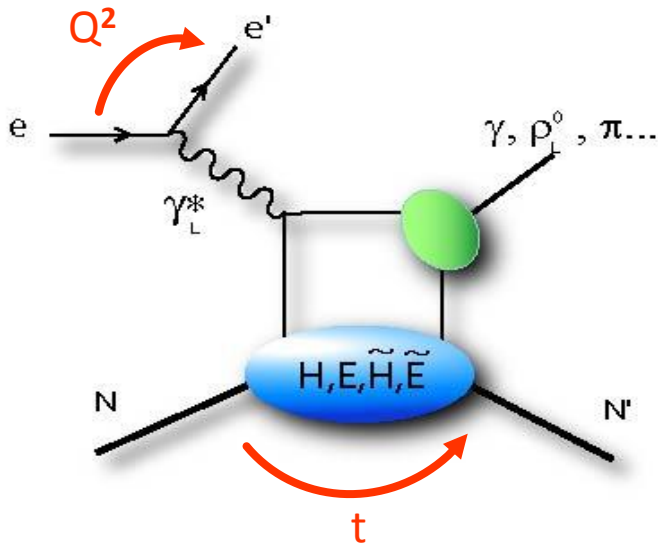
$$Q^2 \gg \Lambda^2, t \ll \Lambda^2$$



- high & variable beam energy
 - ensure hard regime
 - wide kinematic range
 - L/T separation for ps meson prod.
- high luminosity
 - small cross sections
 - fully differential analysis
- hermetic detectors
 - ensure exclusivity

the ideal experiment for measuring hard exclusive processes

$$Q^2 \gg, t \ll$$



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... doesn't exist (yet)...

experimental prerequisites



- polarised 27GeV e^+/e^-
 - unpolarised 920GeV p
 - \approx full event reconstruction
-
- polarised 27GeV e^+/e^-
 - long+transv polarised p, d targets
 - unpolarised nuclear targets
 - missing mass technique
 - 2006/7 data taken with recoil det.



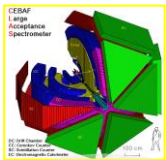
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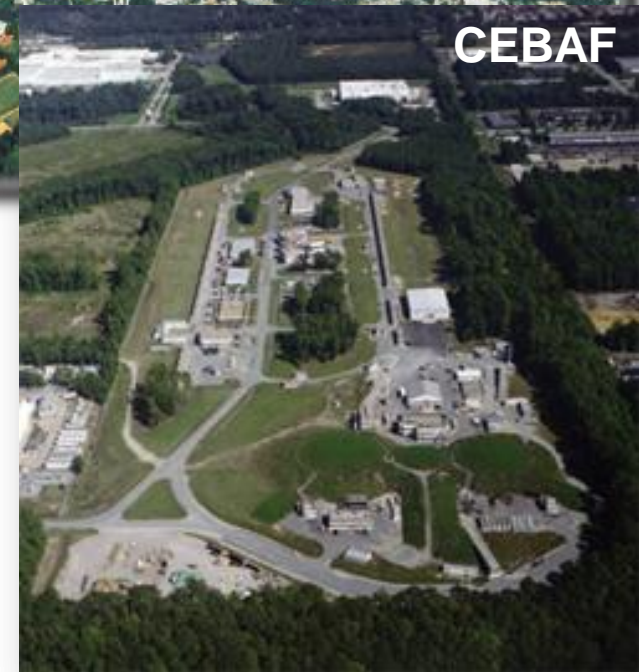


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Hall-A

- highly polarised, high lumi 6GeV e^-
- long polarised effective p, n targets
- CLAS: full event reconstruction
- Hall-A: missing mass/energy technique



experimental prerequisites



- polarised 27GeV e^+/e^-
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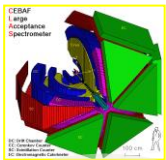
HERA till 2007



- polarised 27GeV e^+/e^-
- long+transv polarised p, d targets
- unpolarised nuclear targets

- missing mass technique
- 2006/7 data taken with recoil det.

CEBAF



Hall-A

- highly polarised, high lumi 6GeV e^-
- long polarised effective p, n targets
- CLAS: full event reconstruction
- Hall-A: missing mass/energy technique



- highly polarised, 160GeV μ
- long+transv polarised effective p, d targets
- missing mass/energy technique

CERN

COMPASS-II with recoil det.



results on /off the menu

data over wide kinematic range: HERA-collider → (COMPASS) → HERMES → JLab

□ VM production → H, E

- low x : gluon imaging
- high x : quarks & gluons; role of NLO contributions
- low W data from JLab
- SDMEs / amplitudes

□ ps meson production → $\tilde{H}, \tilde{E}, \tilde{H}_T, \tilde{E}_T$

- role of transverse photons, power corrections & chiral-odd *GPDs*

□ DVCS → $H, E, \tilde{H}, \tilde{E}$... the golden channel & most rich plate

- nuclear modification of DVCS amplitudes: HERMES

□ hunting the OAM

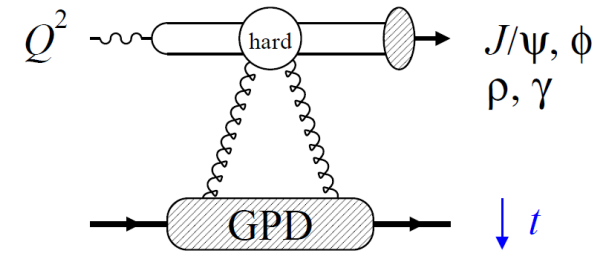


VM production @low x



energy dependence probes transition from soft to hard regime

$$d\sigma/dt \sim e^{-b|t|}$$





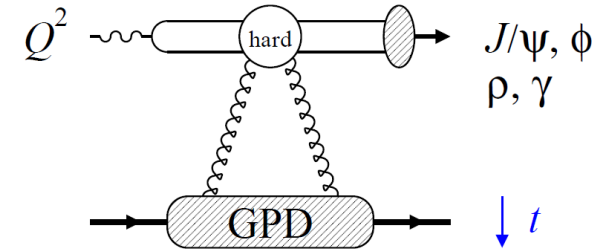
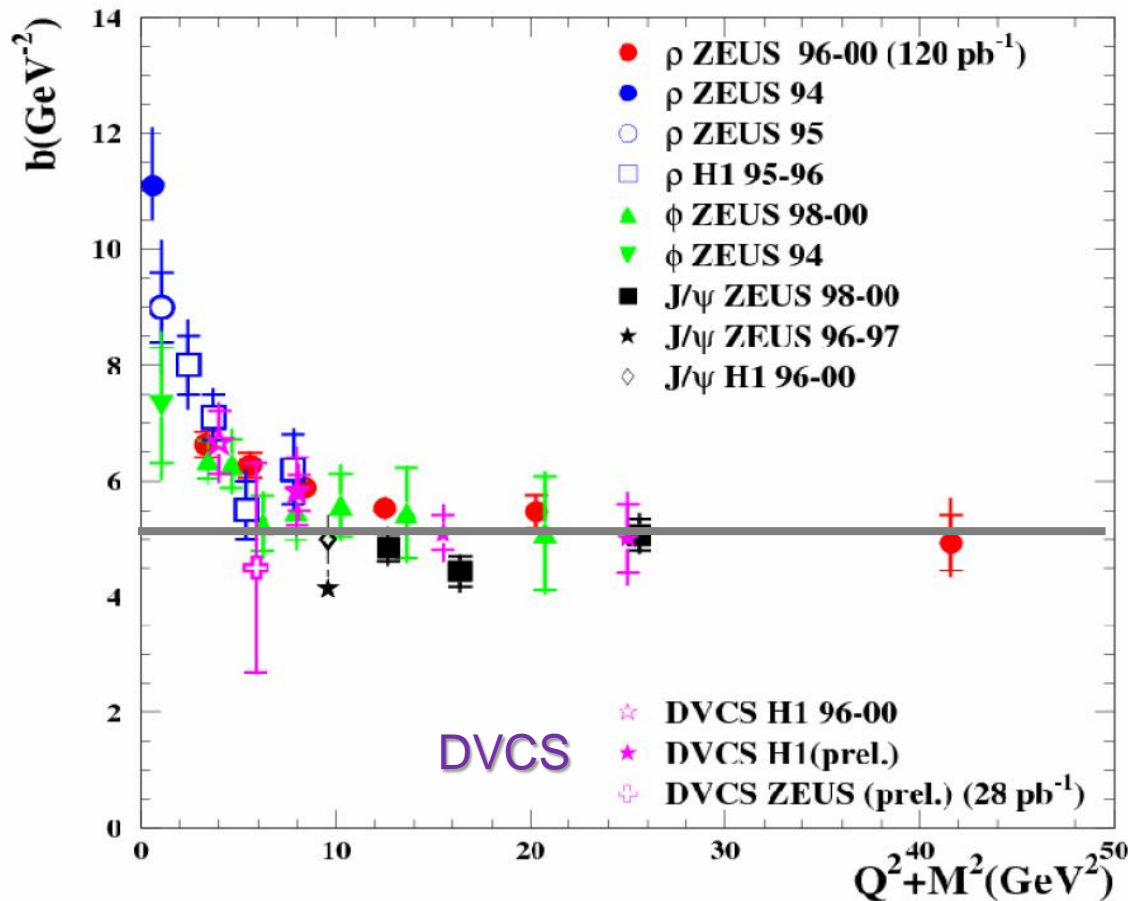
VM production @low x



energy dependence probes transition from soft to hard regime

$\rho, \phi, J/\psi, DVCS$

$$d\sigma/dt \sim e^{-b|t|}$$



universality of b slope parameter

→ point like configurations dominate

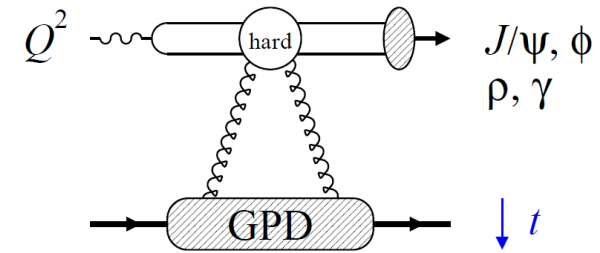


gluon imaging: J/ψ



energy dependence probes hard regime; $FT \rightarrow$ average impact parameter

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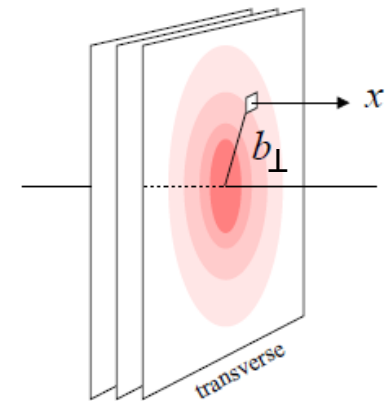


- $FT \rightarrow$ average impact parameter

$$\langle b_{\perp}^2(x_{Bj}) \rangle$$

distance between active quark/gluon and proton center of momentum

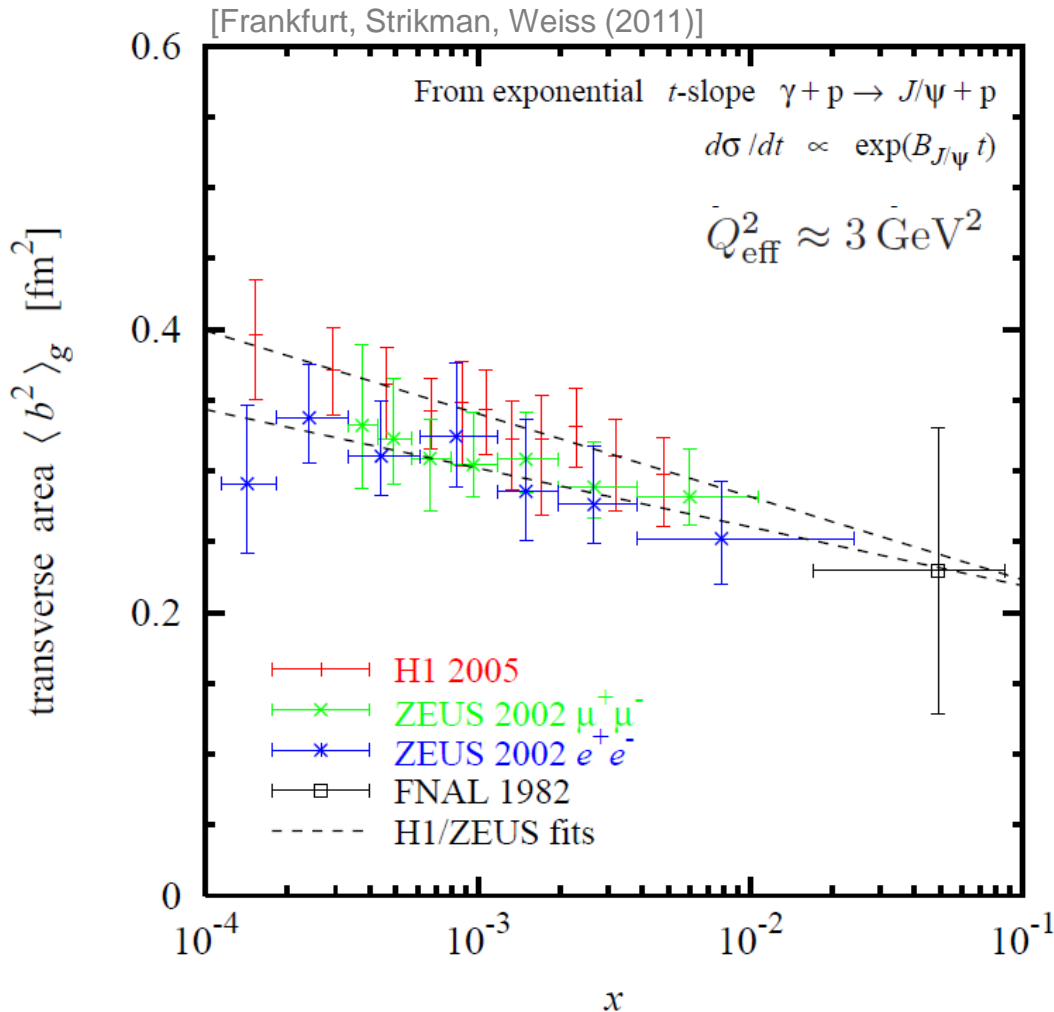
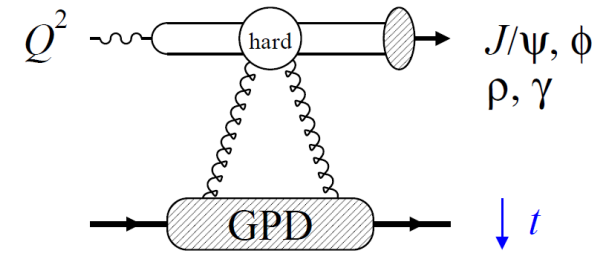
[M. Burkardt(2001), M. Diehl(2002)]



[fig: courtesy C. Weiss]

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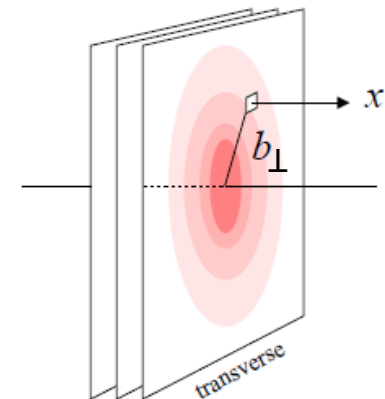


▪ $FT \rightarrow$ average impact parameter

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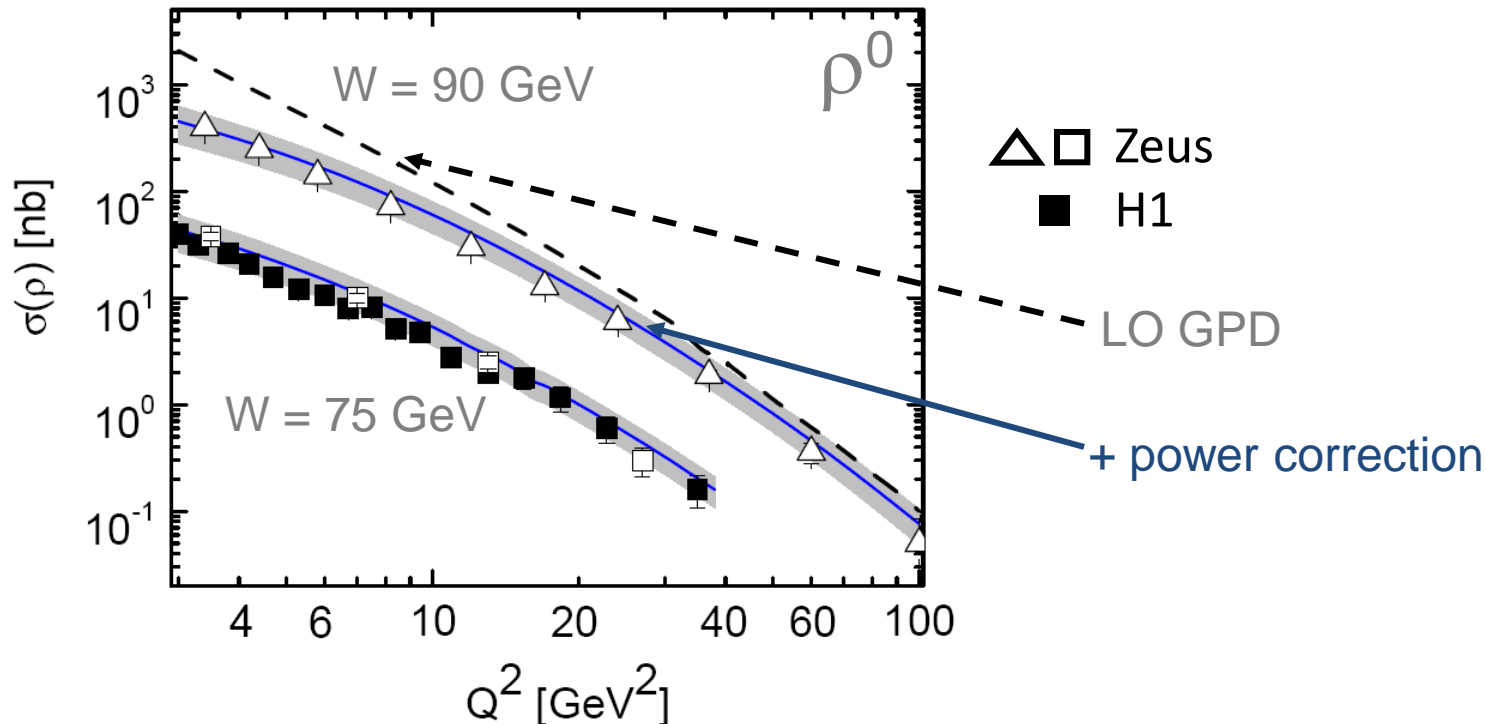
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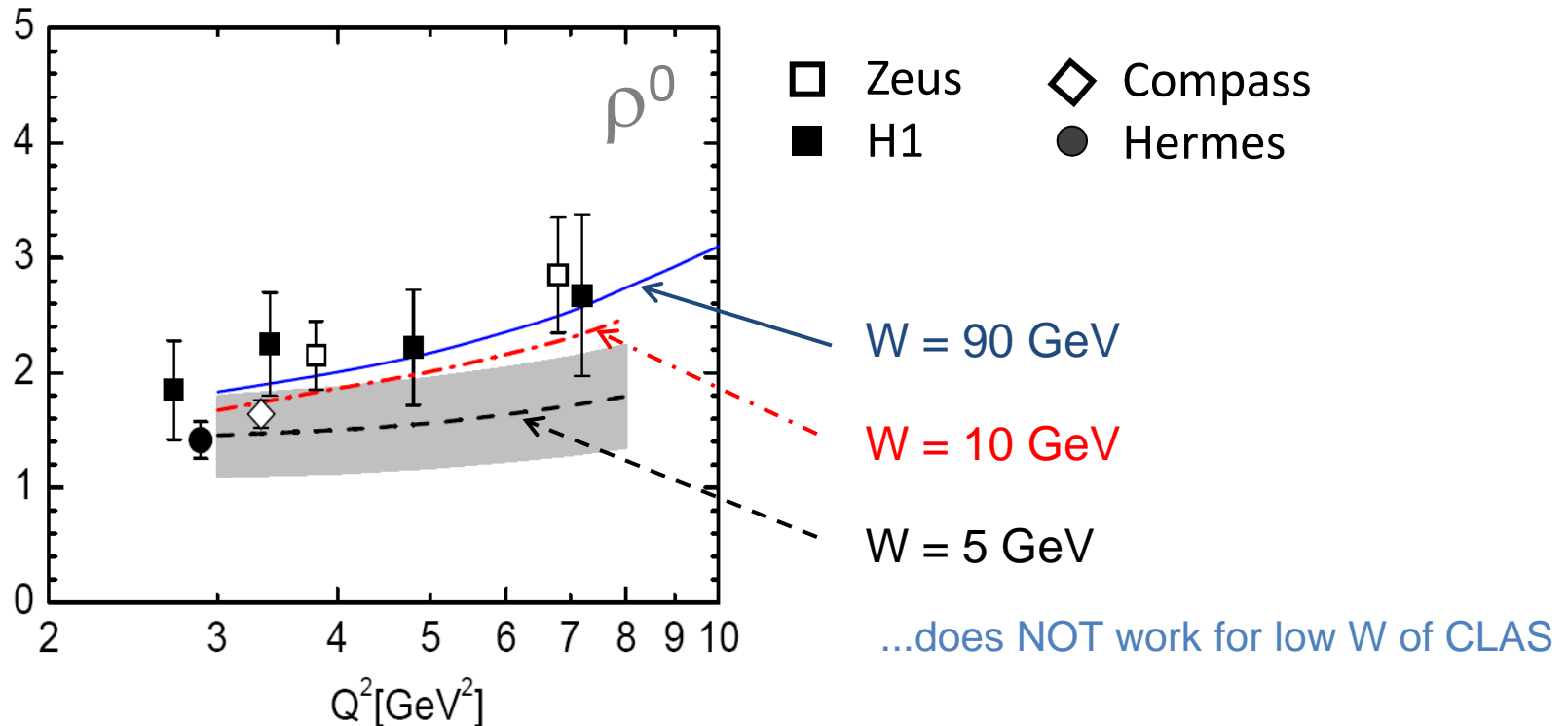
VM production: from low \rightarrow high x

- *NLO corrections* to VM production are *large* @ typical kinematics of COMPASS/ HERMES/ CLAS12 [M. Diehl, W. Kugler (2007)]
- ... *despite*, **LO GPD model** (handbag fact.; DD ansatz): [S. Goloskokov, P. Kroll (2007, 2010)]
+ power corrections



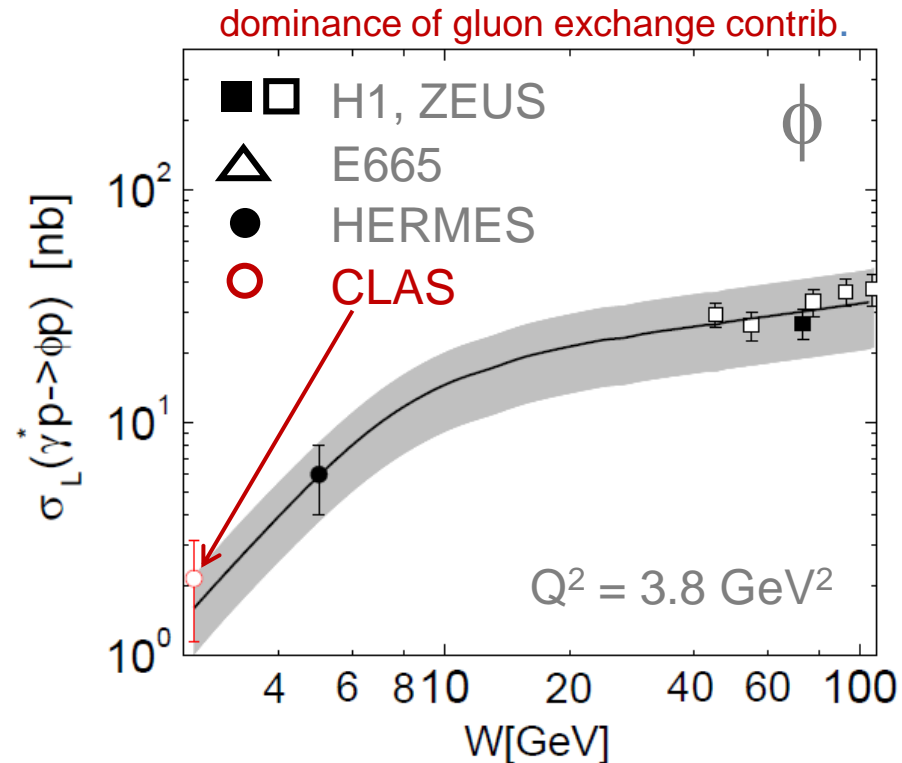
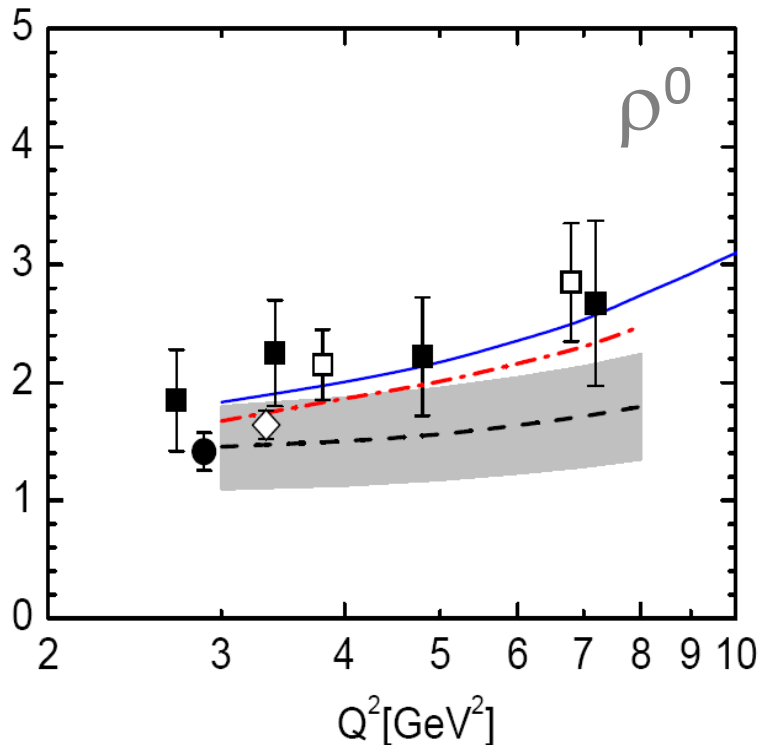
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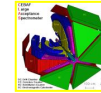
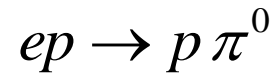
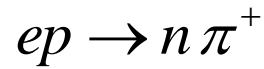
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ps meson production

-- role of power corrections & longitudinal-transverse transitions --



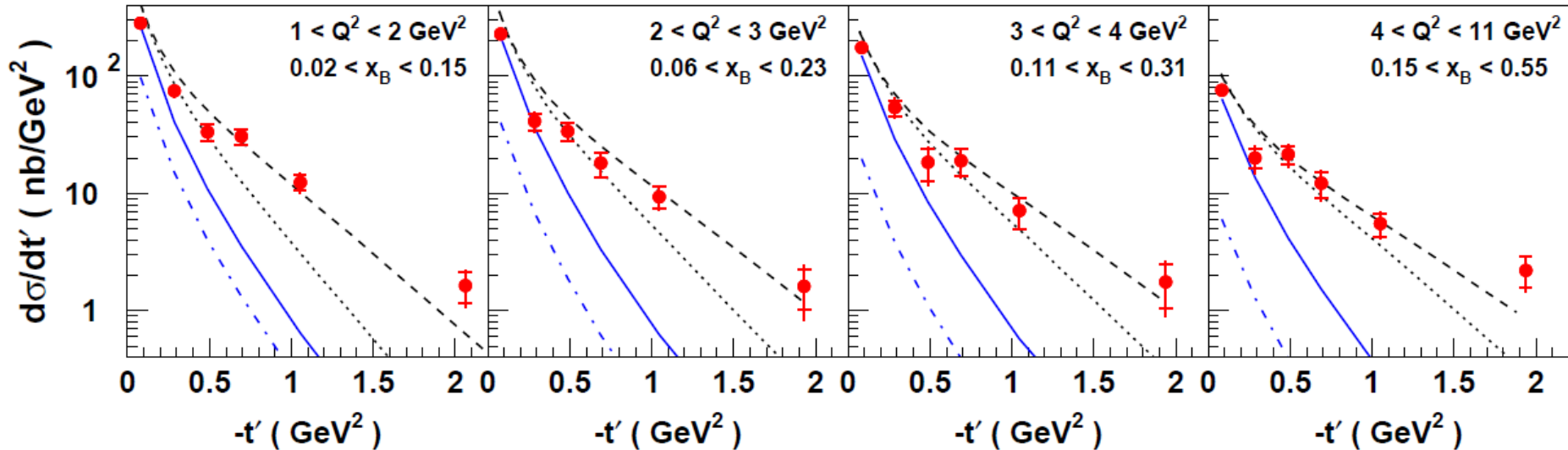
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-- role of power corrections & longitudinal-transverse transitions --



$$\gamma^* p \rightarrow n \pi^+$$

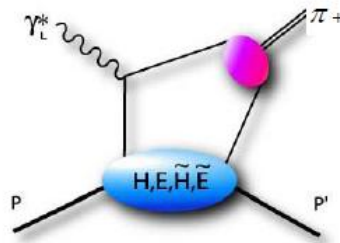
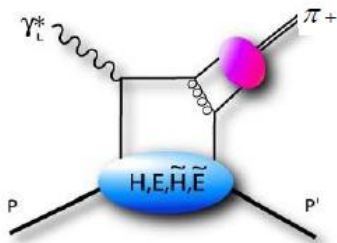
[PLB659(2008)]



GPD model for $\frac{d\sigma_L}{dt'}$

- · - leading-order calculations
- with power corrections

Vanderhaeghen, Guichon, Guidal [PRD60\(1999\)094017](#)



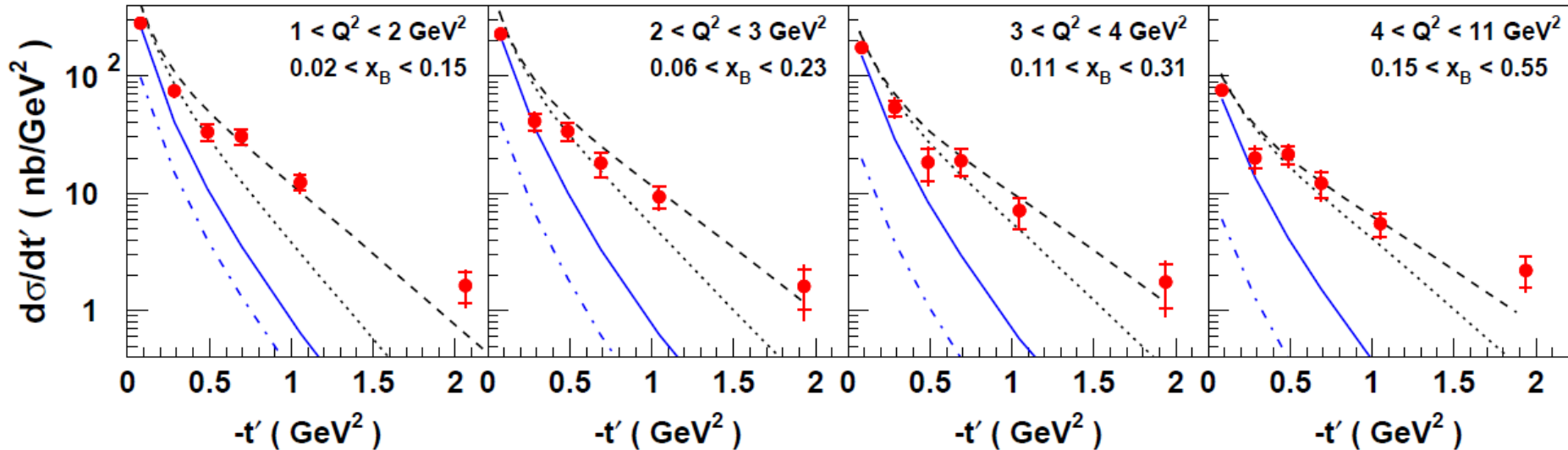
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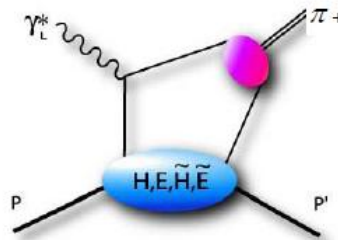
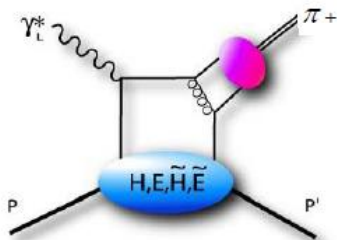
- dash-dotted blue line: leading-order calculations
- solid blue line: with power corrections

Vanderhaeghen, Guichon, Guidal PRD60(1999)094017

Regge model

----- σ_{tot}
 σ_L

[Laget(2008)]



→ need of L/T separation, especially for lower Q^2 , higher t

ps meson production

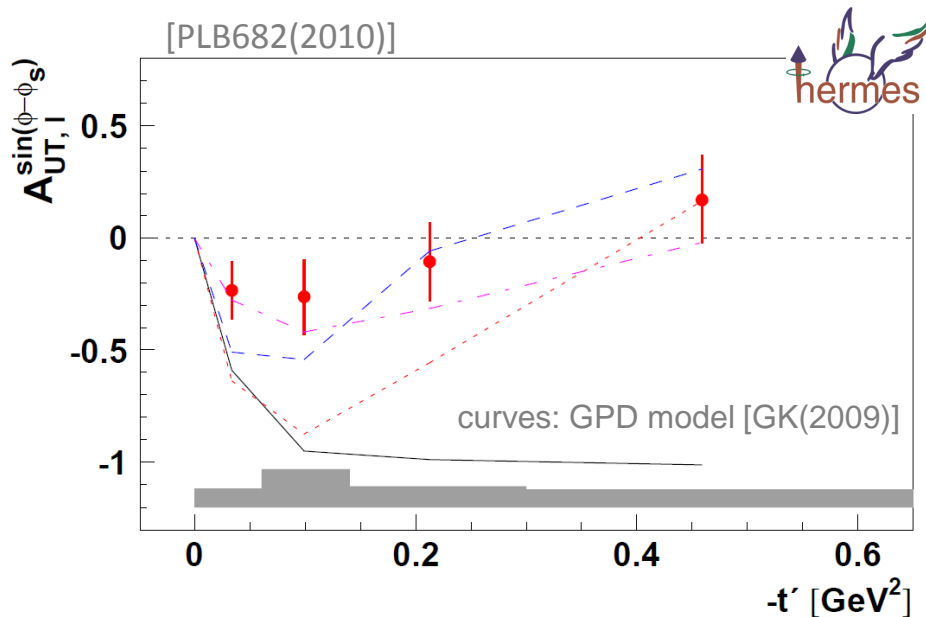
-- role of power corrections & longitudinal-transverse transitions --

$$ep \rightarrow n \pi^+$$

$$A_{UT}^{\sin(\phi-\phi_S)}$$

➤ arises from pure σ_L contribution

➤ NLO/power corrections cancel to large extent in asymmetry



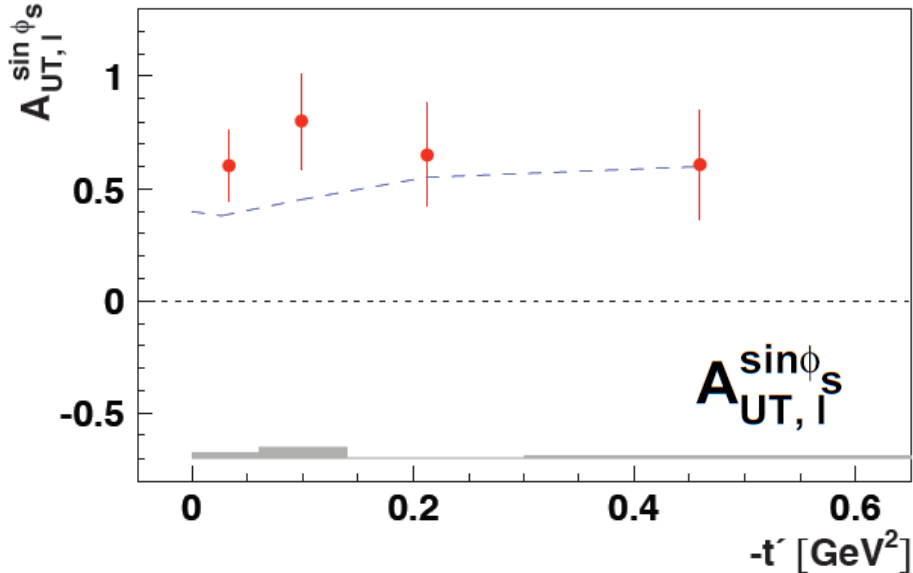
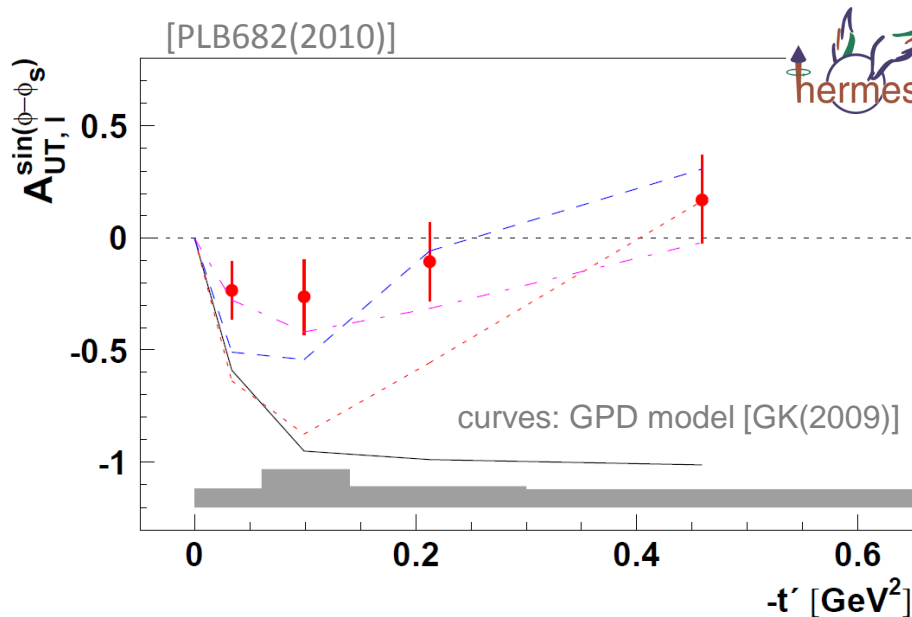
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→ significant contribution from L/T interference, need to go beyond leading-tw description

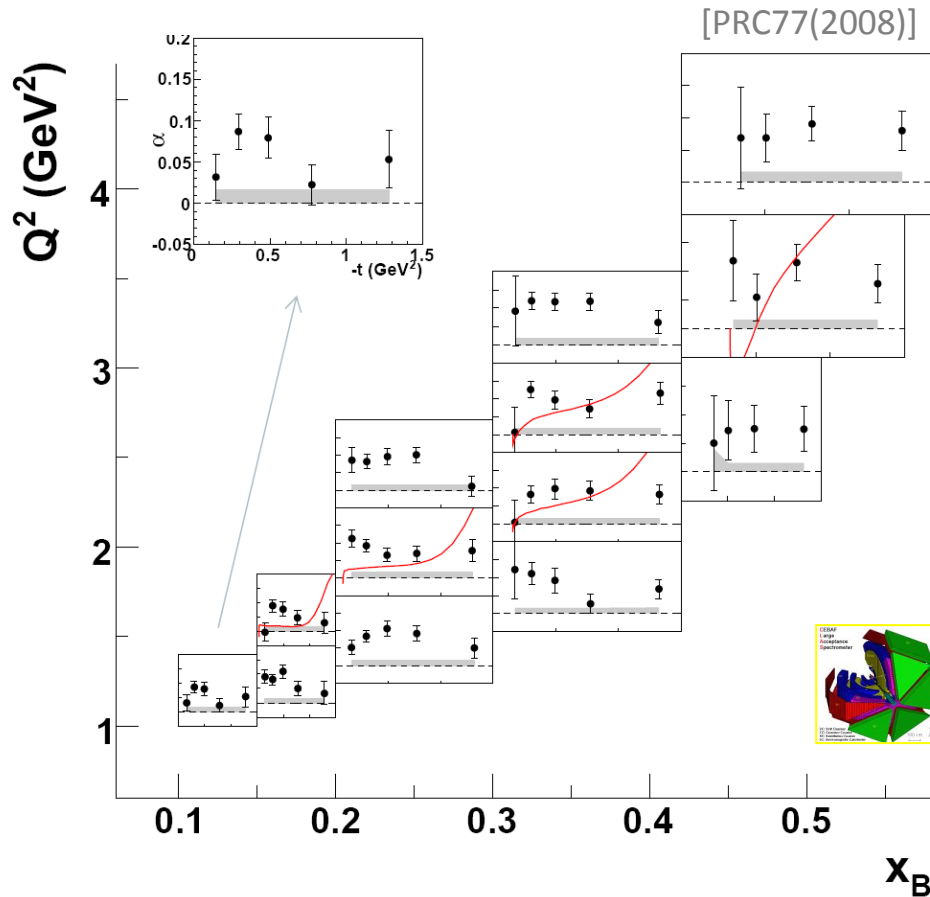
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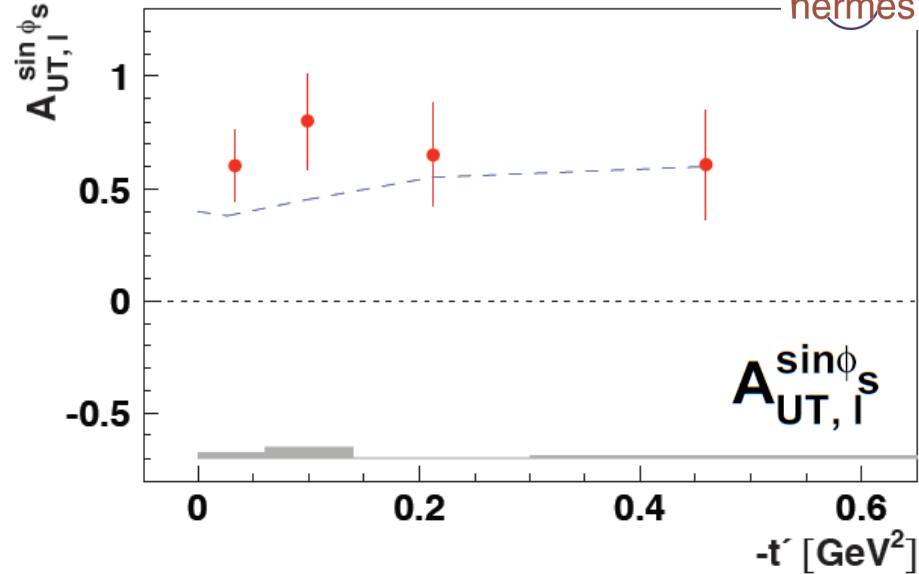
$$ep \rightarrow p \pi^0$$

$$A_{LU}^{\sin\phi}$$

➤ any non-zero beam-spin asymmetry indicates L-T interference



$$ep \rightarrow n \pi^+ \quad [\text{PLB682(2010)}]$$



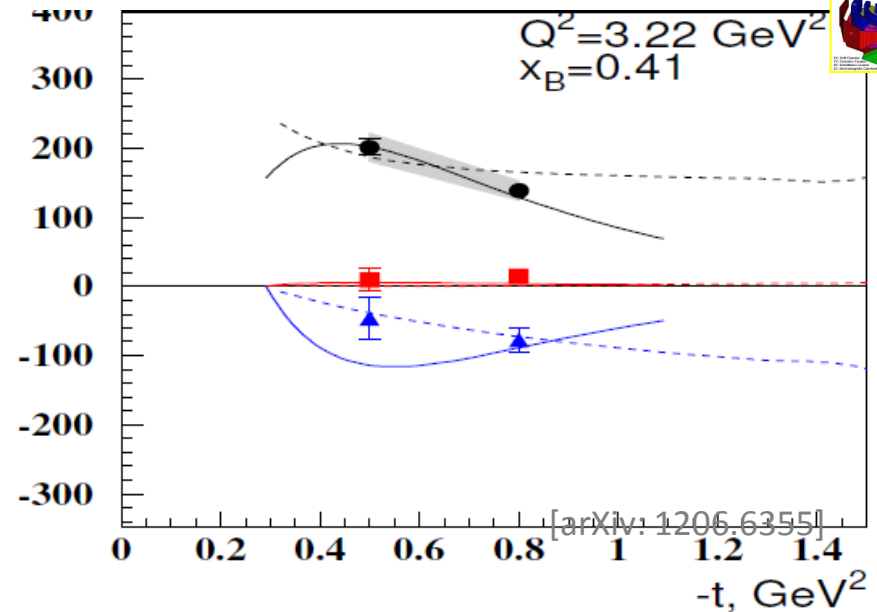
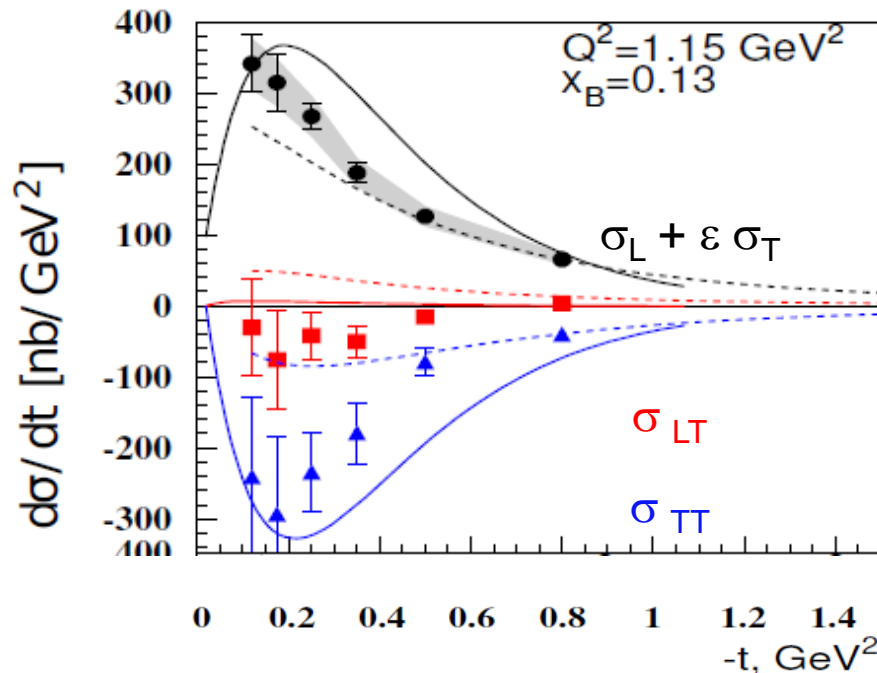
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ps meson production

-- role of transversity GPDs --

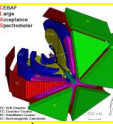
$$ep \rightarrow p \pi^0$$

- cross sections vs $t \rightarrow \sigma_T$ parametrized employing transversity GPDs (and assuming factorization) [Goldstein *etal.*(2011), Goloskokov and Kroll (2011)]

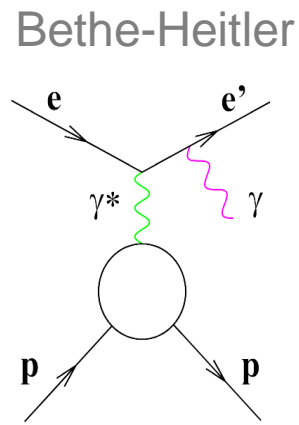
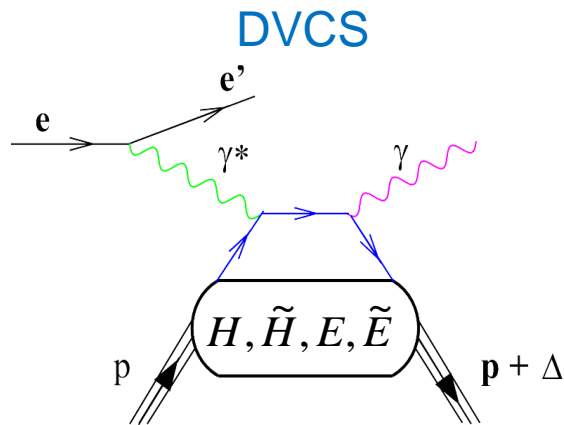


curves: GPD model calc.s with dominant contributions from transversity GPDs

- [Goloskokov Kroll(2011)]
- - - - - [Goldstein *etal.*(2011)]



Deeply virtual Compton Scattering

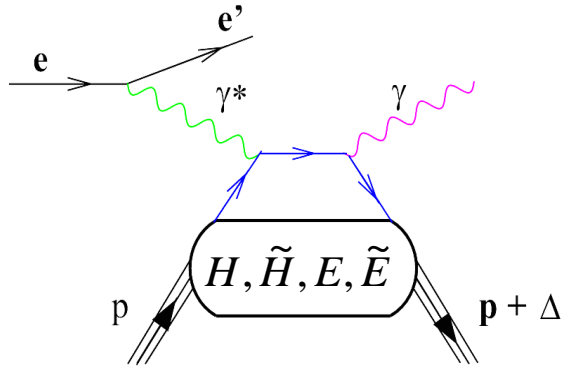


$$d\sigma \propto |\tau_{\text{BH}}|^2 + |\tau_{\text{DVCS}}|^2 + (\tau_{\text{BH}}^* \tau_{\text{DVCS}} + \tau_{\text{DVCS}}^* \tau_{\text{BH}})$$

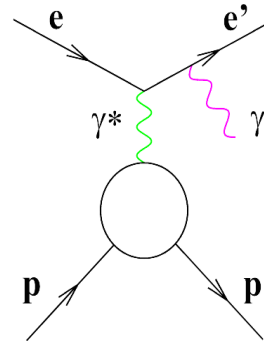
\rightarrow bilinear in GPDs \rightarrow linear in GPDs

Deeply virtual Compton Scattering

DVCS



Bethe-Heitler

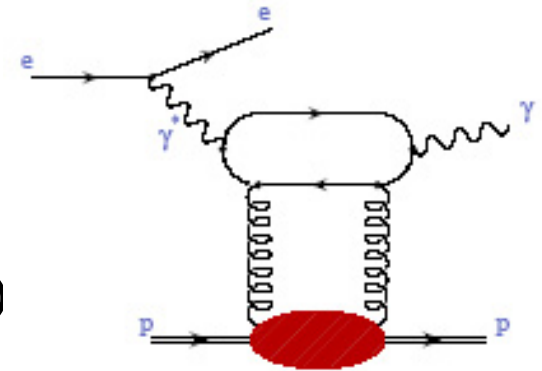


@H1&Zeus

DVCS \approx Bethe-Heitler

$$d\sigma \propto |\tau_{\text{BH}}|^2 + |\tau_{\text{DVCS}}|^2 + (\tau_{\text{BH}}^* \tau_{\text{DVCS}} + \tau_{\text{DVCS}}^* \tau_{\text{BH}})$$

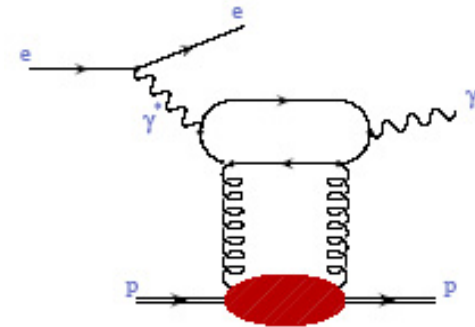
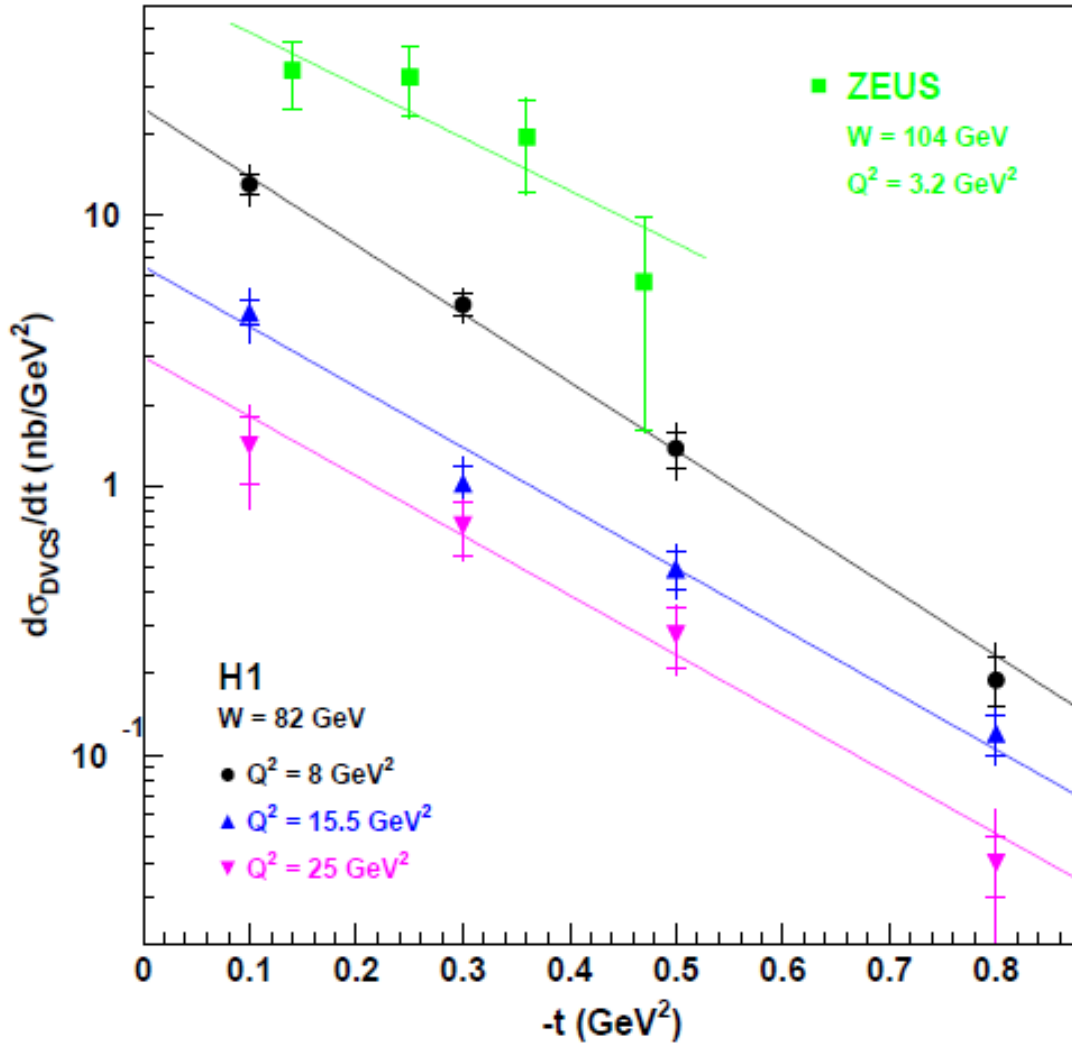
\rightarrow bilinear in GPDs \rightarrow linear in GPDs



LO sea quarks + NLO gluons



DVCS



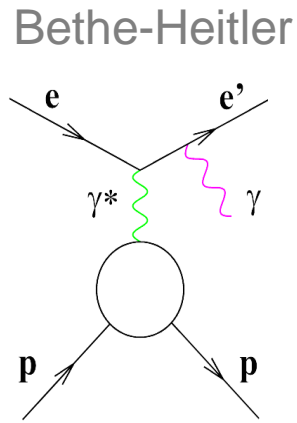
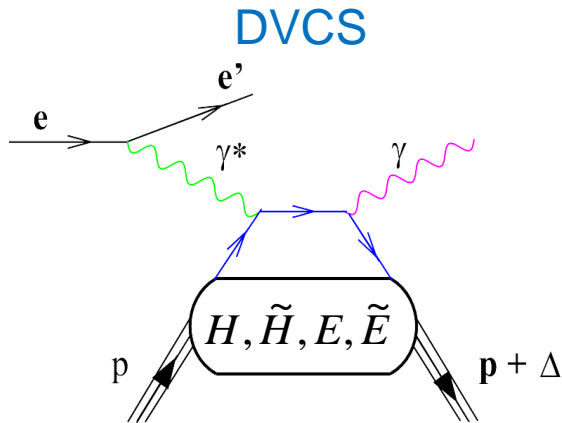
extracted transverse size (as before for VM) [H1, PLB659(2008)]

$$\sqrt{\langle b_T^2 \rangle} = (0.65 \pm 0.02) \text{ fm}$$

@ $x_B = 10^{-3}$

$\langle Q^2 \rangle = 8.0 \text{ GeV}^2$

DVCS



@H1&ZEUS

DVCS \approx Bethe-Heitler

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DVCS \ll Bethe-Heitler

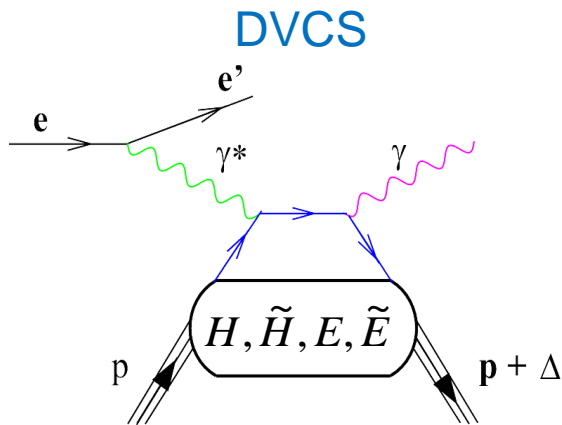
$$d\sigma \propto |\tau_{\text{BH}}|^2 + |\tau_{\text{DVCS}}|^2 + (\tau_{\text{BH}}^* \tau_{\text{DVCS}} + \tau_{\text{DVCS}}^* \tau_{\text{BH}})$$

\rightarrow bilinear in GPDs

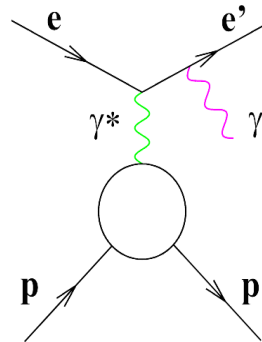
\rightarrow linear in GPDs, information about *phase*

\rightarrow access to *Re* and *Im* parts of *CFFs*

DVCS



Bethe-Heitler



@H1&ZEUS

DVCS \approx Bethe-Heitler

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DVCS \ll Bethe-Heitler

$$d\sigma \propto |\tau_{\text{BH}}|^2 + |\tau_{\text{DVCS}}|^2 + (\tau_{\text{BH}}^* \tau_{\text{DVCS}} + \tau_{\text{DVCS}}^* \tau_{\text{BH}})$$

\rightarrow bilinear in GPDs

\rightarrow linear in GPDs, information about *phase*

isolate interference term:

- different beam charges: e^+e^- **only @HERA**, upcoming @COMPASS

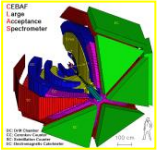
- polarisation observables:

$$\Delta\sigma_{\text{UT}}$$

beam target

U, L U, L, T

Un polarised, **L**ongitudinally, **T**ransversely polarised



DVCS interference term



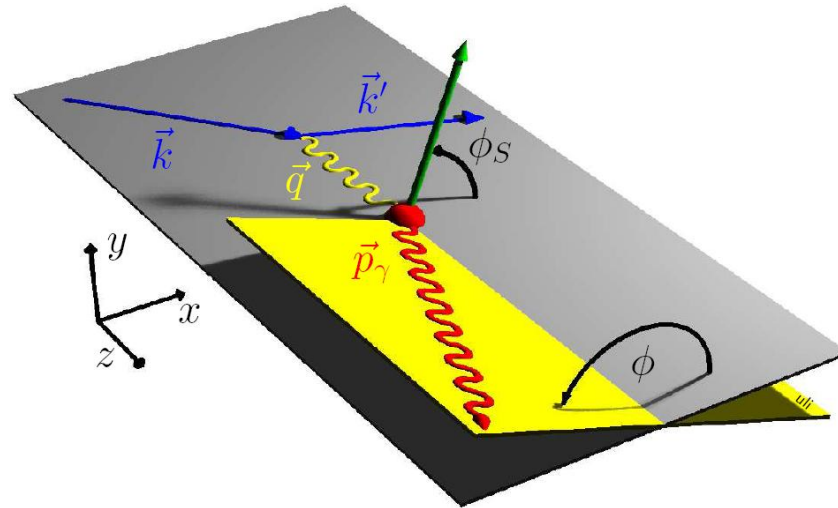
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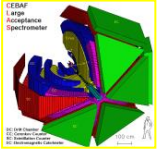
- different beam charges: e^+e^- only @HERA, upcoming @COMPASS
- polarisation observables:

$$\Delta\sigma_{\text{UT}}(\phi, \phi_S, \dots)$$

↙	↘
beam	target
U, L	U, L, T

Unpolarised,
Longitudinally,
Transversely polarised





DVCS interference term



$$d\sigma \propto |\tau_{BH}|^2 + |\tau_{DVCS}|^2 + (\tau_{BH}^* \tau_{DVCS} + \tau_{DVCS}^* \tau_{BH})$$

DVCS cross section in full glory:

[M. Diehl]

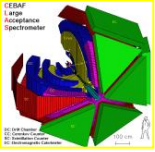
$$d\sigma(\ell p \rightarrow \ell \gamma p) \sim$$

$$\begin{aligned} & d\sigma_{UU}^{BH} + e_\ell d\sigma_{UU}^I + d\sigma_{UU}^{DVCS} \\ & + P_\ell S_L d\sigma_{LL}^{BH} + e_\ell P_\ell S_L d\sigma_{LL}^I + P_\ell S_L d\sigma_{LL}^{DVCS} \\ & + P_\ell S_T d\sigma_{LT}^{BH} + e_\ell P_\ell S_T d\sigma_{LT}^I + P_\ell S_T d\sigma_{LT}^{DVCS} \\ & + e_\ell P_\ell d\sigma_{LU}^I + P_\ell d\sigma_{LU}^{DVCS} \\ & + e_\ell S_L d\sigma_{UL}^I + S_L d\sigma_{UL}^{DVCS} \\ & + e_\ell S_T d\sigma_{UT}^I + S_T d\sigma_{UT}^{DVCS}. \end{aligned}$$

e_ℓ beam charge

P_ℓ longitudinal beam polarisation

$S_L S_T$ Longitudinal or transverse target polarisation



DVCS interference term



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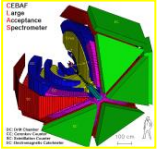
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DVCS interference term



$$d\sigma \propto |\tau_{\text{BH}}|^2 + |\tau_{\text{DVCS}}|^2 + (\tau_{\text{BH}}^* \tau_{\text{DVCS}} + \tau_{\text{DVCS}}^* \tau_{\text{BH}})$$

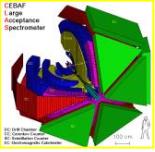
DVCS cross section in full glory: [M. Diehl] $d\sigma(\ell p \rightarrow \ell \gamma p) \sim$

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fourier coefficients c_n and s_n provide experimental constrain on CFFs

example:

$$d\sigma_{LU}^I \propto -e_\ell \left(\sum_{n=0}^3 c_n^I \cos(n\phi) + \lambda \sum_{n=1}^2 s_n^I \sin(n\phi) \right)$$



DVCS interference term



$$d\sigma \propto |\tau_{\text{BH}}|^2 + |\tau_{\text{DVCS}}|^2 + (\tau_{\text{BH}}^* \tau_{\text{DVCS}} + \tau_{\text{DVCS}}^* \tau_{\text{BH}})$$

DVCS cross section in full glory: [M. Diehl] $d\sigma(\ell p \rightarrow \ell \gamma p) \sim$

$$\begin{aligned} & d\sigma_{UU}^{\text{BH}} + e_\ell d\sigma_{UU}^{\text{I}} + d\sigma_{UU}^{\text{DVCS}} \\ & + P_\ell S_L d\sigma_{LL}^{\text{BH}} + e_\ell P_\ell S_L d\sigma_{LL}^{\text{I}} + P_\ell S_L d\sigma_{LL}^{\text{DVCS}} \\ & + P_\ell S_T d\sigma_{LT}^{\text{BH}} + e_\ell P_\ell S_T d\sigma_{LT}^{\text{I}} + P_\ell S_T d\sigma_{LT}^{\text{DVCS}} \\ & + e_\ell P_\ell d\sigma_{LU}^{\text{I}} + P_\ell d\sigma_{LU}^{\text{DVCS}} \\ & + e_\ell S_L d\sigma_{UL}^{\text{I}} + S_L d\sigma_{UL}^{\text{DVCS}} \\ & + e_\ell S_T d\sigma_{UT}^{\text{I}} + S_T d\sigma_{UT}^{\text{DVCS}}. \end{aligned}$$

fourier coefficients c_n and s_n provide experimental constrain on CFFs

example:

$$d\sigma_{LU}^{\text{I}} \propto -e_\ell \left(\sum_{n=0}^3 c_n^{\text{I}} \cos(n\phi) + \lambda \sum_{n=1}^2 s_n^{\text{I}} \sin(n\phi) \right)$$

accessible linear combinations of CFFs, hence GPDs :

$$d\sigma_{LU}^{\text{I}} \propto F_1 \underset{\downarrow}{\textcircled{H}} + \frac{x_{\text{Bj}}}{2 - x_{\text{Bj}}} (F_1 + F_2) \tilde{H} - \frac{t}{4M^2} F_2 \underset{\downarrow}{\textcircled{E}} + \dots$$

dominant contribution for proton

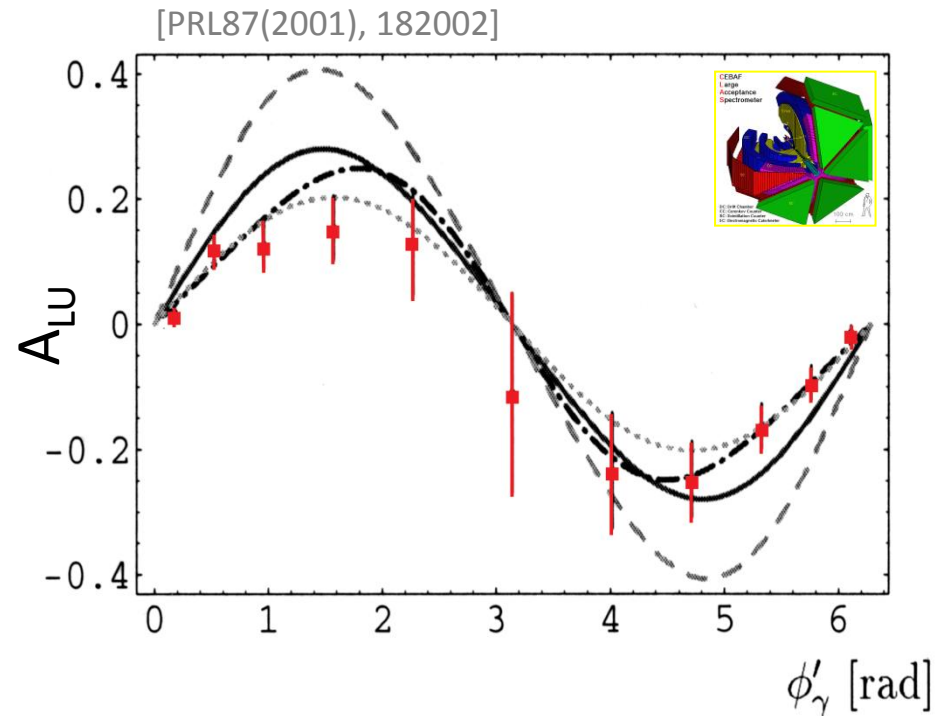
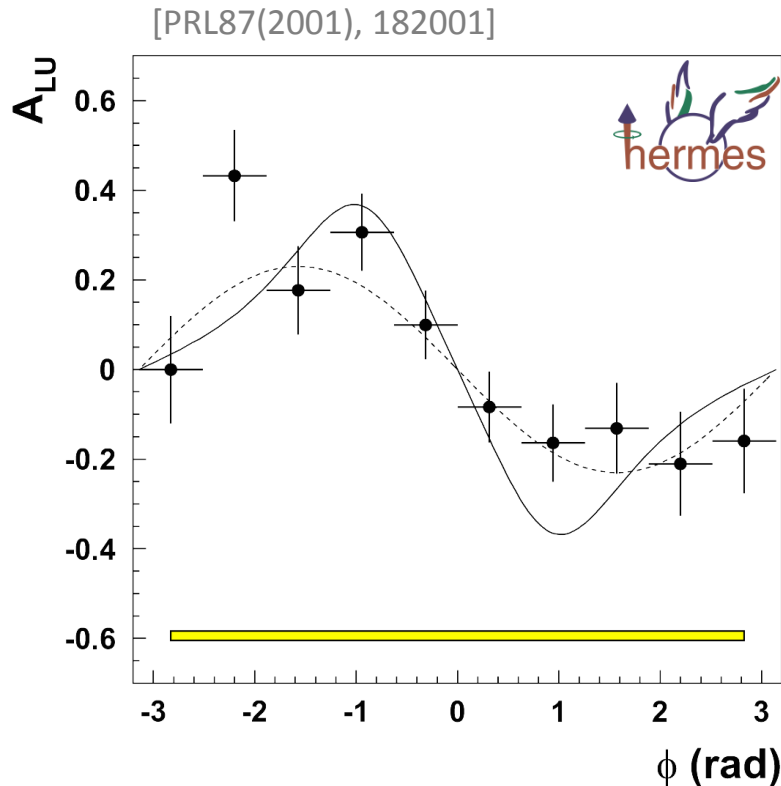
for neutron

$F_1, F_2 \dots$ Pauli & Dirac FF

first DVCS signals

-- interference term --

$$A_{LU} \sim \frac{(BH) * \text{Im}(DVCS) * \sin\phi}{(BH^2 + DVCS^2)}$$



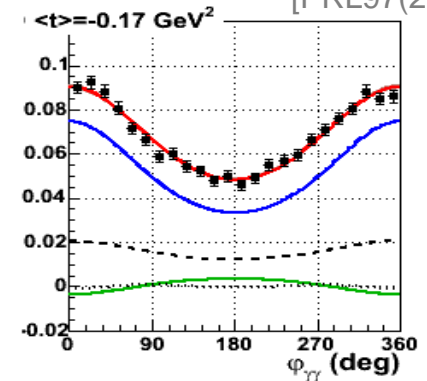
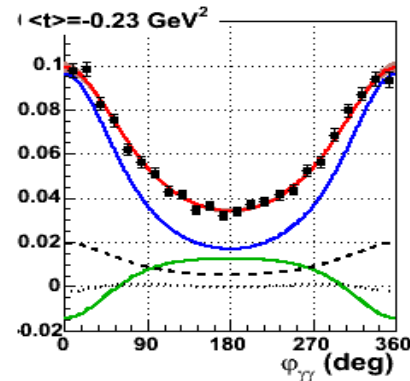
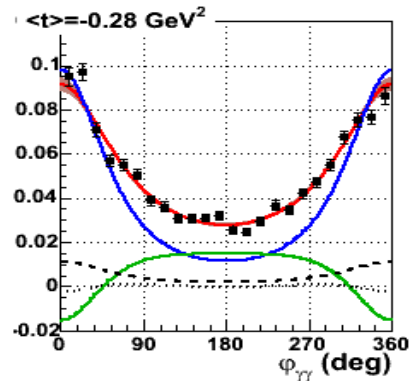
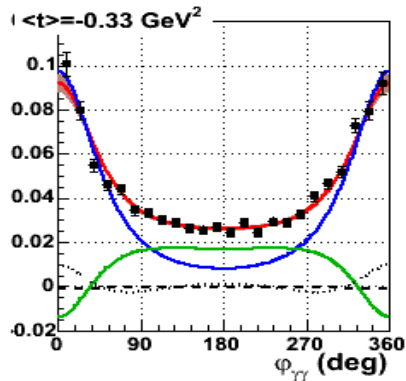
→ $\sin\phi$ dependence indicates dominance of handback contribution

call for high statistics

$$d\sigma \propto |\tau_{\text{BH}}|^2 + |\tau_{\text{DVCS}}|^2 + (\tau_{\text{BH}}^* \tau_{\text{DVCS}} + \tau_{\text{DVCS}}^* \tau_{\text{BH}})$$

 σ_{UU}

$$\frac{d^4\sigma}{dQ^2 dx_B dt d\phi_{\gamma\gamma}} \text{ (nb/GeV}^4\text{)}$$



[PRL97(2006)]

 ϕ

— BH

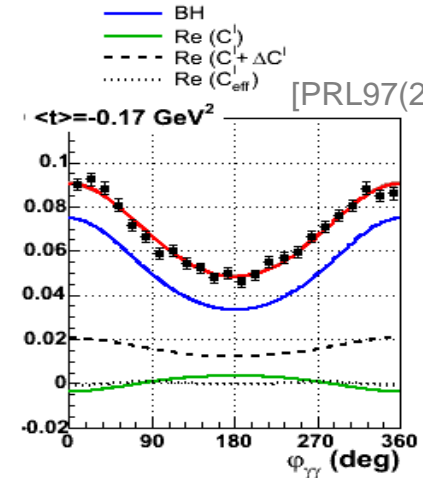
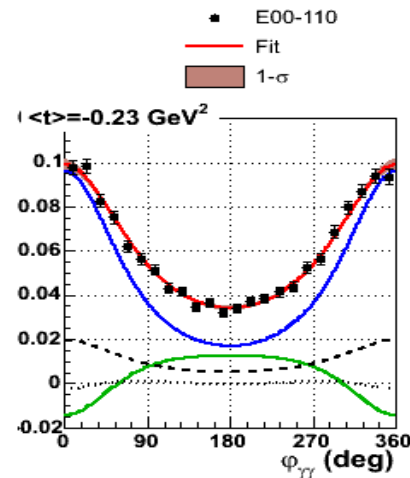
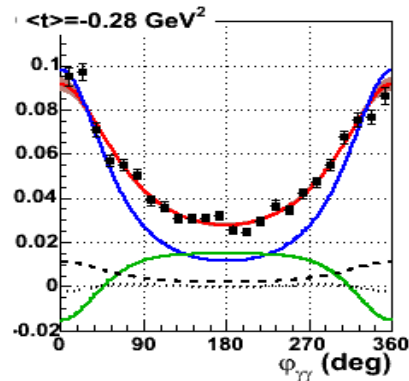
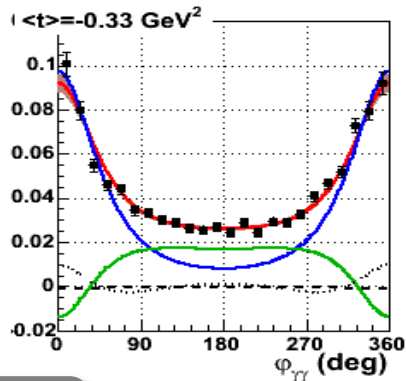
— DVCS [GPD model: VGG(1999)]

call for high statistics

$$d\sigma \propto |\tau_{\text{BH}}|^2 + |\tau_{\text{DVCS}}|^2 + (\tau_{\text{BH}}^* \tau_{\text{DVCS}} + \tau_{\text{DVCS}}^* \tau_{\text{BH}})$$

 σ_{UU}

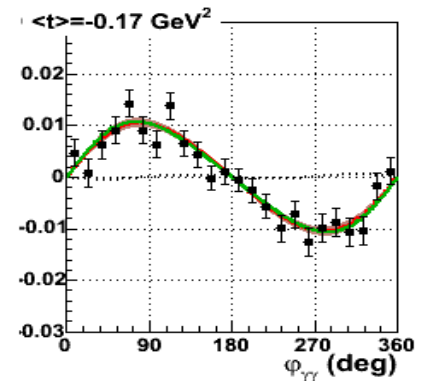
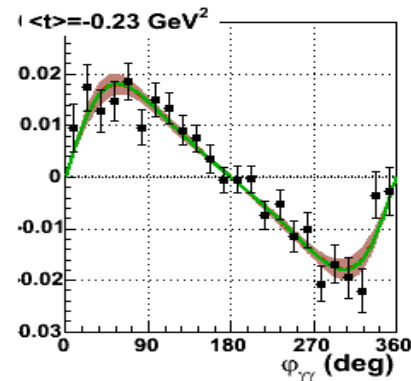
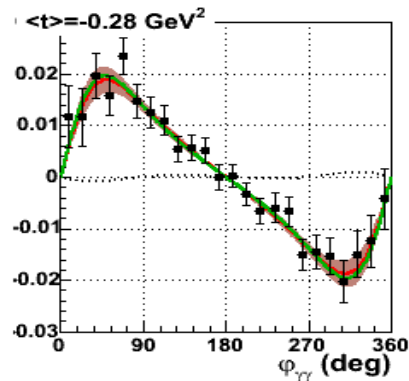
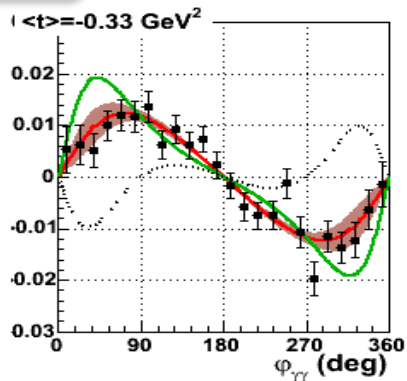
$$\frac{d^4\sigma}{dQ^2 dx_B dt d\phi_{\gamma\gamma}} \text{ (nb/GeV}^4\text{)}$$



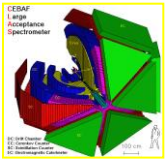
[PRL97(2006)]

 $\Delta\sigma_{\text{LU}}$

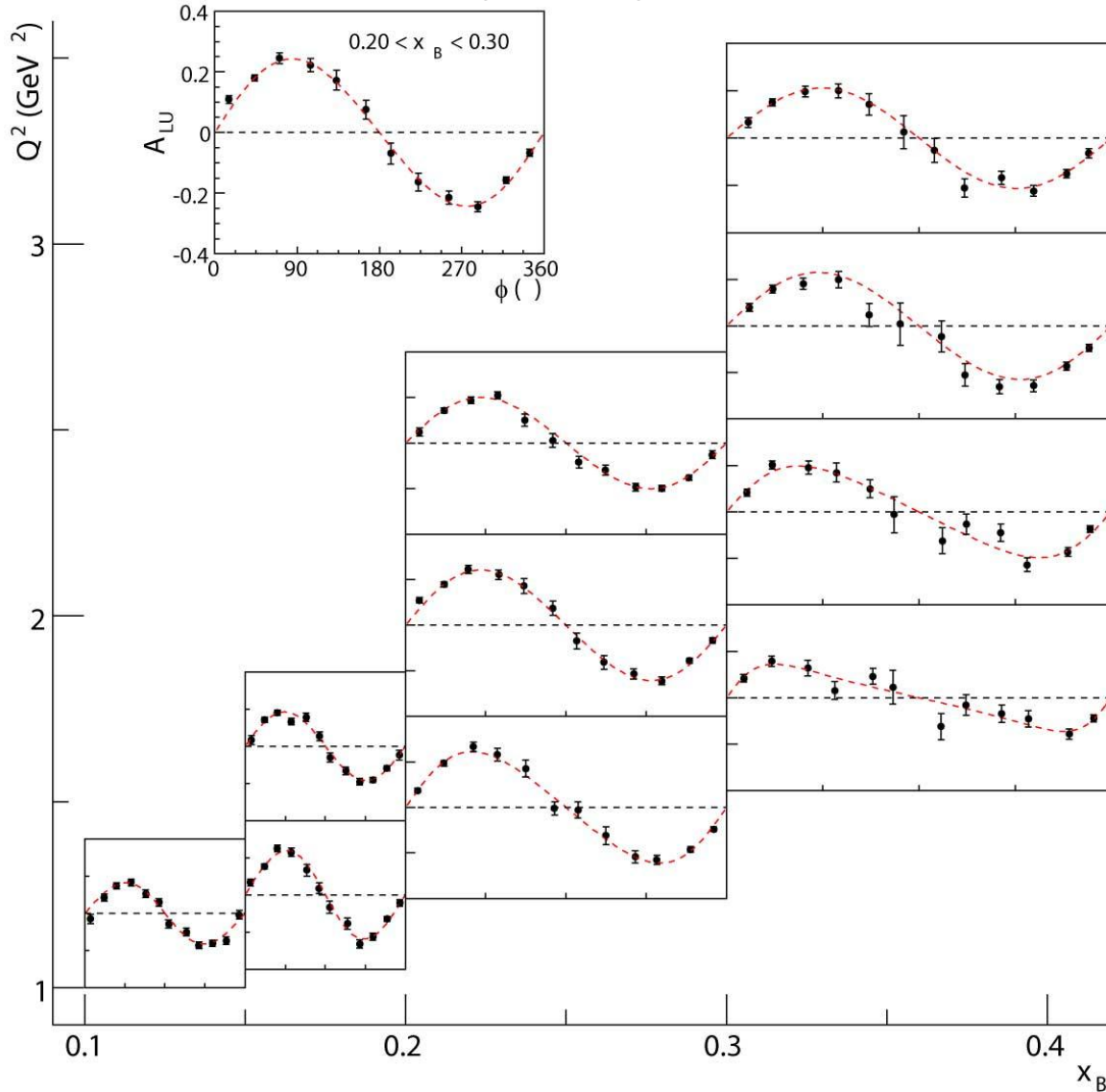
$$\frac{1}{2} \left(\frac{d^4\sigma^+}{dQ^2 dx_B dt d\phi_{\gamma\gamma}} - \frac{d^4\sigma^-}{dQ^2 dx_B dt d\phi_{\gamma\gamma}} \right) \text{ (nb/GeV}^4\text{)}$$



call for high statistics



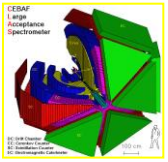
DVCS beam-spin asymmetry [PRL100(2008)]



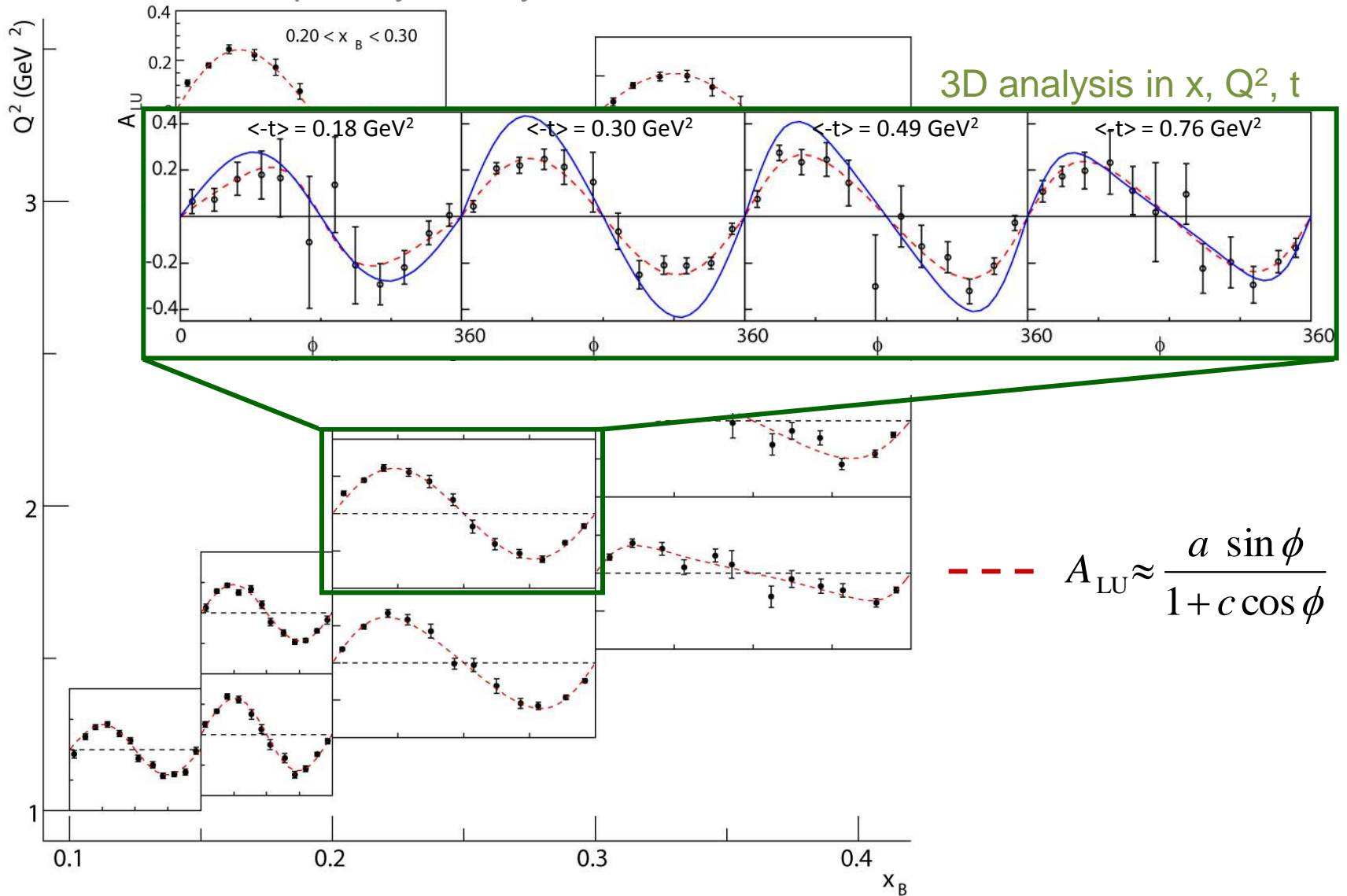
$$A_{LU} \sim \frac{(\text{BH}) * \text{Im}(\text{DVCS}) * \sin\phi}{(\text{BH}^2 + \text{DVCS}^2)}$$

--- $A_{LU} \approx \frac{a \sin\phi}{1 + c \cos\phi}$

call for high statistics



DVCS beam-spin asymmetry [PRL100(2008)]



call for new analysis methods



$$d\sigma \propto |\tau_{\text{BH}}|^2 + |\tau_{\text{DVCS}}|^2 + (\tau_{\text{BH}}^* \tau_{\text{DVCS}} + \tau_{\text{DVCS}}^* \tau_{\text{BH}})$$

combined analysis of **charge & polarisation** observables

→ separation of *Interference* & *DVCS²* amplitudes

call for new analysis methods



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combined analysis of **charge & polarisation** observables

→ separation of *Interference* & *DVCS²* amplitudes

e.g., beam-spin asymmetry:

$$\sigma_{LU}(\phi, P_l, e_l) = \sigma_{UU}(\phi) \cdot \left\{ 1 + P_l A_{LU}^{DVCS}(\phi) + e_l P_l A_{LU}^I(\phi) + e_l A_C(\phi) \right\}$$

call for new analysis methods



$$d\sigma \propto |\tau_{\text{BH}}|^2 + |\tau_{\text{DVCS}}|^2 + (\tau_{\text{BH}}^* \tau_{\text{DVCS}} + \tau_{\text{DVCS}}^* \tau_{\text{BH}})$$

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- *charged-averaged* beam-spin asymmetry:

$$A_{LU}^{DVCS}(\phi) = (\sigma^{+\rightarrow} - \sigma^{+\leftarrow}) + (\sigma^{-\rightarrow} - \sigma^{-\leftarrow}) / \Sigma \quad \propto s_1^{DVCS} \sin \phi$$

call for new analysis methods



$$d\sigma \propto |\tau_{\text{BH}}|^2 + |\tau_{\text{DVCS}}|^2 + (\tau_{\text{BH}}^* \tau_{\text{DVCS}} + \tau_{\text{DVCS}}^* \tau_{\text{BH}})$$

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$$A_{LU}^{DVCS}(\phi) = (\sigma^{+\rightarrow} - \sigma^{+\leftarrow}) + (\sigma^{-\rightarrow} - \sigma^{-\leftarrow}) / \Sigma \quad \propto s_1^{DVCS} \sin \phi$$

- *charge-difference* beam-spin asymmetry:

$$A_{LU}^{DVCS}(\phi) = (\sigma^{+\rightarrow} - \sigma^{+\leftarrow}) - (\sigma^{-\rightarrow} - \sigma^{-\leftarrow}) / \Sigma \quad \propto \sum_{n=1}^2 s_n^I \sin(n\phi) \rightarrow \text{Im}(CFF)$$

call for new analysis methods



$$d\sigma \propto |\tau_{\text{BH}}|^2 + |\tau_{\text{DVCS}}|^2 + (\tau_{\text{BH}}^* \tau_{\text{DVCS}} + \tau_{\text{DVCS}}^* \tau_{\text{BH}})$$

combined analysis of **charge & polarisation** observables

→ separation of *Interference* & *DVCS*² amplitudes

e.g., beam-spin asymmetry:

$$\sigma_{LU}(\phi; P_l, e_l) = \sigma_{UU}(\phi) \cdot \left\{ 1 + P_l A_{LU}^{DVCS}(\phi) + e_l P_l A_{LU}^I(\phi) + e_l A_C(\phi) \right\}$$

- *charged-averaged* beam-spin asymmetry:

$$A_{LU}^{DVCS}(\phi) = (\sigma^{+\rightarrow} - \sigma^{+\leftarrow}) + (\sigma^{-\rightarrow} - \sigma^{-\leftarrow}) / \Sigma \quad \propto s_1^{DVCS} \sin \phi$$

- *charge-difference* beam-spin asymmetry:

$$A_{LU}^{DVCS}(\phi) = (\sigma^{+\rightarrow} - \sigma^{+\leftarrow}) - (\sigma^{-\rightarrow} - \sigma^{-\leftarrow}) / \Sigma \quad \propto \sum_{n=1}^2 s_n^I \sin(n\phi) \rightarrow \text{Im}(CFF)$$

- beam-spin averaged *charge* asymmetry:

$$A_C(\phi) = (\sigma^{+\rightarrow} + \sigma^{+\leftarrow}) - (\sigma^{-\rightarrow} + \sigma^{-\leftarrow}) / \Sigma \quad \propto \sum_{n=0}^3 c_n^I \cos(n\phi) \rightarrow \text{Re}(CFF)$$

call for new analysis methods

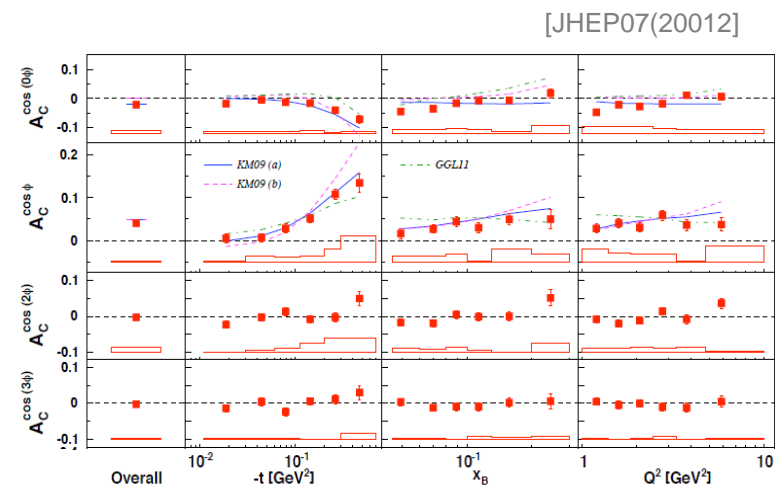
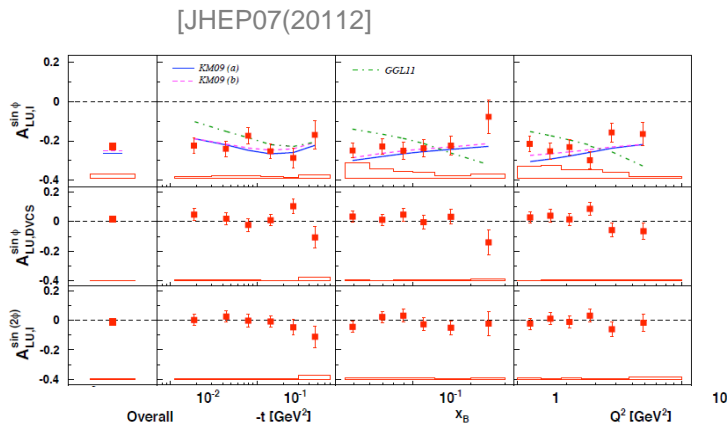


$$d\sigma \propto |\tau_{BH}|^2 + |\tau_{DVCS}|^2 + (\tau_{BH}^* \tau_{DVCS} + \tau_{DVCS}^* \tau_{BH})$$

combined analysis of **charge & polarisation** observables

→ separation of *Interference & DVCS²* amplitudes

$$\sigma_{LU}(\phi; P_l, e_l) = \sigma_{UU}(\phi) \cdot \left\{ 1 + \underbrace{P_l}_{s_1^{DVCS} \sin \phi} A_{LU}^{DVCS}(\phi) + \underbrace{e_l P_l}_{\sum_{n=1}^2 s_n^I \sin(n\phi)} A_{LU}^I(\phi) + \underbrace{e_l}_{\sum_{n=0}^3 c_n^I \cos(n\phi)} A_C(\phi) \right\}$$

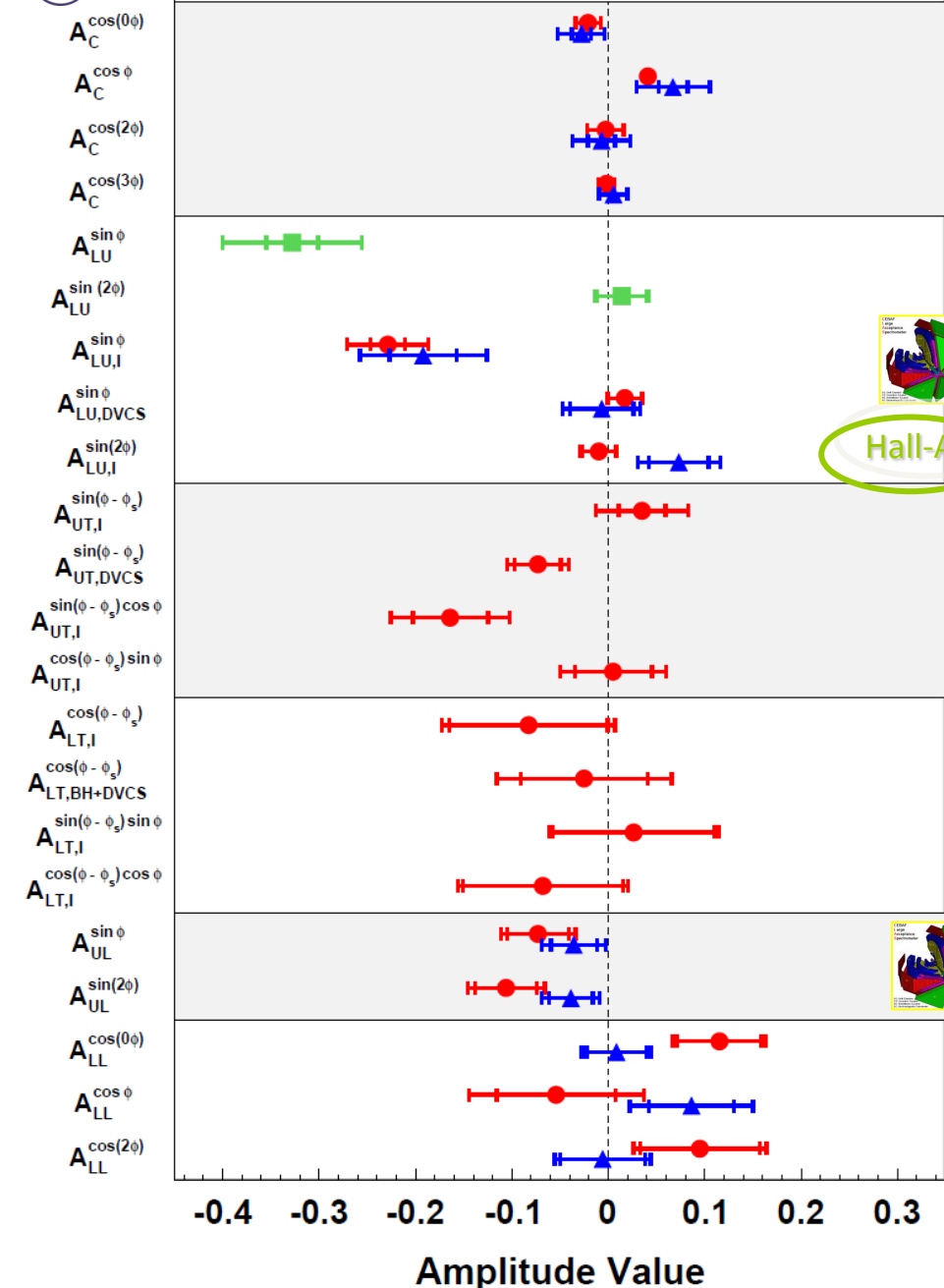




HERMES DVCS

- Hydrogen
- ▲ Deuterium
- Hydrogen Pure

call for completeness



Hall-A

→ charge asymmetry

$$Re(H)$$

→ beam-spin asymmetry

$$Im(H)$$

→ transverse target spin asymmetry

$$Im(H-E)$$

→ transverse-target double-spin

$$Re(H-E)$$

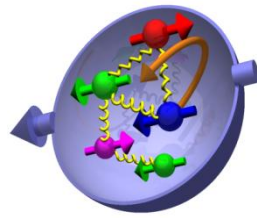
→ longitudinal target spin asymm.

$$Im(\tilde{H})$$

→ longitudinal-target double-spin

$$Re(\tilde{H})$$

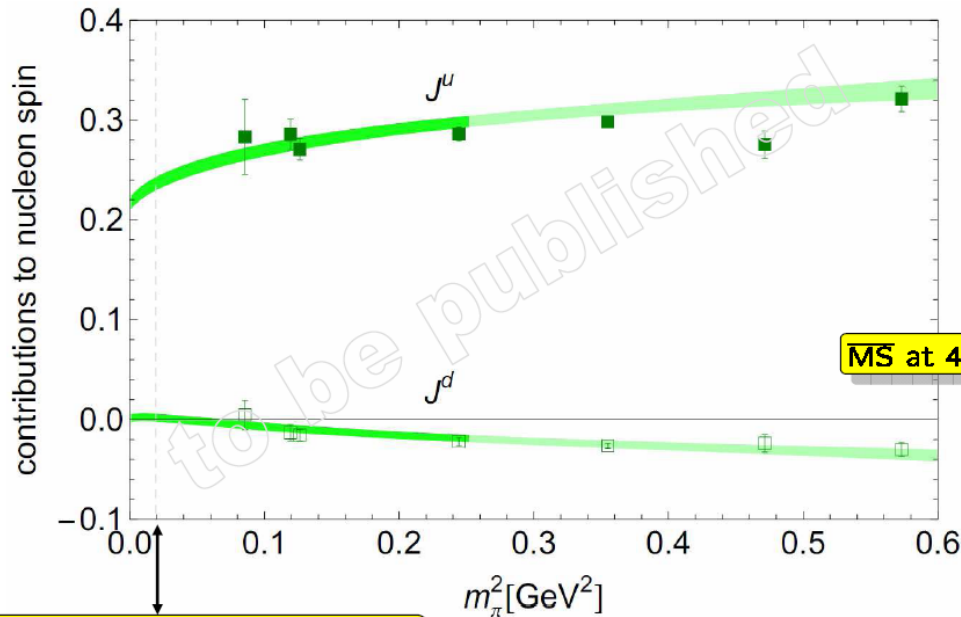
hunting the OAM



$$\frac{1}{2} = J^q + J^g, \quad J^{q,g} = \frac{1}{2} \int_{-1}^1 x dx \left[H^{q,g}(x, \xi, t) + E^{q,g}(x, \xi, t) \right]_{t=0}$$

➤ lattice results:

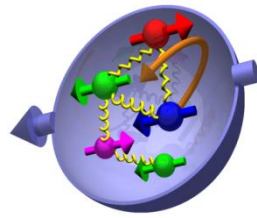
[P. Hägler et al.(2011)]



$J^u = 0.236(6) \approx 47\%$ of $1/2$
 $J^d = 0.0018(37) \approx 1\%$ of $1/2$

$J^{u+d} \approx 0.238 \pm 0.008 \approx 48\%$ of $1/2$

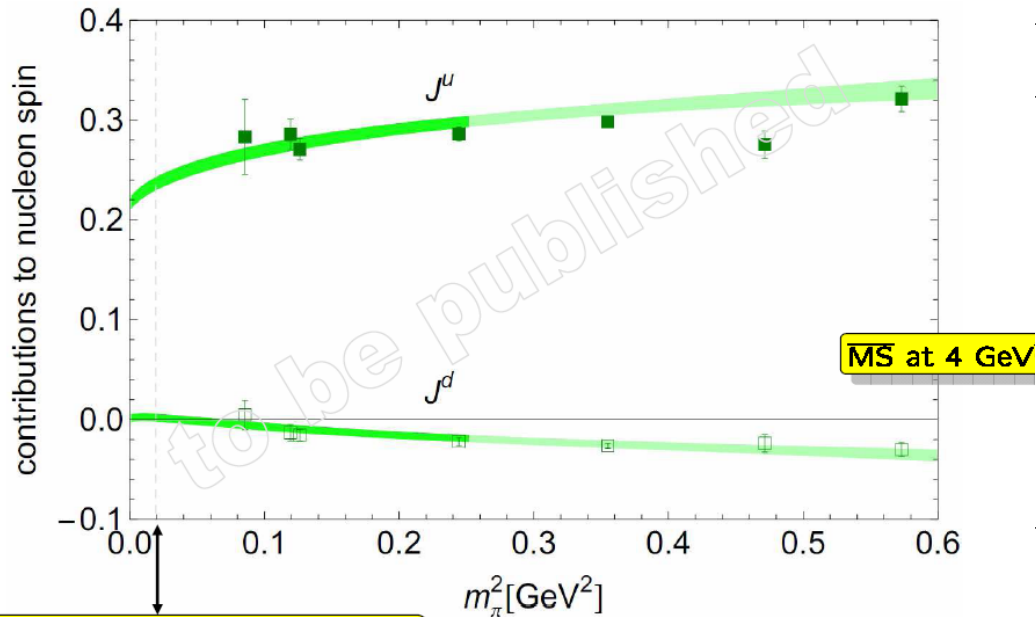
hunting the OAM



$$\frac{1}{2} = J^q + J^g, \quad J^{q,g} = \frac{1}{2} \int_{-1}^1 x dx \left[H^{q,g}(x, \xi, t) + E^{q,g}(x, \xi, t) \right]_{t=0}$$

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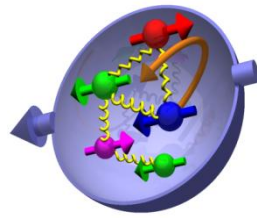
➤ GPD model tuned to VM:

[Goloskokov, Kroll(2008)]

J^u	J^d	J^s	J^g
0.250	0.020	0.015	0.214
0.276	0.046	0.041	0.132
0.225	-0.005	-0.011	0.286
0.209	0.013	0.015	0.257
0.230	0.024	0.015	0.228
0.234	0.028	0.019	0.214

variants for GPD E

hunting the OAM



→ GPD models: J^q free parameter in ansatz for E

$$J^q = \frac{1}{2} \int_{-1}^1 x dx \left[H^q(x, \xi, t) - E^q(x, \xi, t) \right]_{t=0}$$

▪ sensitivity to GPD E (@fixed target exp. kinematics)

▪ pDVCS: $A_{UT} \rightarrow$ HERMES

▪ nDVCS: $A_{LU} \rightarrow$ Hall A

▪ meson prod. $A_{UT}: \rho^0 \rightarrow$ HERMES, COMPASS

...also $\omega, \phi, \rho^+, K^{*0}$

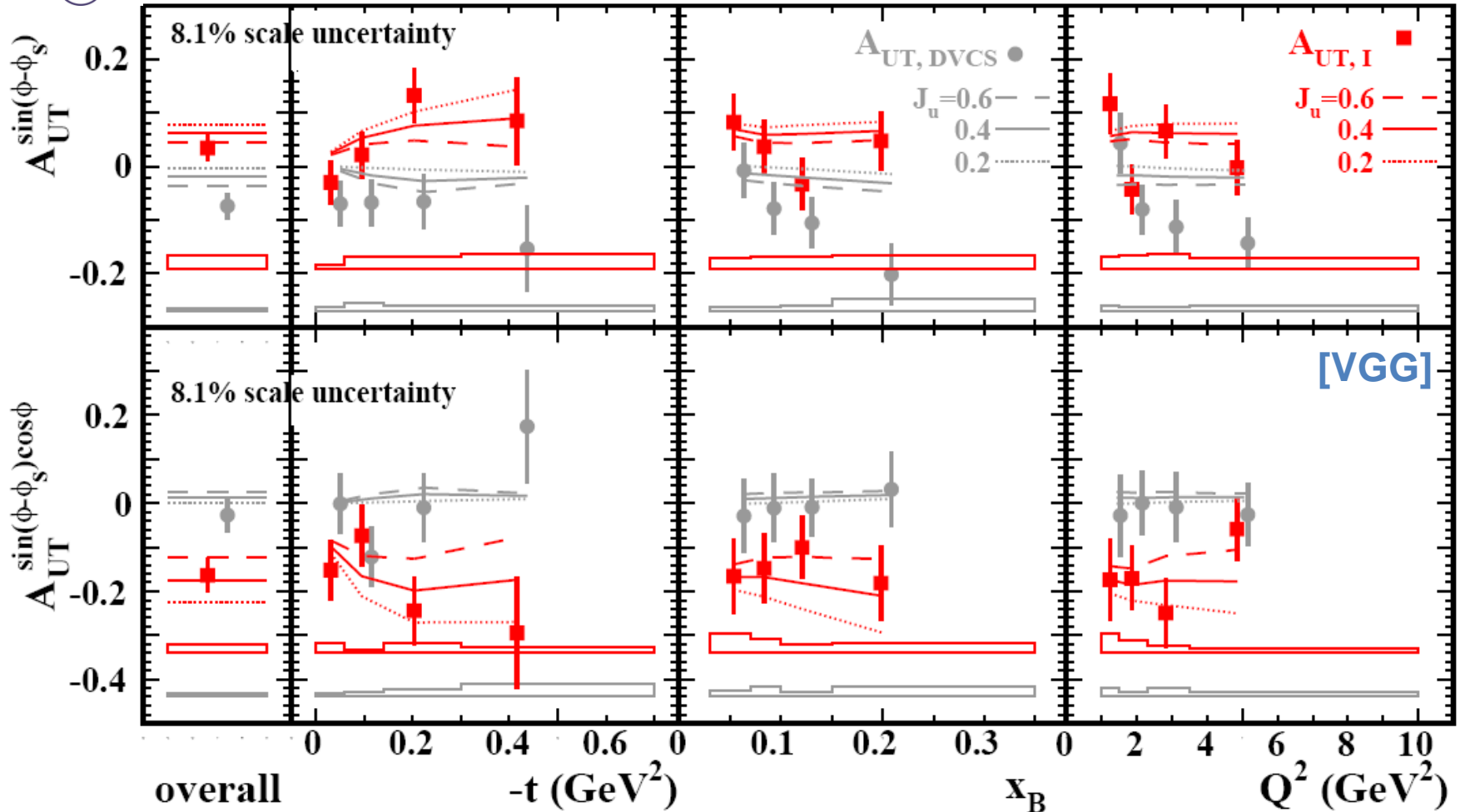
hunting the OAM

-- pDVCS : transverse target-spin asymmetry --



→ GPD models: J^q free parameter in ansatz for E

[JHEP06(2008)]

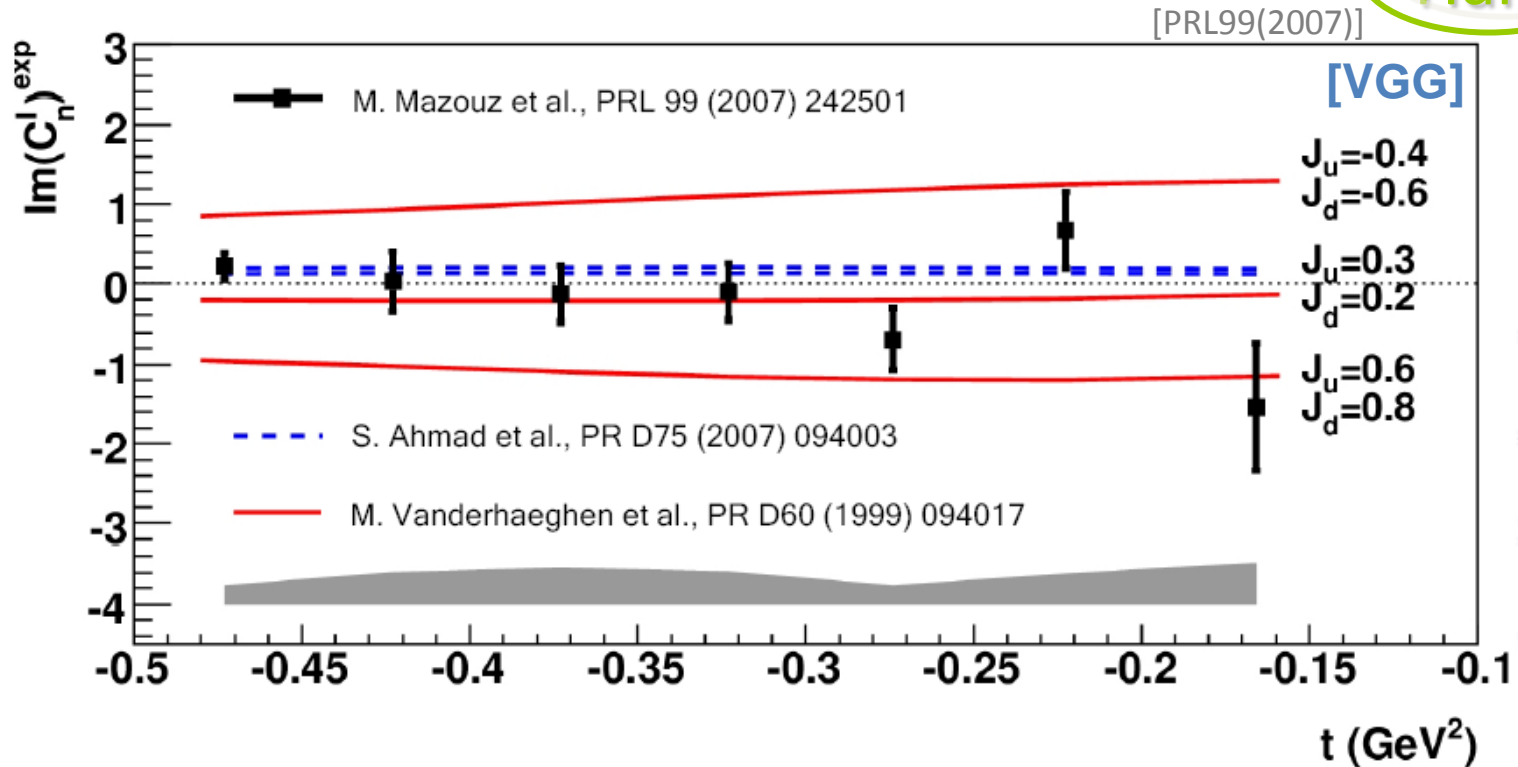


hunting the OAM

-- nDVCS : beam-spin cross section difference --

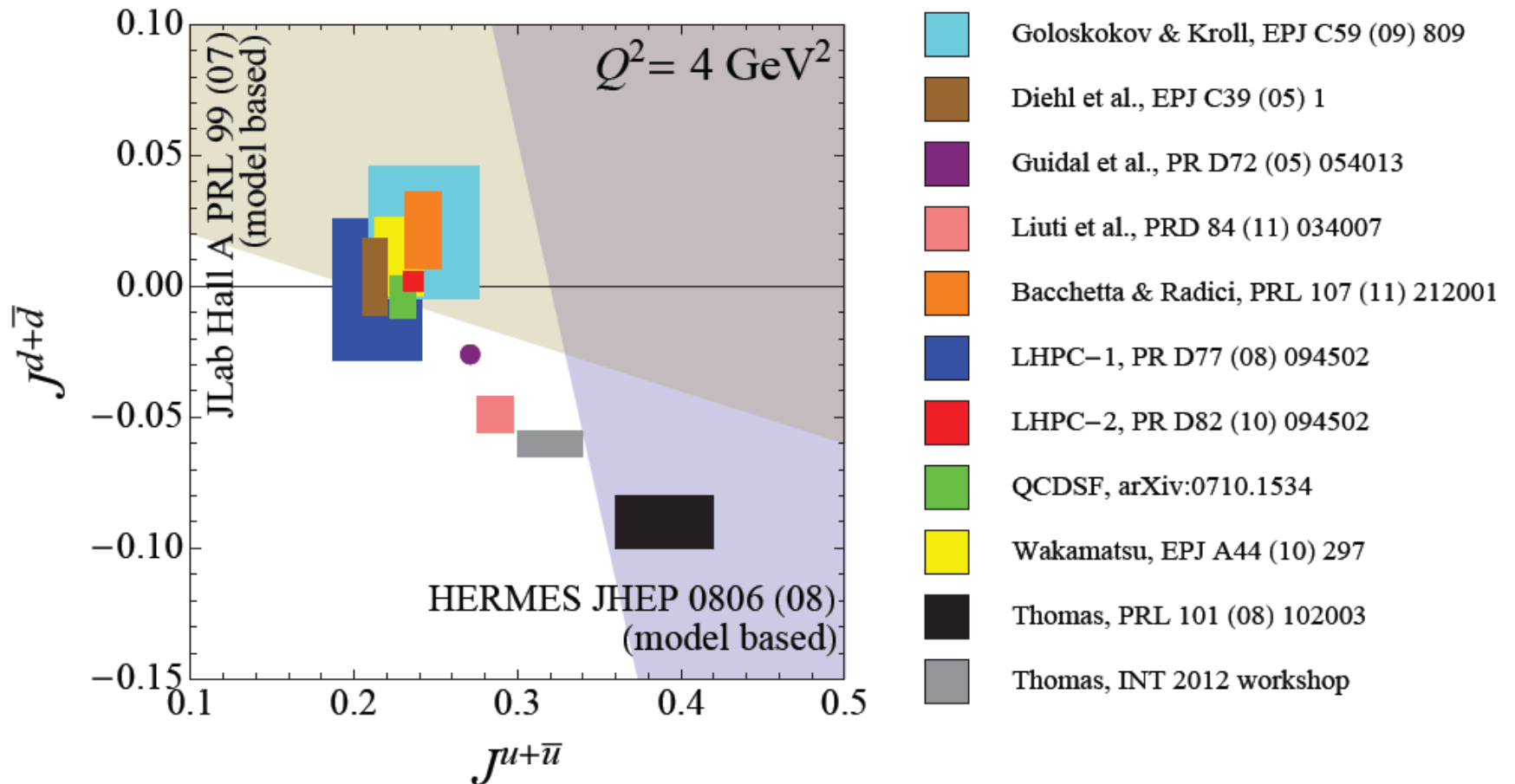
→ GPD models: J^q free parameter in ansatz for E

Hall-A



hunting the OAM

- *model dependent* [VGG(1999)] constrain of J_u vs J_d
- lattice
- GPD & TMD models



[figure taken from Bacchetta&Radici, PRL107(2011)]

conclusions



HERA collider

COMPASS

HERMES / JLab

$$10^{-4} < x_B < 0.02$$

$$0.02 < x_B < 0.4 \quad / \quad 0.1 < x_B < 0.6$$

sea quarks & gluons

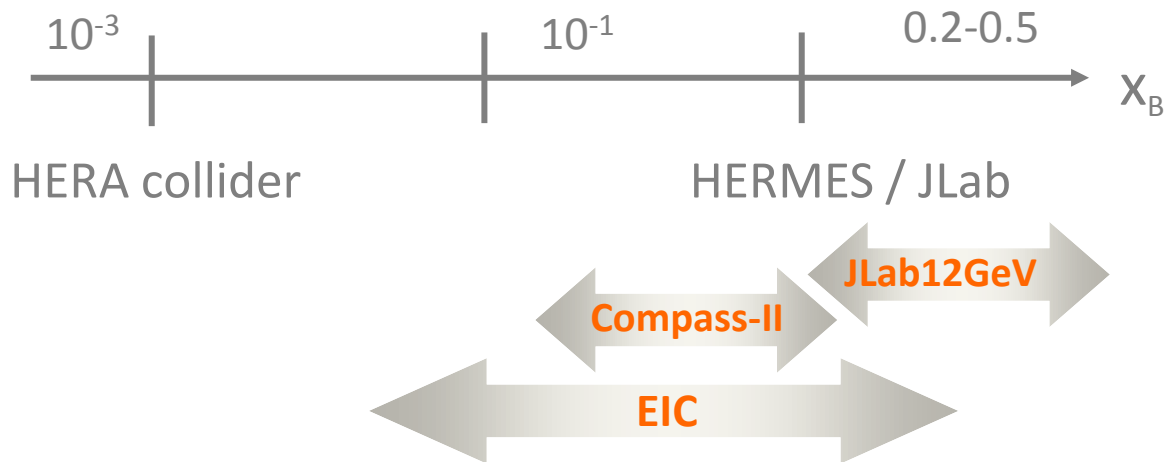
(gluons) (valence) quarks

DVCS, VM

DVCS, (mesons)

- increasing amount and precision of experimental data
- large variety of different observables (however, many still with limited precision)
- progress in model calculations, *plenty of room for more work...*

conclusions & perspectives



- increasing amount and precision of experimental data
- large variety of different observables (however, many still with limited precision)
- progress in model calculations, *plenty of room for more work...*
- **bright future for GPD studies:**
 - **JLab12**: DVCS in valence kinematic region
 - **COMPASS-II** with recoil: DVCS & VM in transition kinematic region

12 GeV Approved Experiments by Physics Topics

[<http://www.jlab.org/12GeV/>]

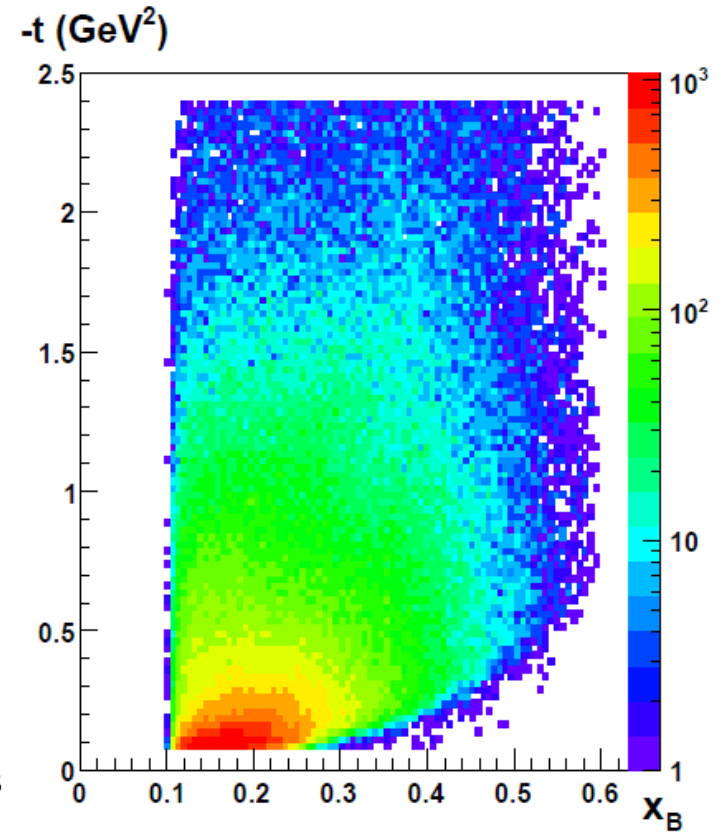
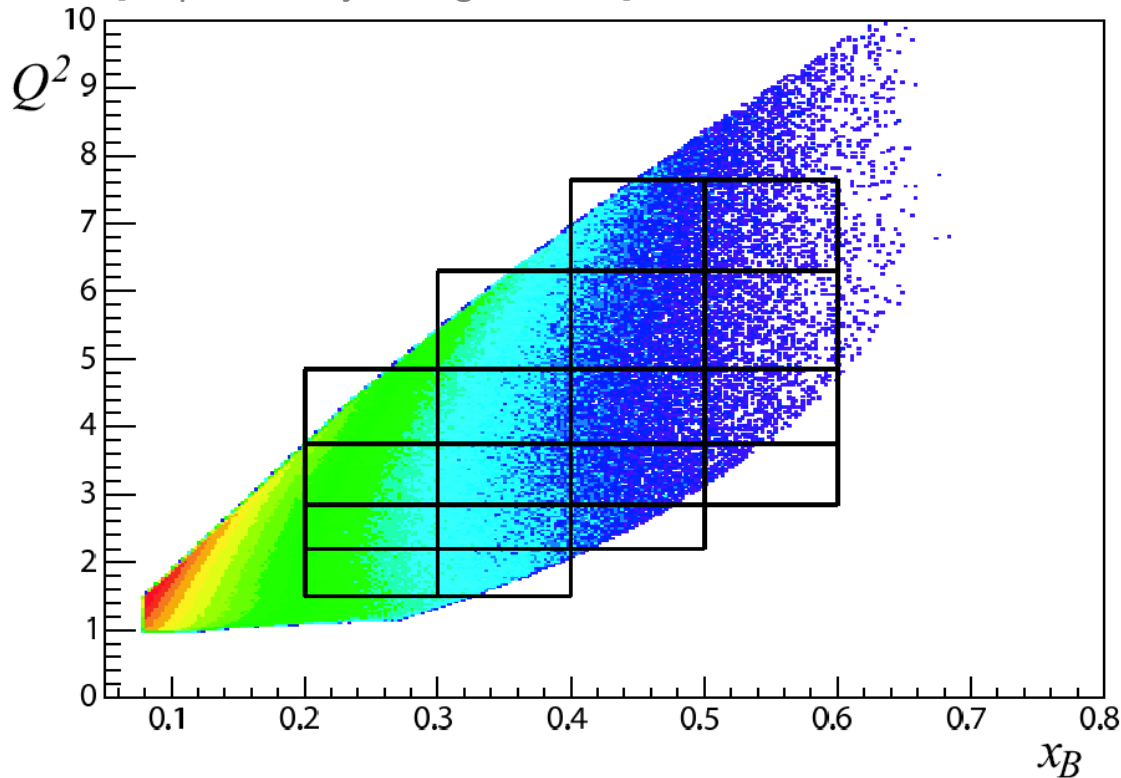
Topic	Hall A	Hall B	Hall C	Hall D	Total
The Hadron spectra as probes of QCD (rated) (GlueX and heavy baryon and meson spectroscopy)		1		1	2
The transverse structure of the hadrons (rated) (Elastic and transition Form Factors)	4	2	3		9
The longitudinal structure of the hadrons (rated) (Unpolarized and polarized parton distribution functions)	2	2	4		8
The 3D structure of the hadrons (unrated) (Generalized Parton Distributions and Transverse Momentum Distributions)	3	8 ^(*)	4		15
Hadrons and cold nuclear matter (rated) (Medium modification of the nucleons, quark hadronization, N-N correlations, hypernuclear spectroscopy, few-body experiments)	1	2	5		8
Low-energy tests of the Standard Model and Fundamental Symmetries (rated)	2			1	3
TOTAL	12	15	16	2	45

Current PAC approved experiments represent over 6 years of running at 35 weeks/year

(*) 3 new approved proposals on the topic @Hall B since then

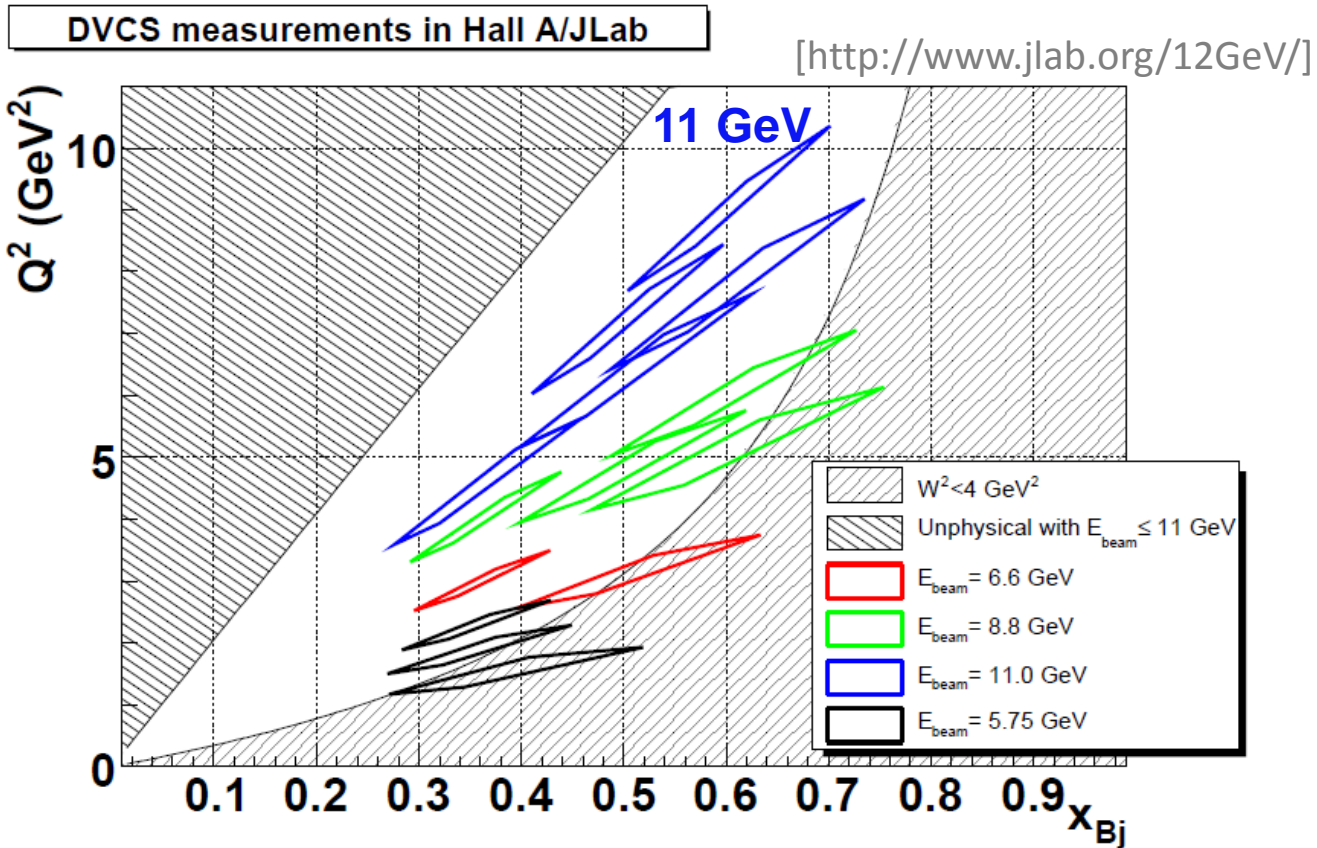
DVCS @ CLAS12 [2014+]

[<http://www.jlab.org/12GeV/>]



- fully differential analysis
- watch requirement $t \ll Q^2$

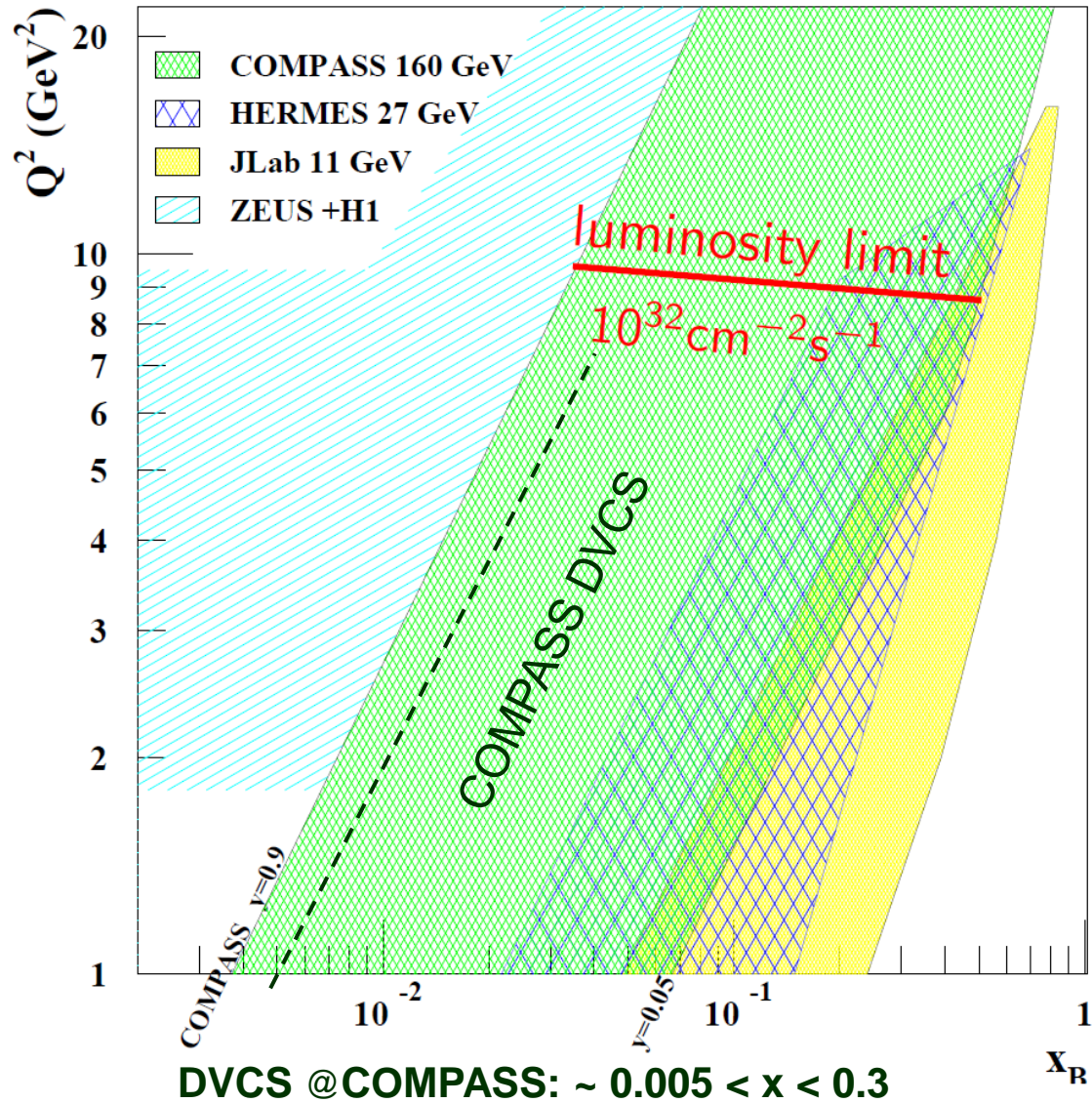
DVCS @Hall A [2014+]



- fully differential analysis
- watch requirement $t \ll Q^2$

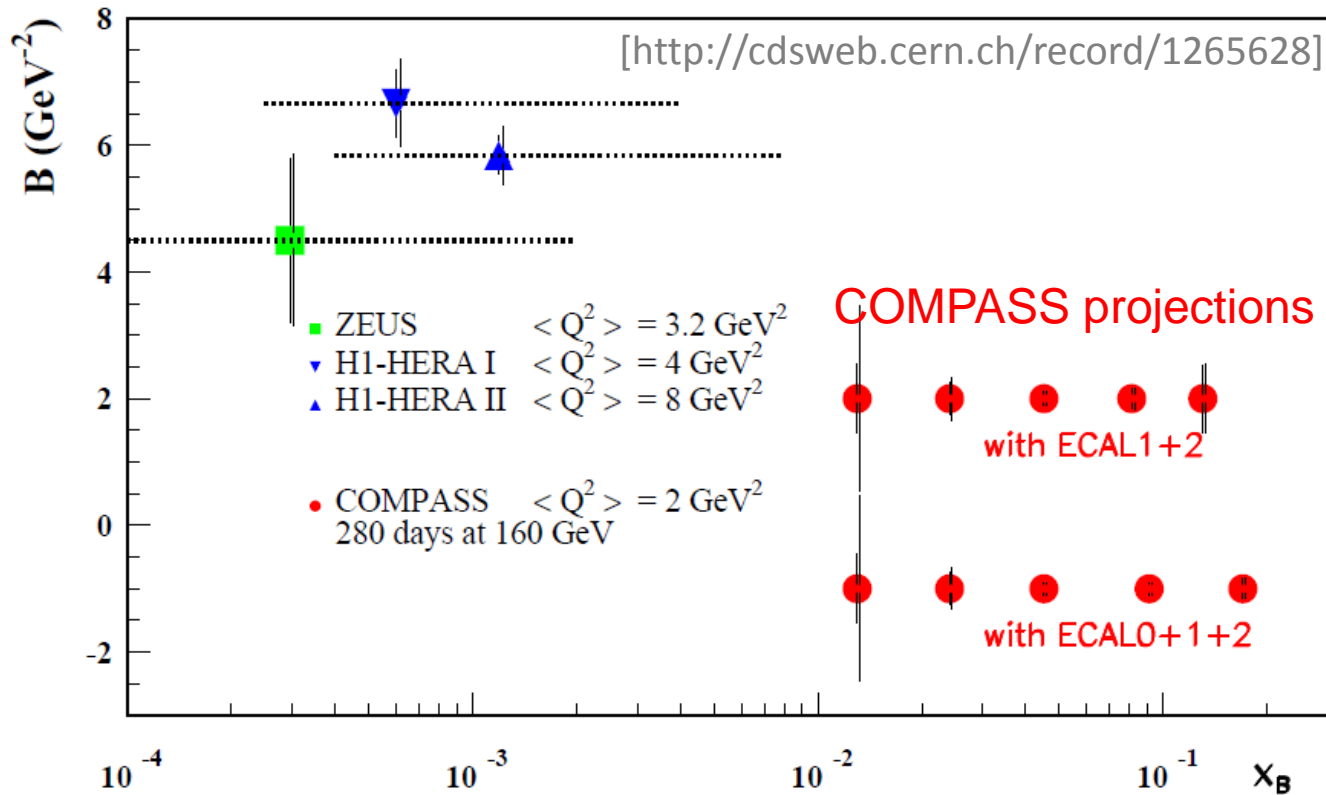
DVCS @COMPASS-II 2014+

[<http://cdsweb.cern.ch/record/1265628>]



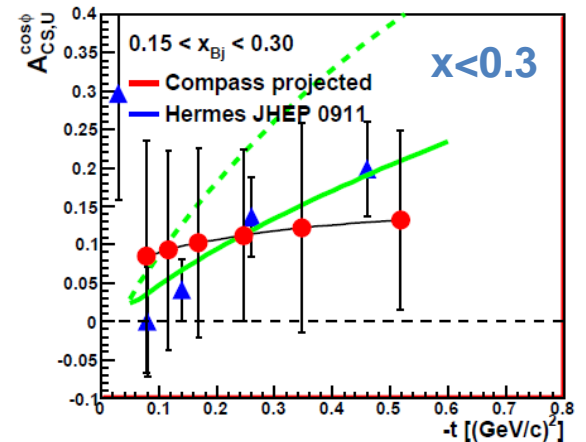
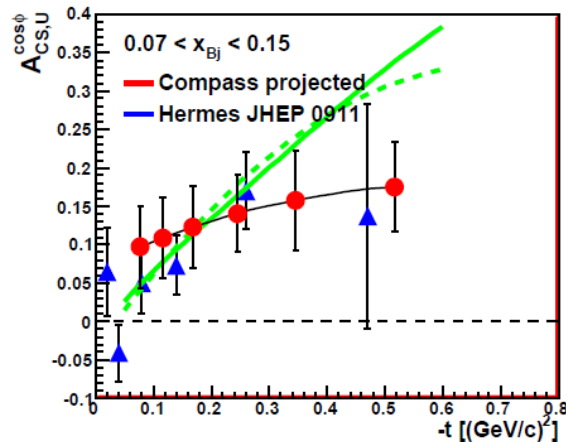
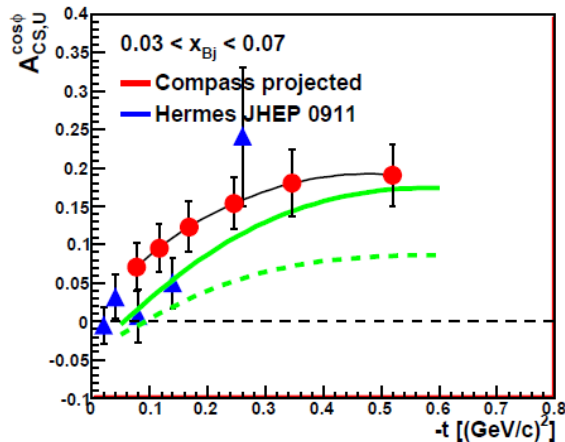
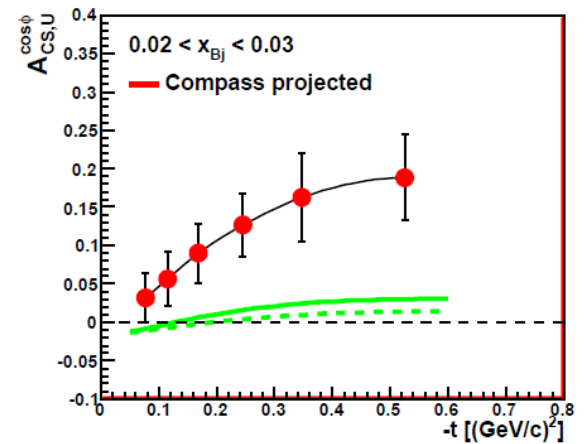
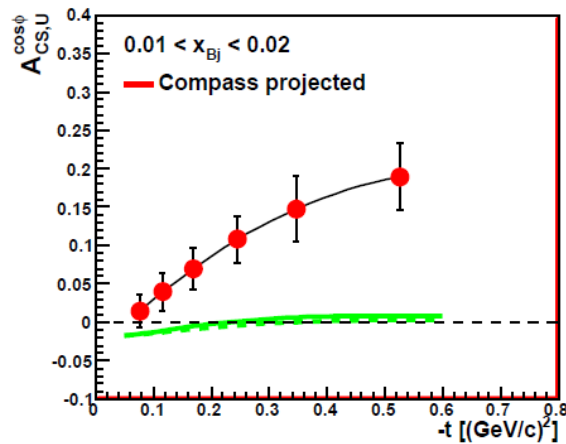
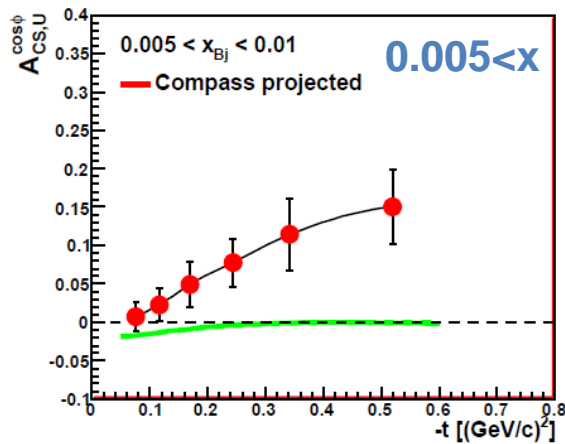
DVCS @ COMPASS-II 2014+

➤ DVCS cross section: slope parameter b : $d\sigma/dt \sim e^{-b|t|}$

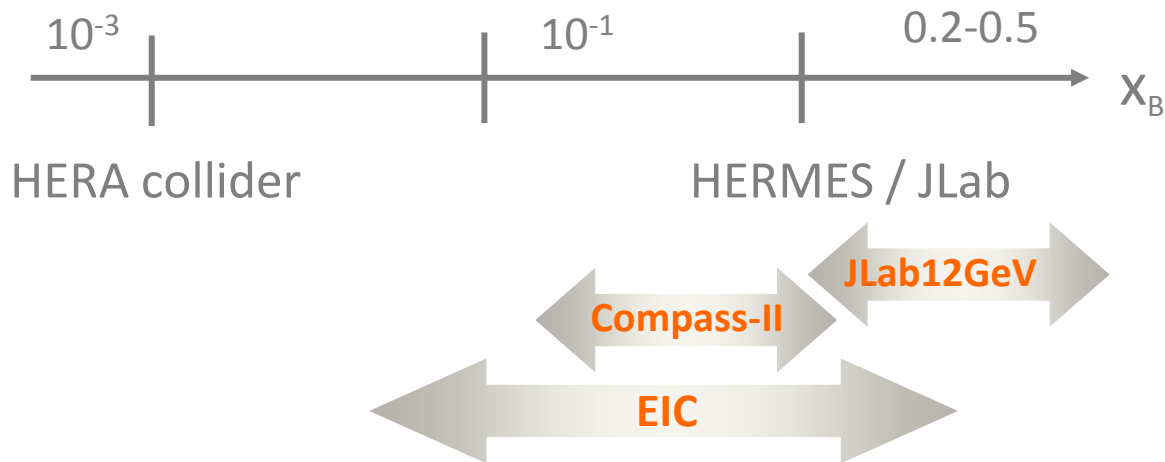


DVCS @ COMPASS-II 2014+

➤ DVCS beam helicity & charge asymmetry $A_C^{\cos\phi}(t, x_B)$



conclusions & perspectives

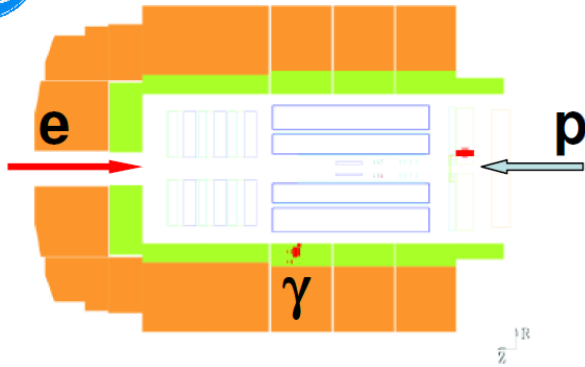
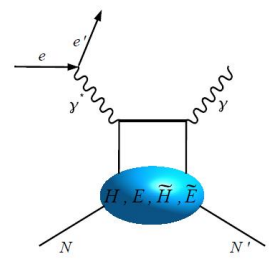


- increasing amount and precision of experimental data
- large variety of different observables (however, many still with limited precision)
- progress in model calculations, *plenty of room for more work...*
- bright future for GPD studies:
 - JLab12: DVCS in valence kinematic region
 - COMPASS-II with recoil: DVCS & VM in transition kinematic region
 - EIC: mapping GPDs from Q^2 evolution of DVCS & from meson production

additional slides

exclusivity

@ the HERA collider experiments

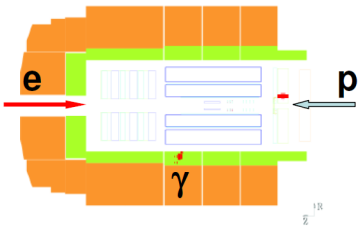


\approx hermetic detector

$\rightarrow p$ escapes through beam pipe

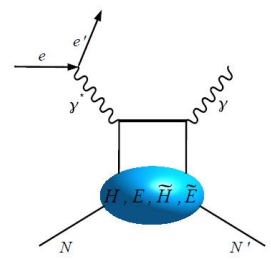


LPS: p tagged control sample

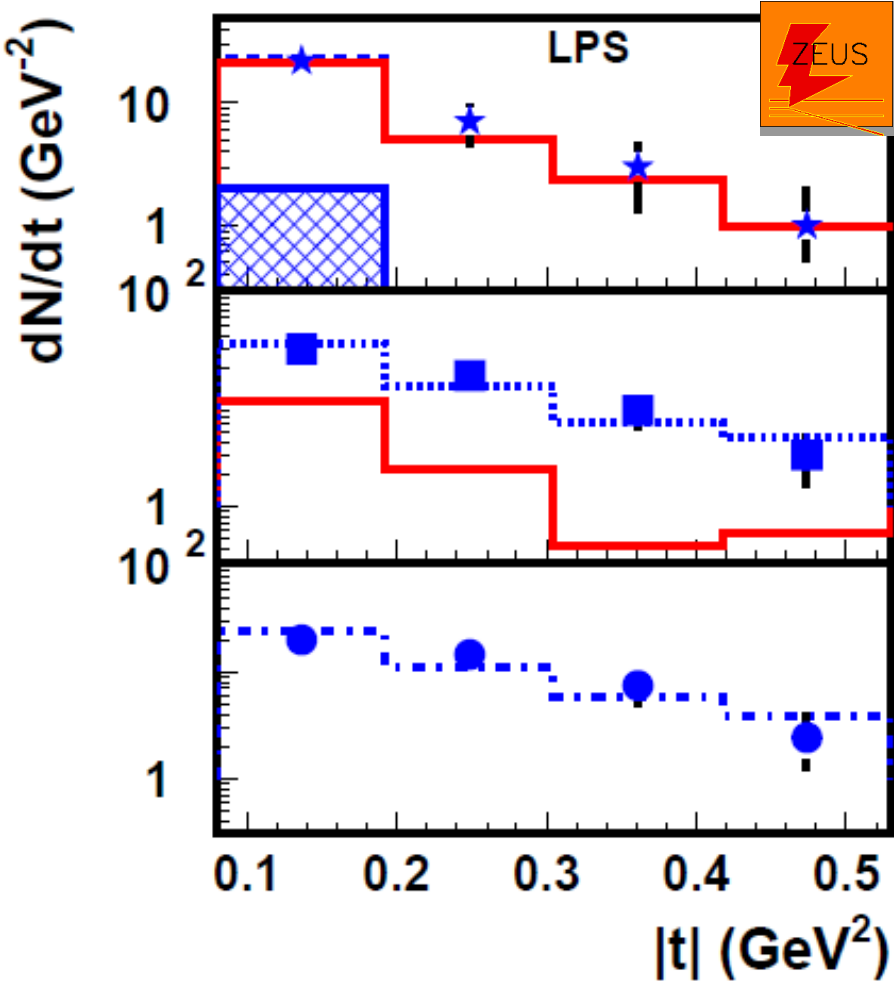


exclusivity

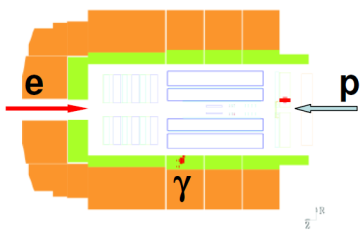
@ the HERA collider experiments



LPS: p tagged data sample

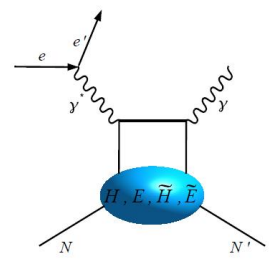


- ★ e-sample: BH control sample
- ▨ e+e-, J/ψ bg-sample
- ⋯ BH+e⁺e⁻+J/ψ
- BH
- γ-sample: BH+DVCS
- BH
- ⋯ BH+FFS (DVCS)
- (BH+DVCS) - BH
- ⋯ FFS (DVCS)

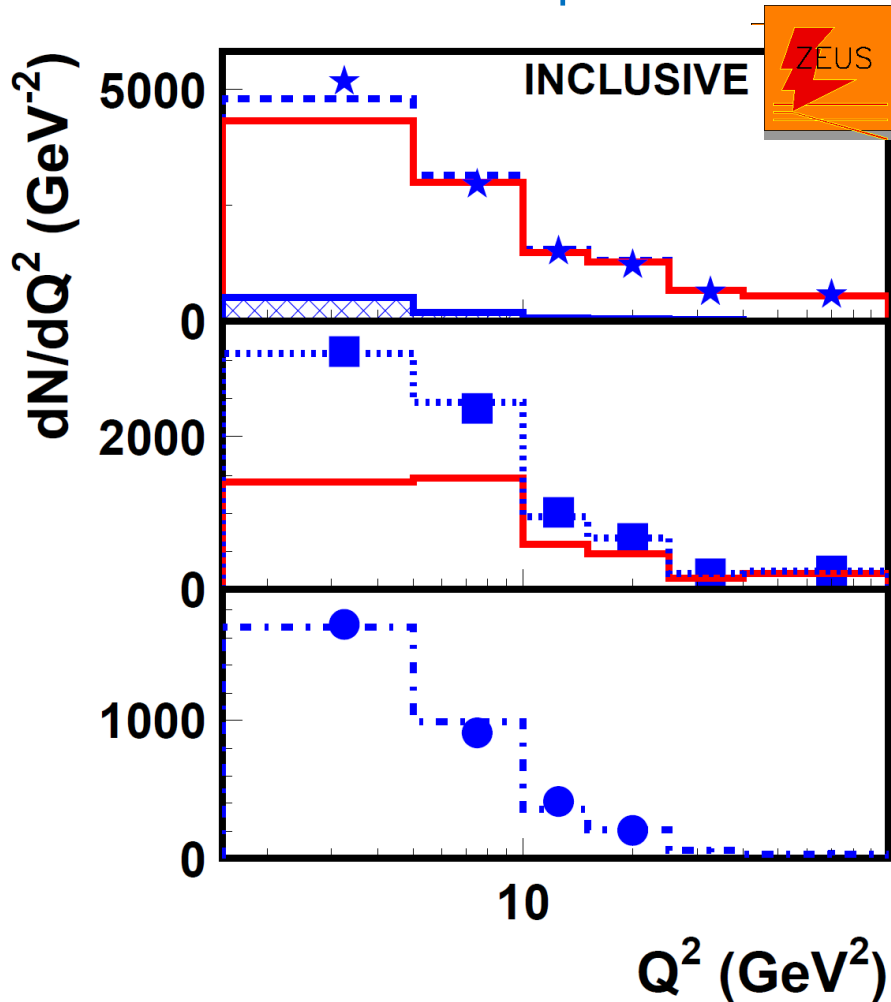


exclusivity

@ the HERA collider experiments



full data sample



★ e-sample: BH control sample

⊠ e+e-, J/ψ bg-sample

⋯ BH+e⁺e⁻+J/ψ

— BH

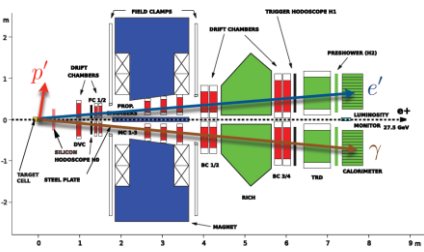
■ γ-sample: BH+DVCS

— BH

⋯ BH+FFS (DVCS)

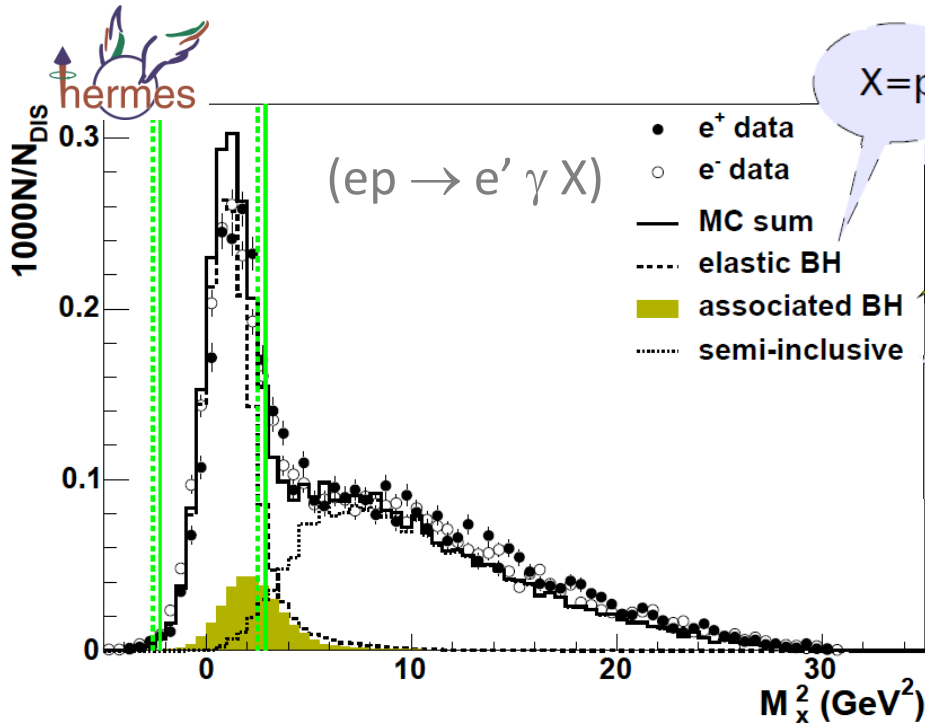
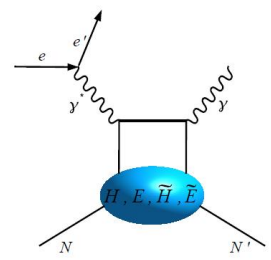
● (BH+DVCS) - BH

⋯ FFS (DVCS)



exclusivity

fixed target: via missing mass / energy

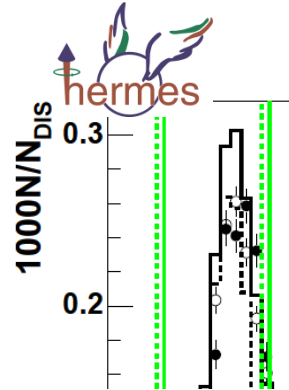
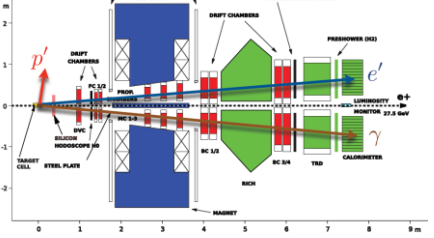
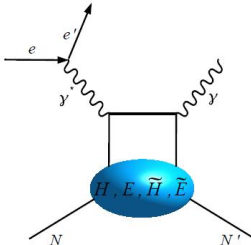


part of the signal

subtracted
very well understood

exclusivity

fixed target: via missing mass / energy

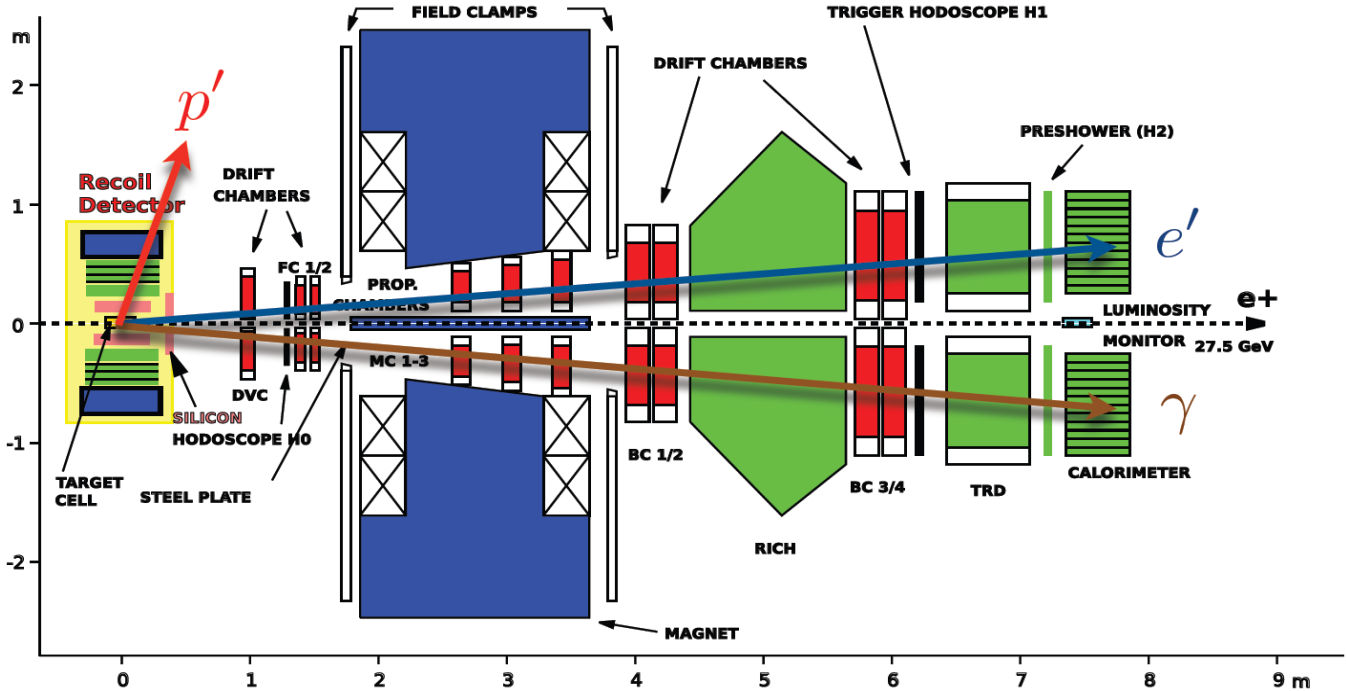


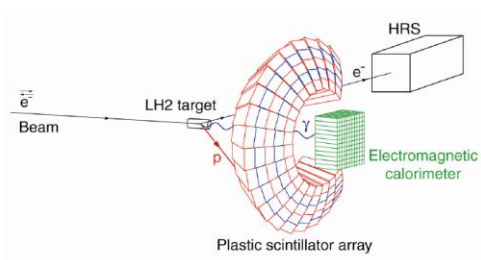
$(ep \rightarrow e' \gamma X)$

- e⁺ data
- e⁻ data
- MC sum
- - - elastic BH
- associated BH
- ⋯ semi-inclusive

X=p
Resonant excitation: X=Δ⁺

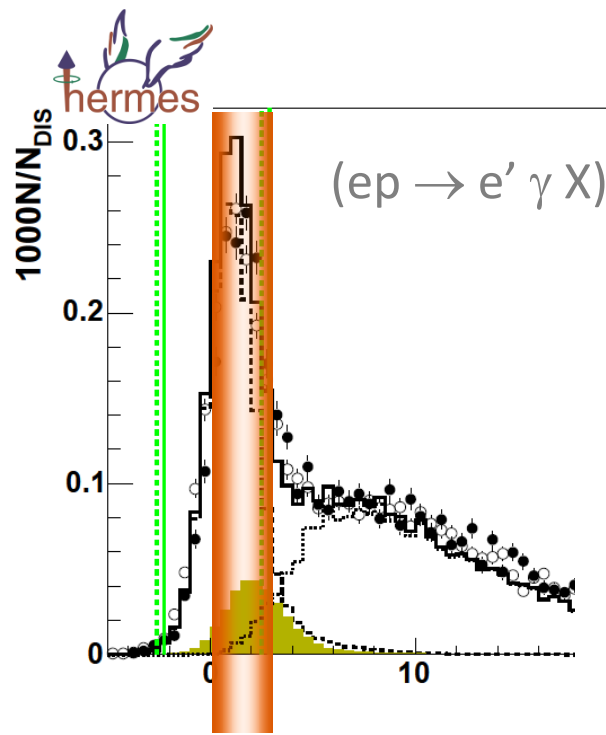
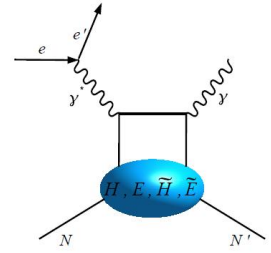
with p detection & Δ⁺ ID: transition GPDs





exclusivity

fixed target: via missing mass / energy

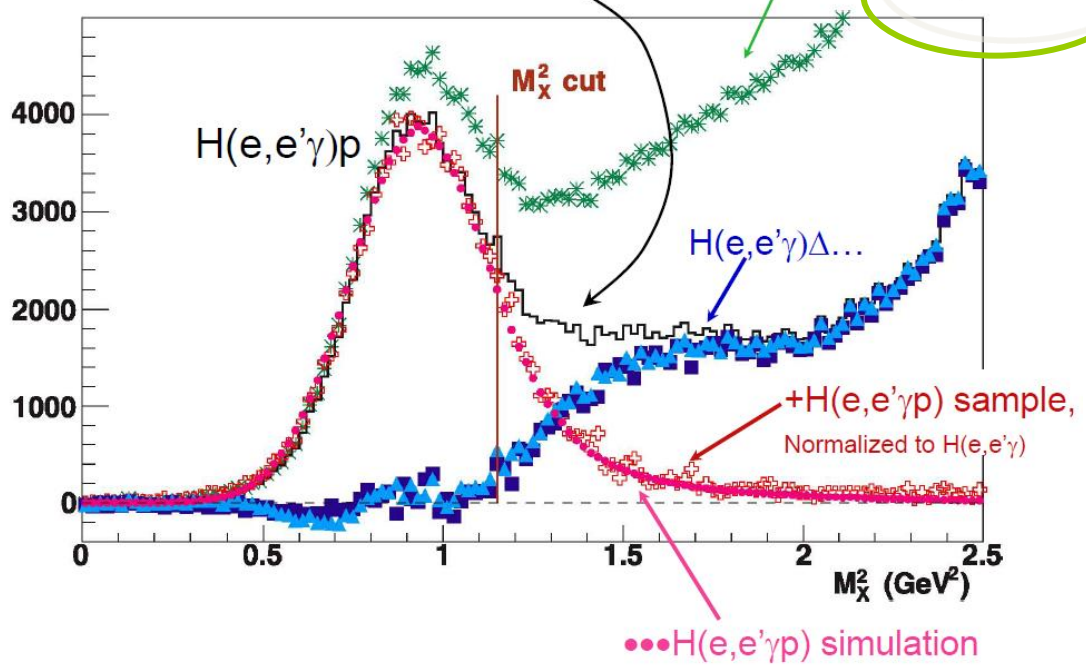


- e⁺ data
 - e⁻ data
 - MC sum
 - elastic PH
- X=p
- Resonant excitation: X=Δ⁺

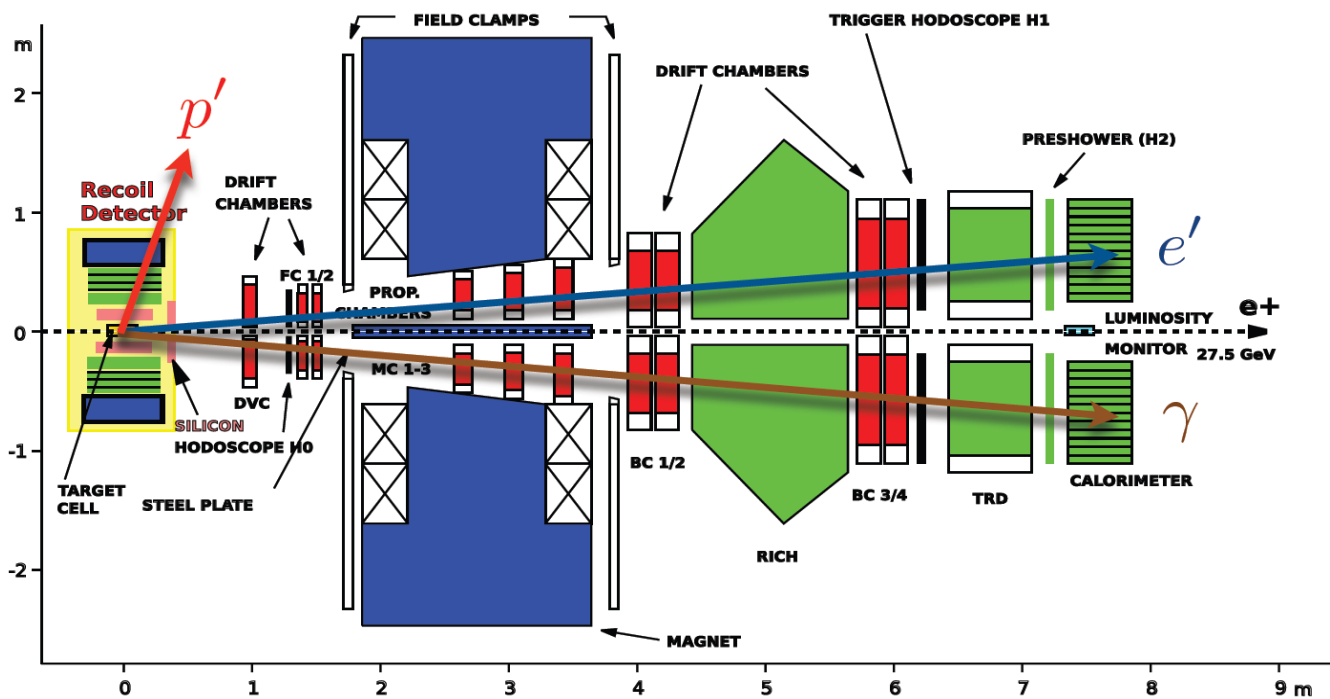
part of the signal

Raw H(e,e'γ)X Missing Mass² (after accidental subtraction).

[H(e,e'γ)X - H(e,e'γ)γY]: Missing Mass²



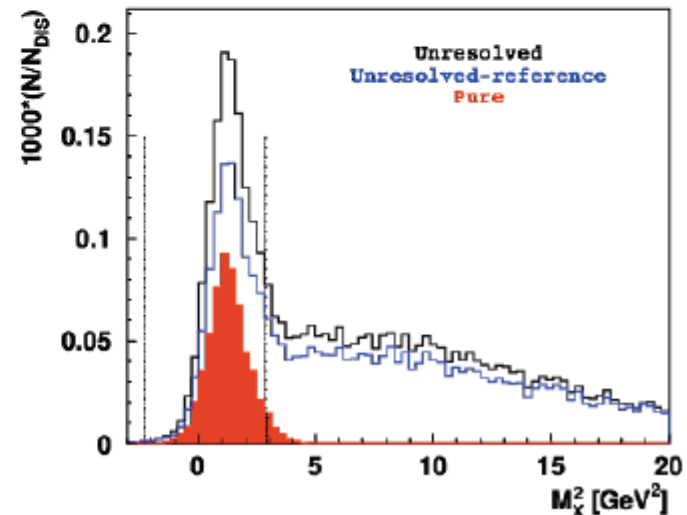
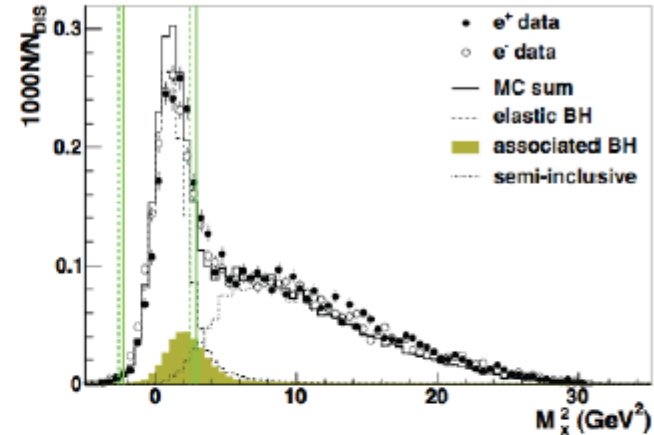
exclusivity: HERMES with recoil



exclusivity: HERMES with recoil

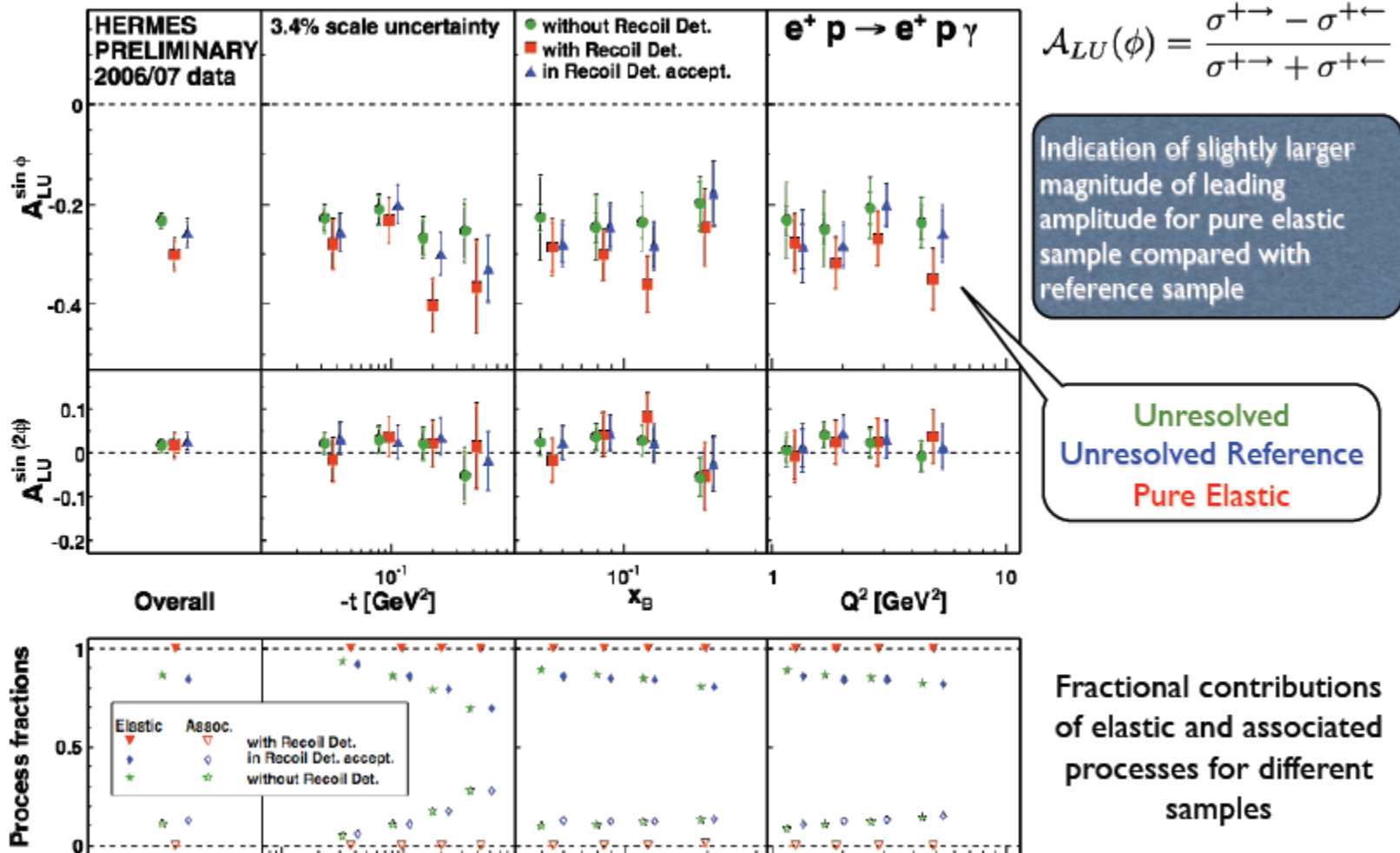
Event Selection with Recoil Detector

- Events with one DIS lepton and one trackless cluster in the calorimeter.
- “**Unresolved**” for associated process $ep \rightarrow e\Delta^+\gamma \approx 12\%$
- “**Unresolved reference**” sample.
- “Hypothetical” proton required in the Recoil Detector acceptance.
- “**Pure Elastic**” sample.
- Kinematic event fitting technique.
Allows to achieve purity $> 99.9\%$



exclusivity: HERMES with recoil

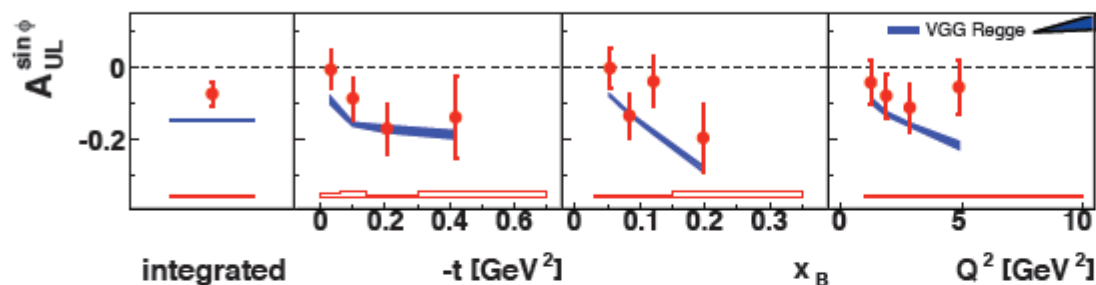
Beam-Spin asymmetry with Recoil



HERMES target spin asymmetries

JHEP 06 (2010) 019 Longitudinal Single Target-Spin and Double-Spin asymmetries

$$A_{UL}(\phi) = \frac{(\sigma^{\rightarrow\rightarrow} + \sigma^{\leftarrow\rightarrow}) - (\sigma^{\rightarrow\leftarrow} + \sigma^{\leftarrow\leftarrow})}{(\sigma^{\rightarrow\rightarrow} + \sigma^{\leftarrow\rightarrow}) + (\sigma^{\rightarrow\leftarrow} + \sigma^{\leftarrow\leftarrow})}$$



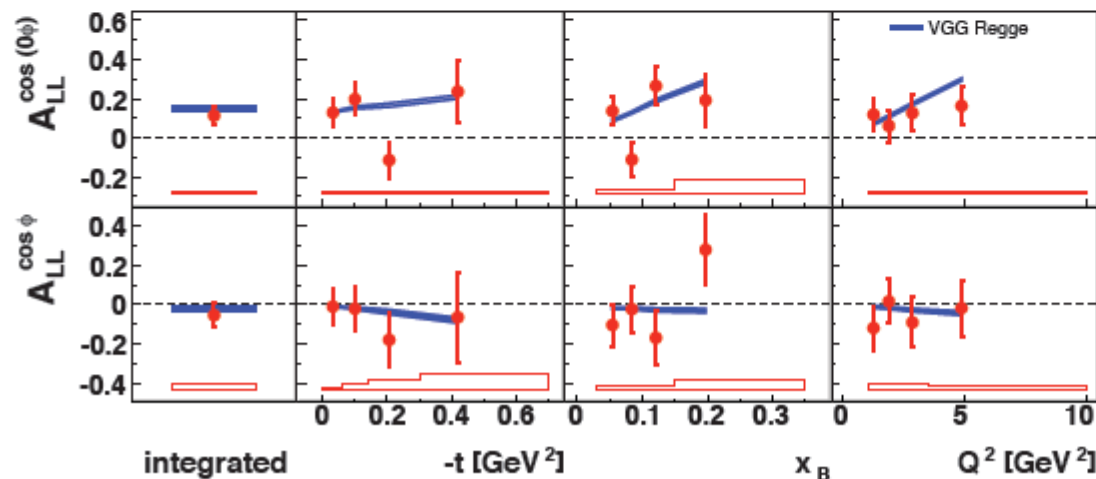
VGG: Model calculation
M. Vanderhaeghen, P. Guichon, M. Guidal
Phys..Rev.D (1999) 094017
Prog. Nucl. Phys, 47 (2001) 401

$$\propto \text{Im} [F_1 \tilde{\mathcal{H}}]$$

Longitudinal Target Spin Asymmetry

- non-zero negative value of the leading $\sin(\phi)$ amplitude
- mild kinematic dependence

$$A_{LL}(\phi) = \frac{(\sigma^{\rightarrow\rightarrow} + \sigma^{\leftarrow\leftarrow}) - (\sigma^{\rightarrow\leftarrow} + \sigma^{\leftarrow\rightarrow})}{(\sigma^{\rightarrow\rightarrow} + \sigma^{\leftarrow\leftarrow}) + (\sigma^{\rightarrow\leftarrow} + \sigma^{\leftarrow\rightarrow})}$$



Longitudinal Double-Spin Asymmetry

- constant term is positive
- leading $\cos(\phi)$ amplitude is consistent with zero

$$\propto \text{Re} [F_1 \tilde{\mathcal{H}}]$$

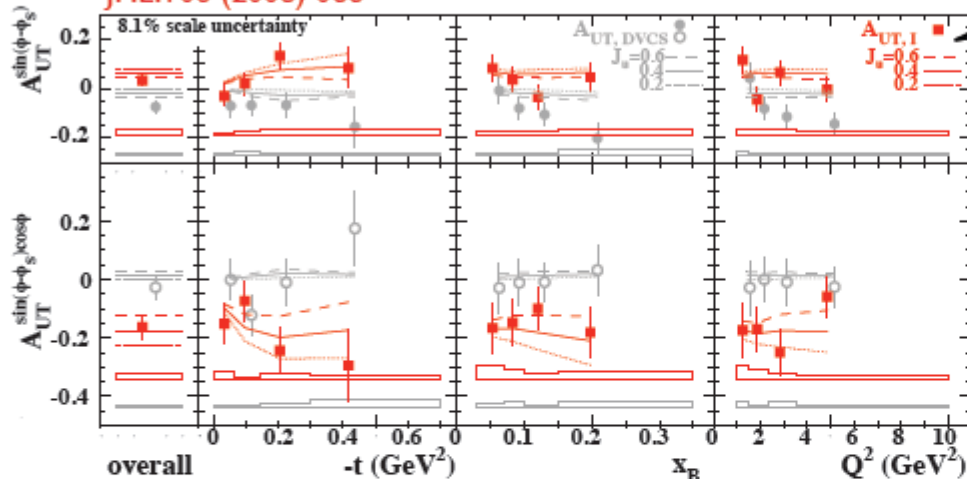
Asymmetry amplitudes are attributed not only to squared DVCS and Interference terms but also to squared BH term

HERMES target spin asymmetries

Transverse Single Target-Spin and Double-Spin asymmetries

$$A_{UT}^{I,DVCS}(\phi, \phi_S) = \frac{(\sigma^{+\uparrow} - \sigma^{+\downarrow})_+ (\sigma^{-\uparrow} - \sigma^{-\downarrow})_-}{(\sigma^{+\uparrow} + \sigma^{+\downarrow})_+ + (\sigma^{-\uparrow} + \sigma^{-\downarrow})_-}$$

JHEP.06 (2008) 066



VGG: Model calculation
M.Vanderhaeghen, P. Guichon, M. Guidal
Phys..Rev.D (1999) 094017
Prog. Nucl. Phys, 47 (2001) 401

Charge-difference Transverse Target-Spin asymmetry

- Non-zero leading $\cos(n\phi)$ amplitudes.

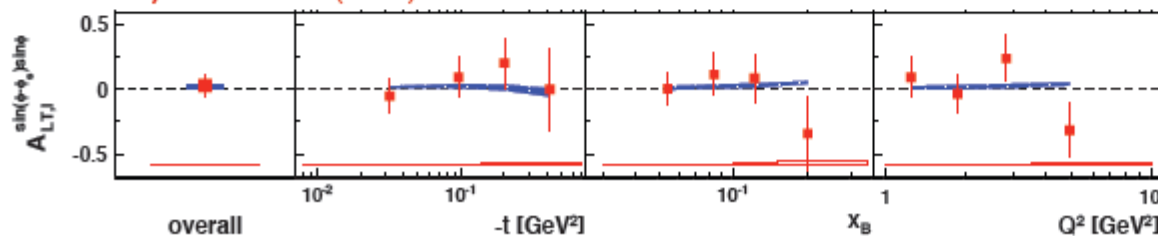
$$\propto \text{Im}[F_2\mathcal{H} - F_1\mathcal{E}]$$

$$\propto \text{Im}[\mathcal{H}\mathcal{E}^* - \mathcal{E}\mathcal{H}^* - \xi(\tilde{\mathcal{H}}\tilde{\mathcal{E}}^* - \tilde{\mathcal{E}}\tilde{\mathcal{H}}^*)]$$

Leading $\cos(\phi)$ amplitude of charge difference target-spin asymmetry A_{UT}^I is sensitive to CFF \mathcal{E} , therefore J_u .

$$A_{LT}^I(\phi, \phi_S) = \frac{(\vec{\sigma}^{+\uparrow} + \vec{\sigma}^{+\downarrow} - \vec{\sigma}^{+\downarrow} - \vec{\sigma}^{+\uparrow}) - (\vec{\sigma}^{-\uparrow} + \vec{\sigma}^{-\downarrow} - \vec{\sigma}^{-\downarrow} - \vec{\sigma}^{-\uparrow})}{(\vec{\sigma}^{+\uparrow} + \vec{\sigma}^{+\downarrow} + \vec{\sigma}^{+\downarrow} + \vec{\sigma}^{+\uparrow}) + (\vec{\sigma}^{+\uparrow} + \vec{\sigma}^{+\downarrow} + \vec{\sigma}^{+\downarrow} + \vec{\sigma}^{+\uparrow})}$$

Phys. Lett. B704 (2011) 15-23



Charge-difference Transverse Double-Spin asymmetry

- leading amplitudes are consistent with zero
- sensitivity to is suppressed J_u is suppressed by kinematic pre-factor

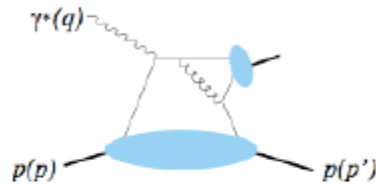
$$\propto \text{Re}[F_2\mathcal{H} - F_1\mathcal{E}]$$

HERMES VM SDMEs

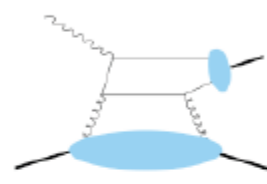
Exclusive Vector Meson Production

pQCD description of the process.

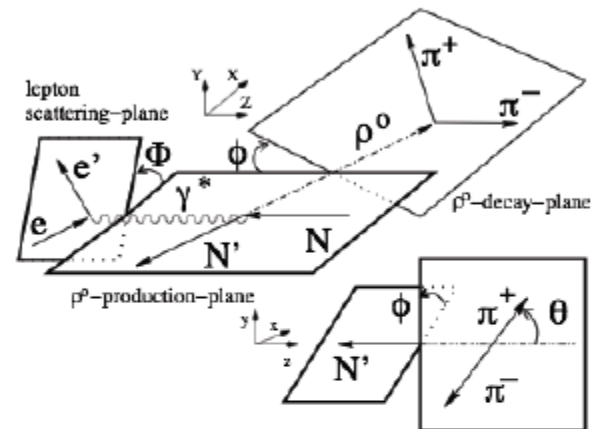
- I) dissociation of the virtual photon into quark-antiquark pair
- II) scattering of a pair on a nucleon
- III) formation of the observed vector meson



UPE
GPDs \tilde{H}, \tilde{E}



NPE
GPDs H, E



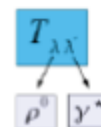
Cross Section

$$\frac{d\sigma}{dx_B dQ^2 dt d\Phi d \cos \theta d\phi} \propto \frac{d\sigma}{dx_B dQ^2 dt} W(x_B, Q^2, t, \Phi, \cos \theta, \phi)$$

production and decay angular distribution: W decomposition

$$W = W_{UU} + P_L W_{LU} + S_L W_{UL} + P_L S_L W_{LL} + S_T W_{UT} + P_L S_T W_{LT}$$

parameterization in terms of helicity amplitudes



or SDMES

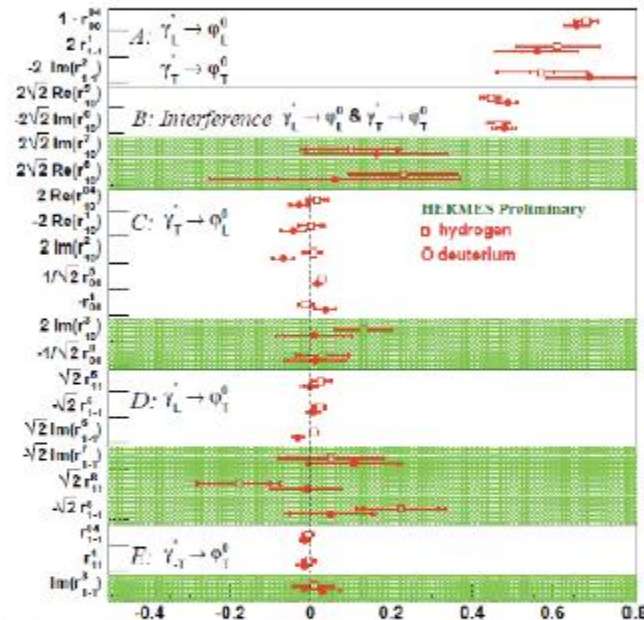
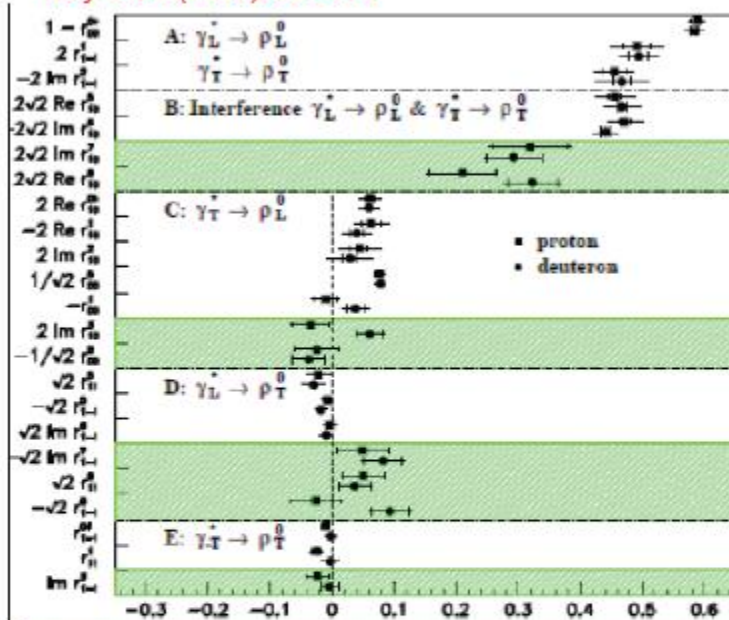


HERMES VM SDMEs

ρ^0 and ϕ SDMEs on an unpolarized target

EPJ C 62 (2009) 659-694

$$|T_{00}|^2 \sim |T_{11}|^2 \gg |T_{01}|^2 > |T_{10}|^2 \sim |T_{-11}|^2$$



$\gamma_{L \rightarrow V_L}^* \text{ \& } \gamma_{T \rightarrow V_T}^*$

- SDMEs are significantly different from zero
- 10-20% difference between ρ and ϕ SDMEs

$\gamma_{L \rightarrow V_T}^* \text{ \& } \gamma_{T \rightarrow V_T}^*$

- SDMEs are consistent with zero

$\gamma_{T \rightarrow V_L}^*$

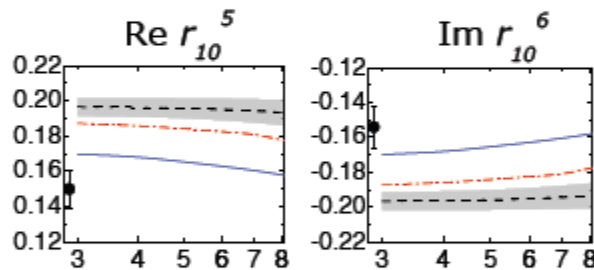
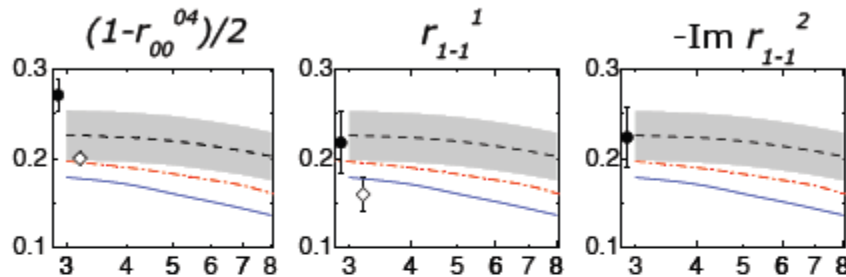
- pronounced difference between ρ and ϕ SDMEs
- 2-10 σ level violation from SCHC for ρ

- Selected hierarchy is confirmed
- No differences between proton and deuteron

HERMES VM SDMEs

Comparison of ρ^0 SDMEs to GPD model

GPD model: [S.Goloskokov, P. Kroll \(2007\)](#)



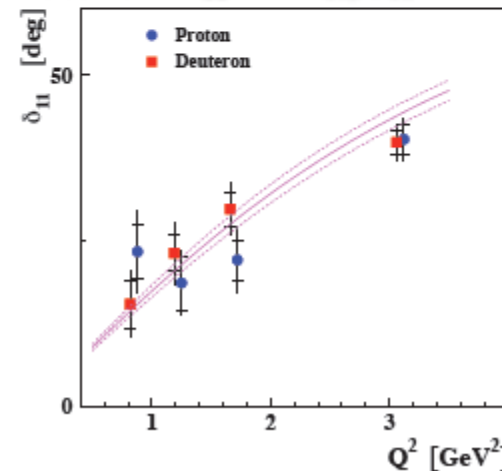
$$\tan \delta_{11} = \frac{\text{Im}(T_{11}/T_{00})}{\text{Re}(T_{11}/T_{00})}$$

HERMES result $\delta_{11} = 31.5 \pm 1.4$ deg.

Large phase difference was observed also by H1 ($\delta_{11} = 20$)

W=5 GeV (HERMES)
W=10 GeV (COMPASS)
W=75 GeV (H1, ZEUS)

$\gamma^*_L \rightarrow \rho^0_L$ & $\gamma^*_T \rightarrow \rho^0_T$
 $1 - r_{00}^{04}, r_{1-1}^1, -\text{Im} r_{1-1}^2 \propto T_{11}$
 model is in an agreement with data
Interference $\gamma^*_L \rightarrow \rho^0_L$ & $\gamma^*_T \rightarrow \rho^0_T$
 model dose not describe the data
 model predicts phase difference
 between T_{00} and T_{11} , $\delta_{11} = 3.1$ deg.



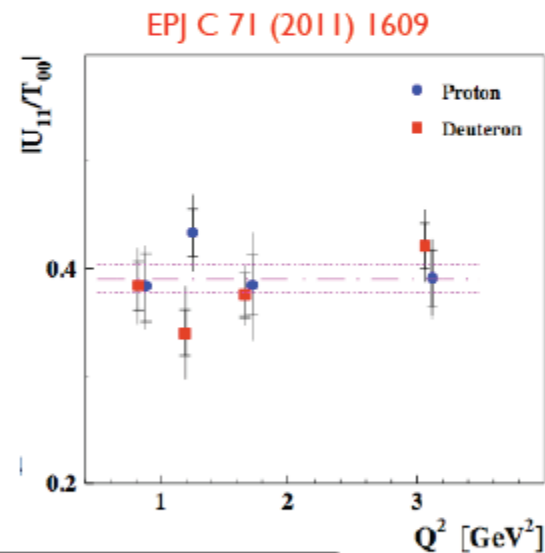
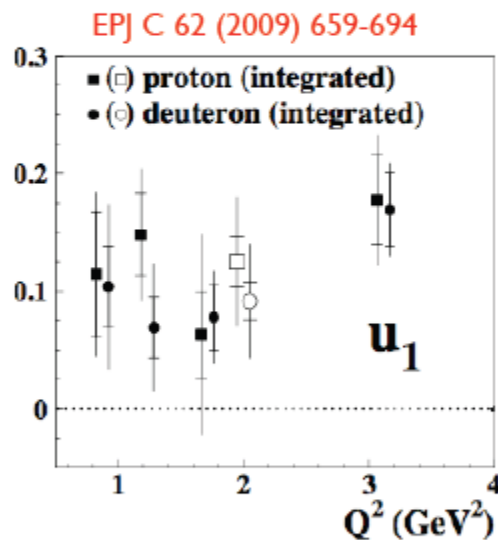
HERMES VM SDMEs

Observation of Unnatural-parity exchange

At large W^2 and Q^2 the transition should be suppressed by M/Q

- direct helicity amplitude ratio analysis: U_{11}/T_{00}
- the combination of SDMEs is expected to be zero in case of NPE

$$u_1 = 1 - r_{00}^{04} + 2r_{1-1}^{04} - 2r_{11}^1 - 2r_{1-1}^1 \quad u_2 = r_{11}^5 + r_{1-1}^5 \quad u_3 = r_{11}^8 + r_{1-1}^8$$



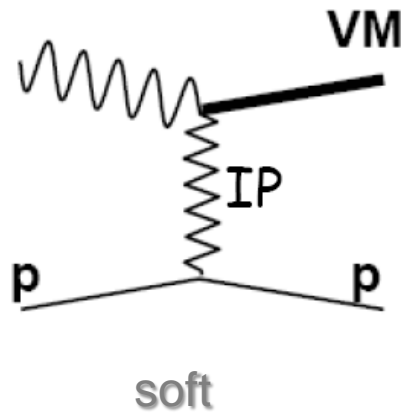
- Significant UPE contribution for ρ^0
- Sensitivity to GPD H
- No signal of UPE contribution for ϕ



VM production @low x

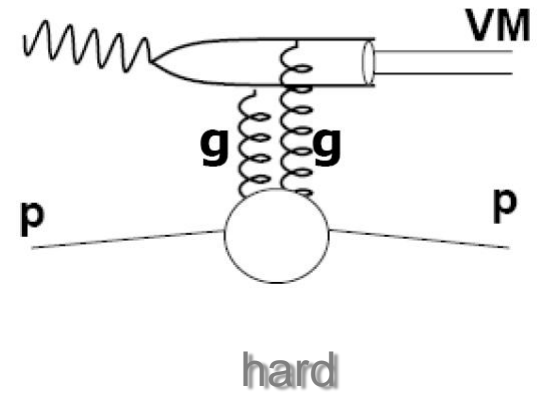


W & t dependences: probe transition from soft to hard regime



$$\sigma(W) \propto W^\delta$$

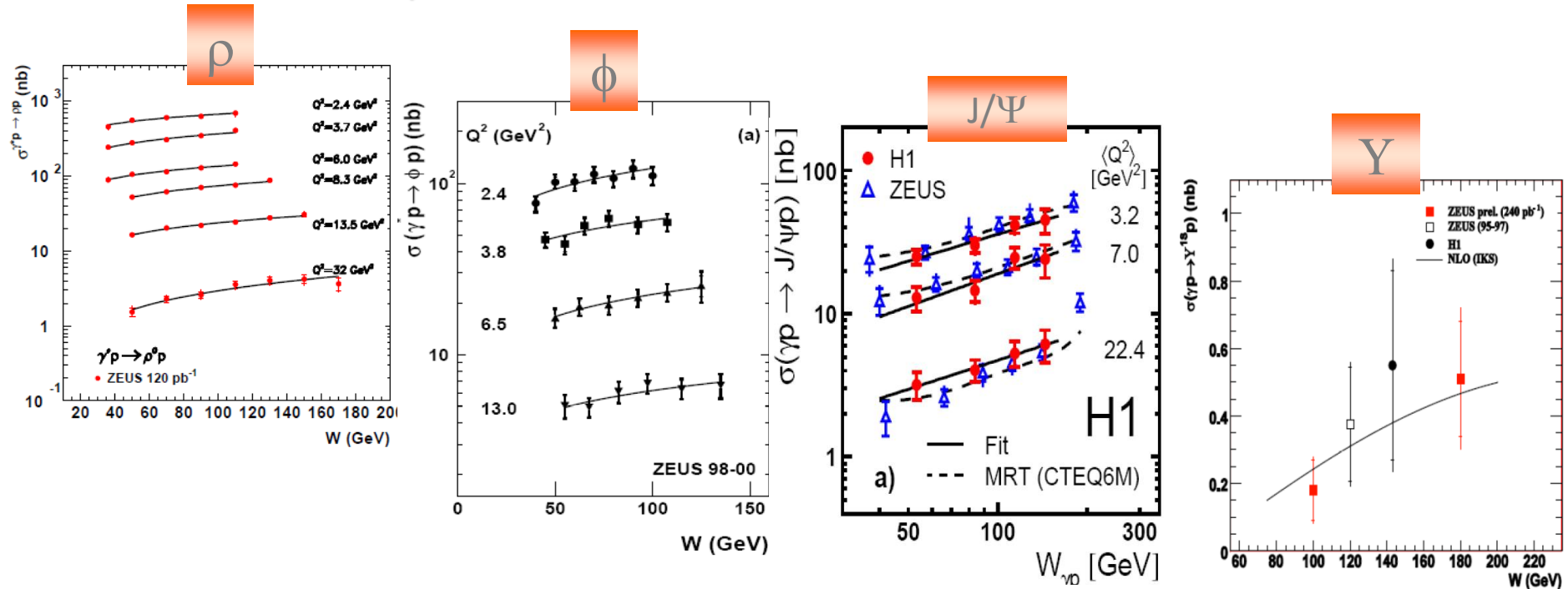
$$\frac{d\sigma}{dt} \propto e^{-b|t|}$$



→ expect δ to increase from ~ 0.2 to ~ 0.8

b to decrease from ~ 10 to $\sim 4-5 \text{ GeV}^2$

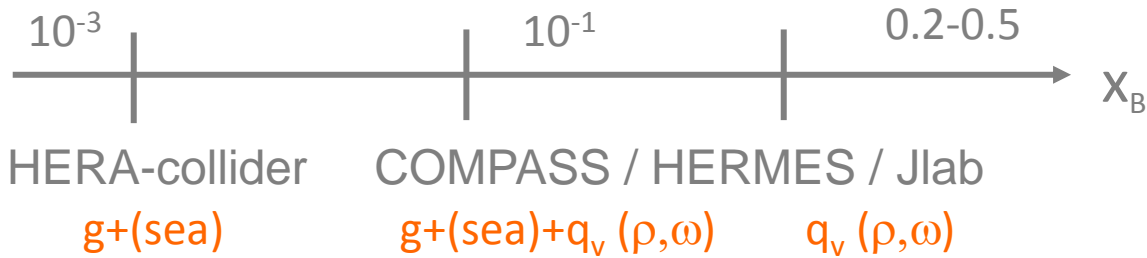
W dependence: probe transition from soft to hard regime



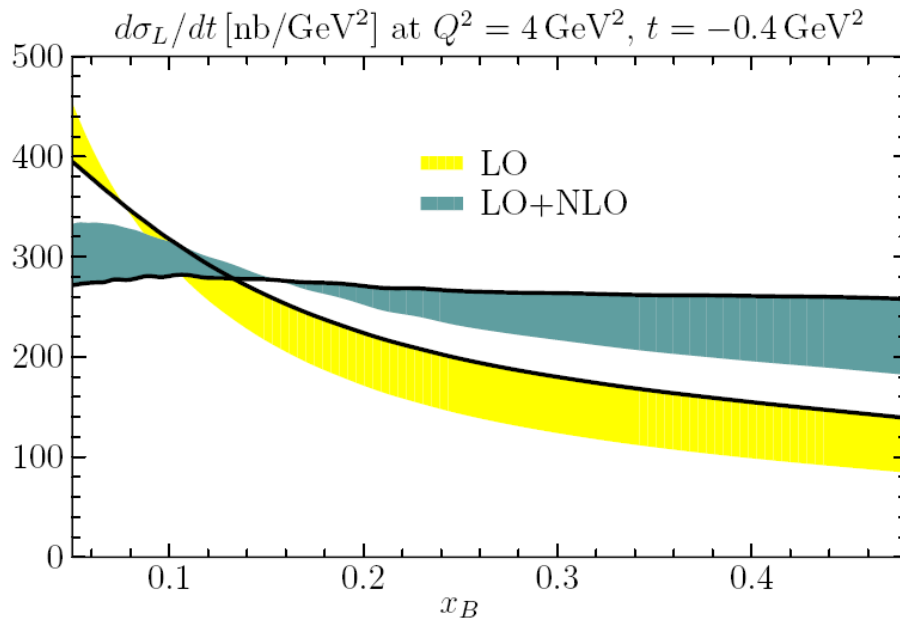
two ways to set a *hard* scale: \blacksquare large Q^2
 \blacksquare mass of produced VM

universality: ρ and ϕ at large Q^2+M^2 similar to J/Ψ , Y

VM production from low \rightarrow high x



- NLO corrections to VM production are large: [M. Diehl, W. Kugler (2007)]



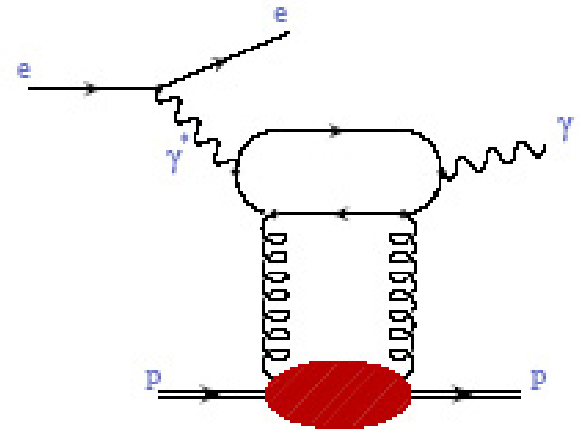
ρ^0 cross section @typical
kinematics of COMPASS /
HERMES / JLab12

Deeply Virtual Compton Scattering

$\rightarrow H, \tilde{H}, E, \tilde{E}$

- DVCS cross sections @ low x

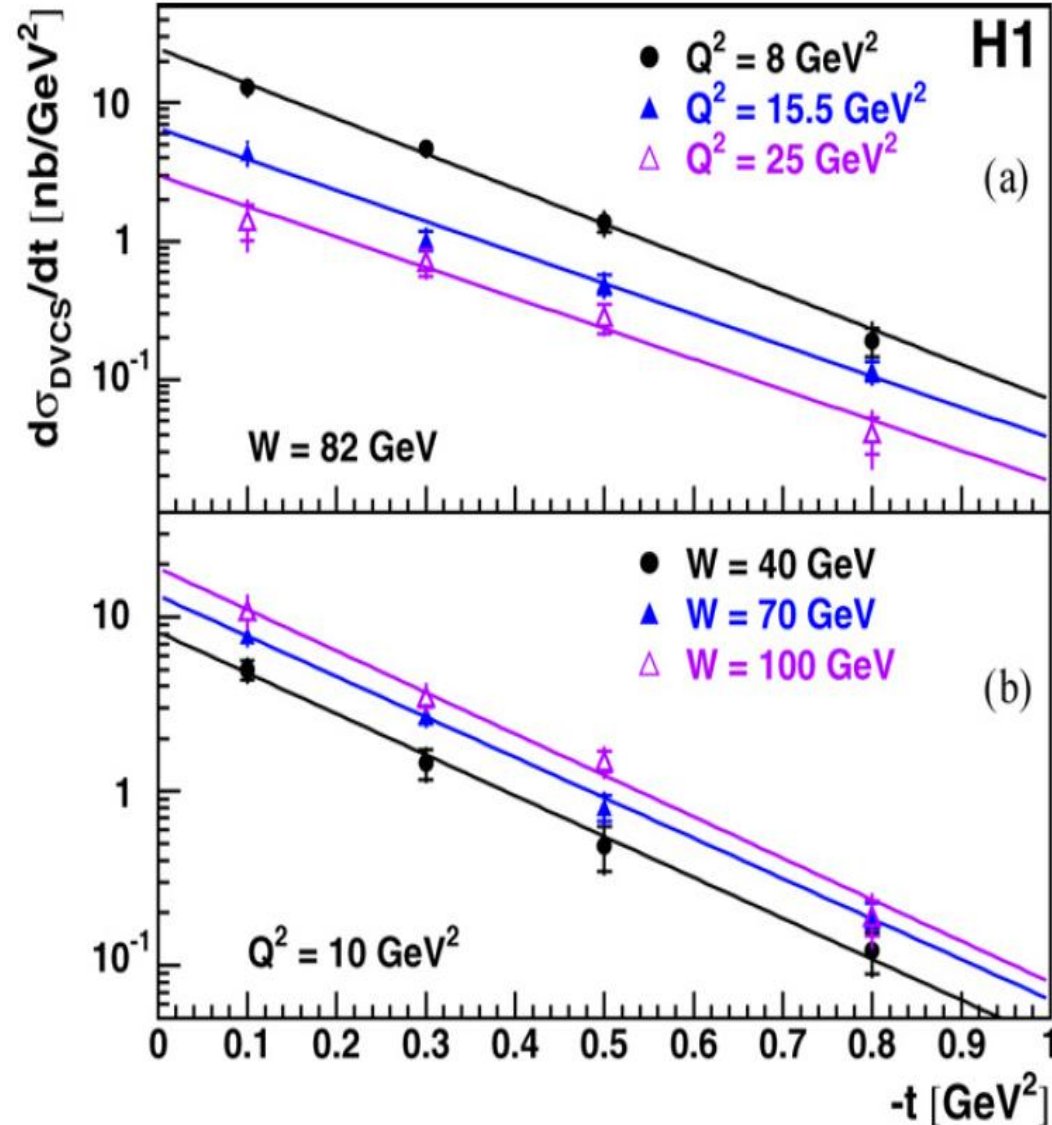
$$d\sigma \propto |\tau_{\text{BH}}|^2 + |\tau_{\text{DVCS}}|^2 + I$$



$$\frac{d\sigma}{dt} \propto e^{-b|t|}$$

- t slope provides absolute normalisation
- $FT \rightarrow$ average impact parameter

[PLB659(2008)]

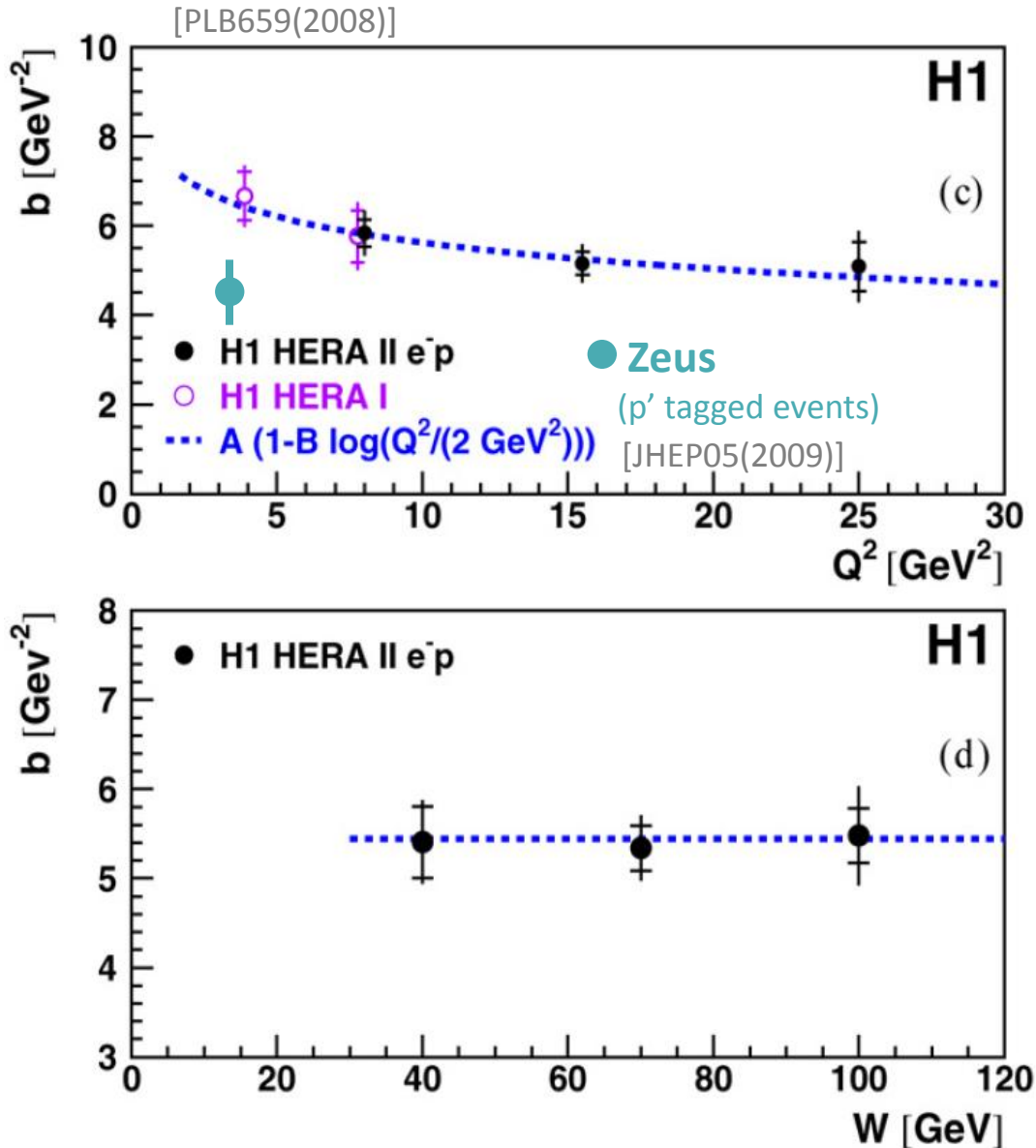


- t slope measurement provides absolute normalisation

$$\frac{d\sigma}{dt} \propto e^{-b|t|}$$



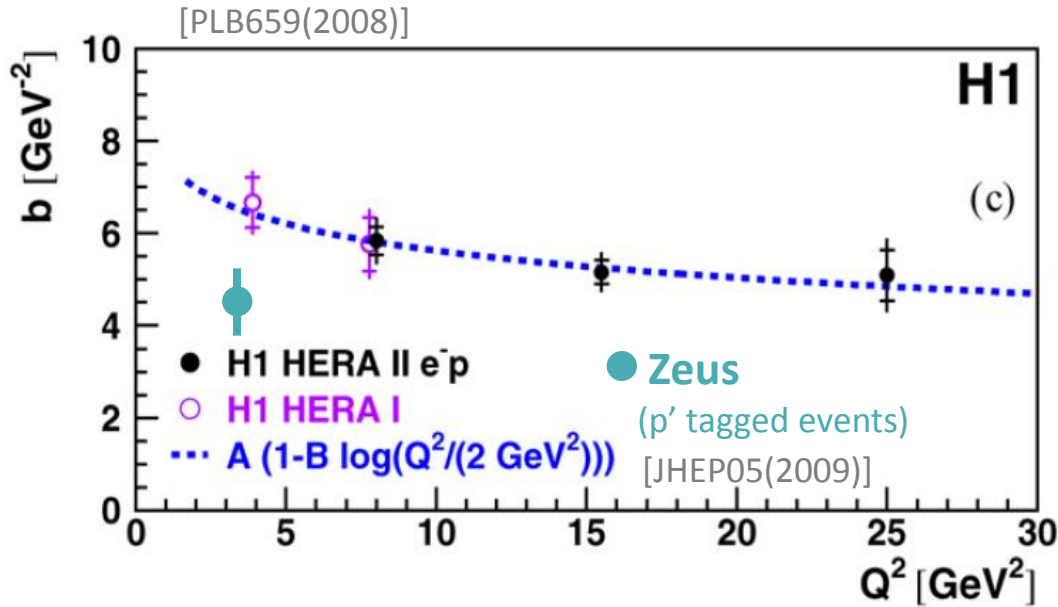
DVCS cross section



- t slope measurement provides absolute normalisation

$$\frac{d\sigma}{dt} \propto e^{-b|t|}$$

- **universality** of slope parameter: pointlike configurations dominate



- t slope measurement provides absolute normalisation

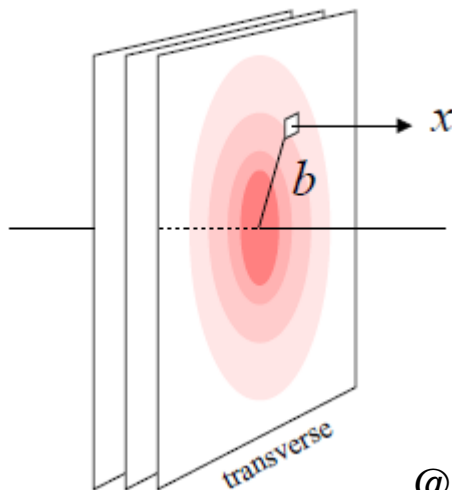
$$\frac{d\sigma}{dt} \propto e^{-b|t|}$$

- **universality** of slope parameter: pointlike configurations dominate
- $FT \rightarrow$ average impact parameter

$$\sqrt{\langle b_T^2 \rangle} = (0.65 \pm 0.02) \text{ fm}$$

$$@ x_B = 10^{-3}$$

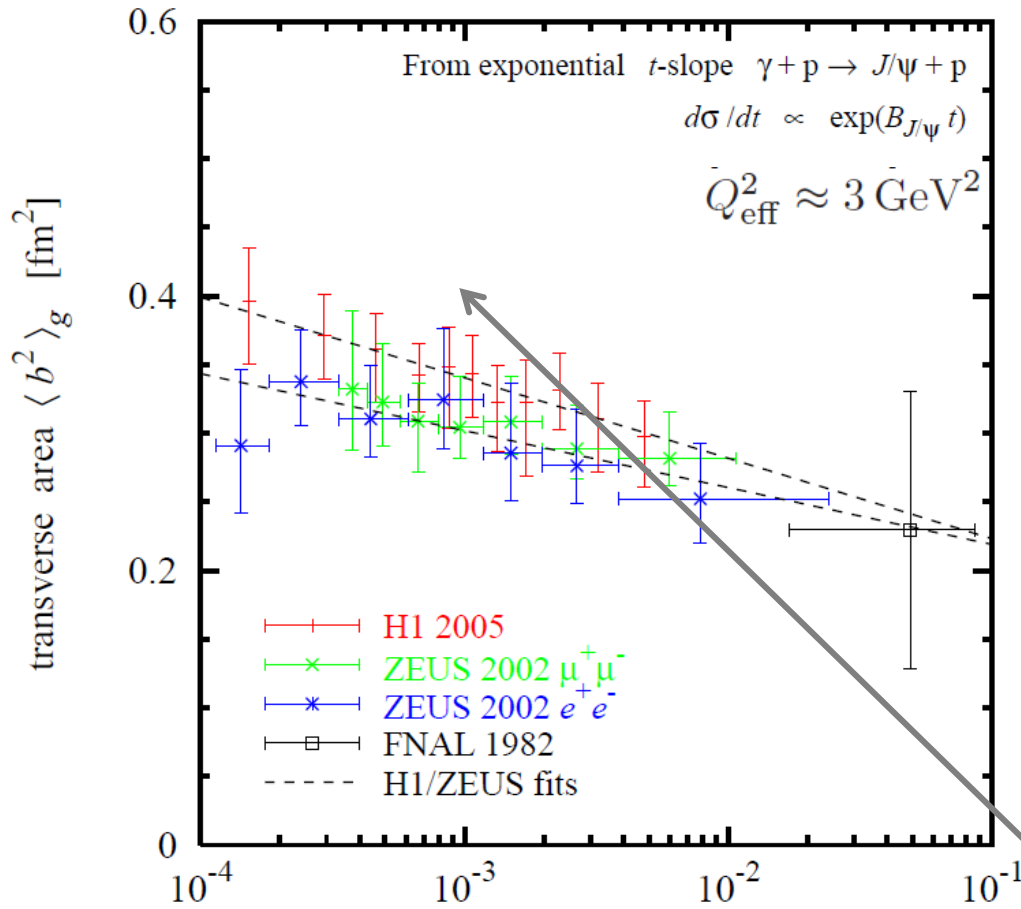
$$\langle Q^2 \rangle = 8.0 \text{ GeV}^2$$



$$@ x_B = 10^{-3}$$



sea quark & gluon imaging



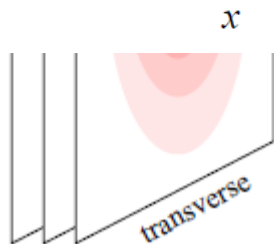
→ remember J/ψ

- universality of slope parameter: pointlike configurations dominate
- $FT \rightarrow$ average impact parameter

$$\sqrt{\langle b_T^2 \rangle} = (0.65 \pm 0.02) \text{ fm}$$

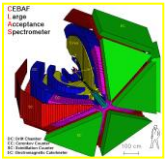
@ $x_B=10^{-3}$

$\langle Q^2 \rangle = 8.0 \text{ GeV}^2$

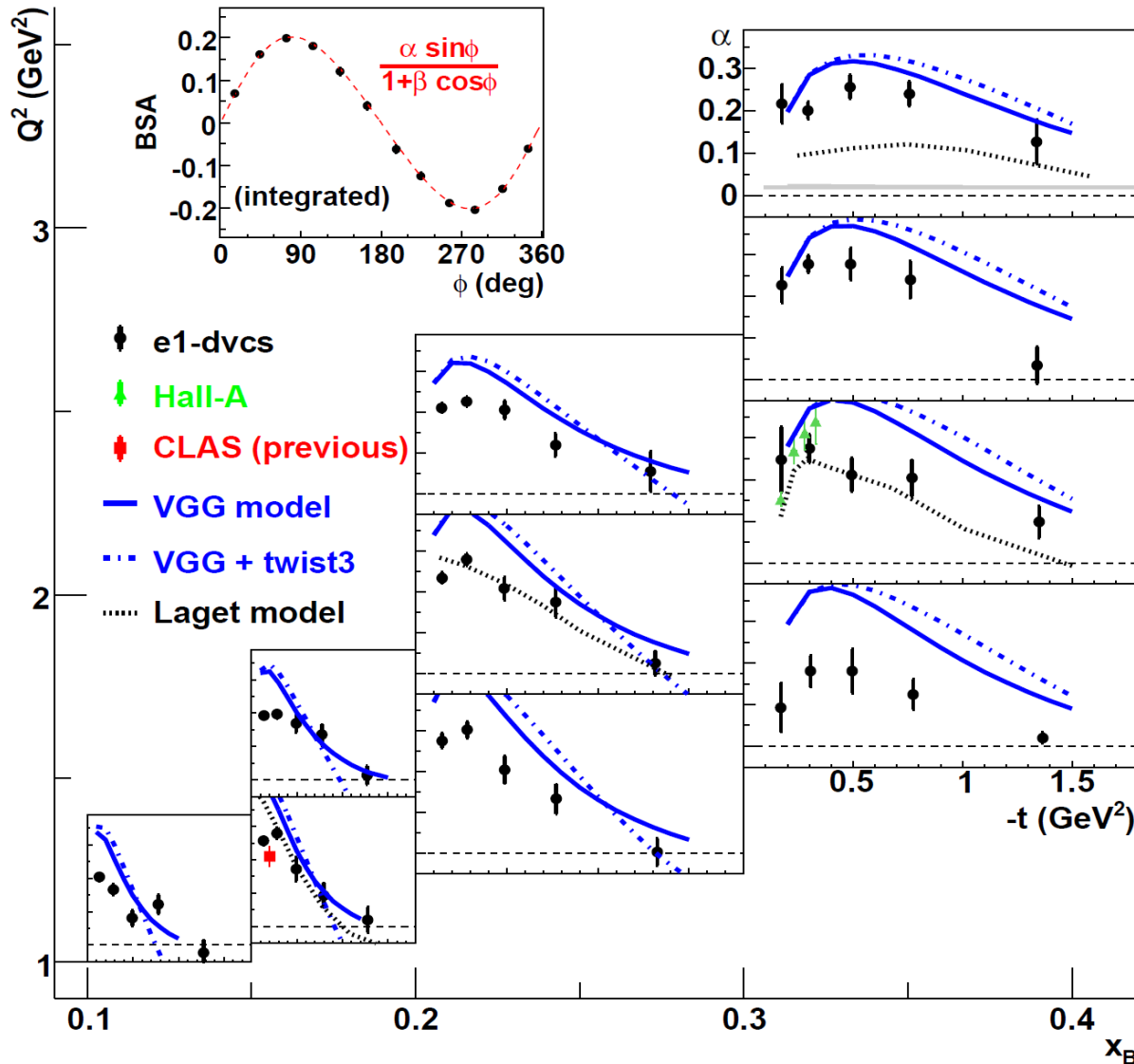


@ $x_B=10^{-3}$

call for high statistics



DVCS beam-spin asymmetry [PRL100(2008)]



$$\alpha \propto \text{Im}(F_1 H)$$

hunting the OAM

-- ρ^0 : transverse target-spin asymmetry --

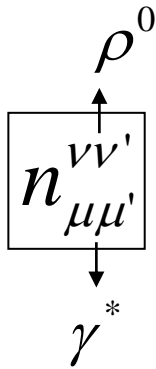


after the full glory of SDME extractions

[formalism by M. Diehl (2007)]

$$(\gamma_L^* \rightarrow \rho_L^0):$$

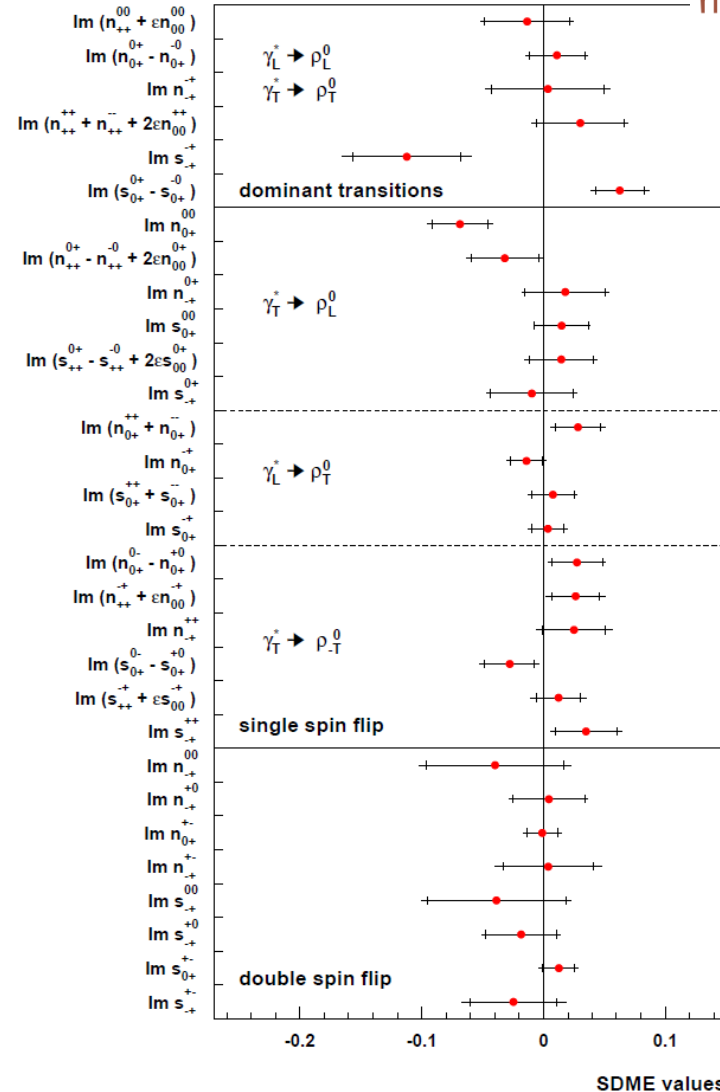
$$A_{UT}^{\gamma^*}(\phi, \phi_s) = \frac{\text{Im } n_{00}^{00}}{u_{00}^{00}}$$



$$\mu, \nu = 0, \pm 1$$

long.pol: 0

transv.pol: ± 1



[PLB679(2009)]

hunting the OAM

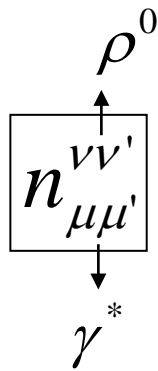
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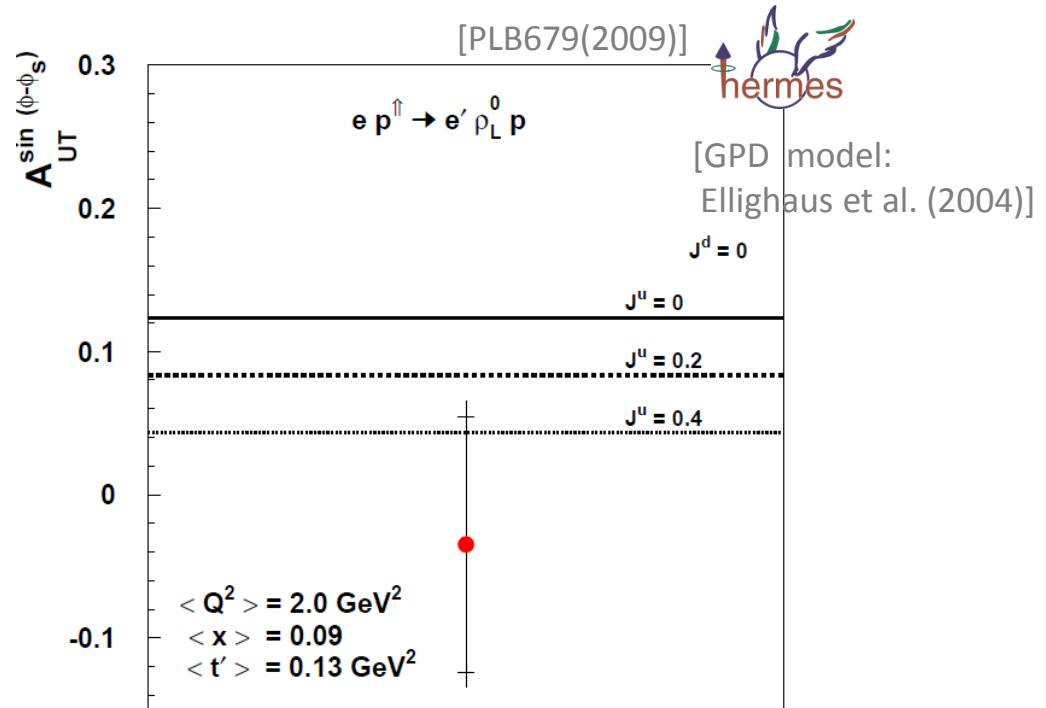
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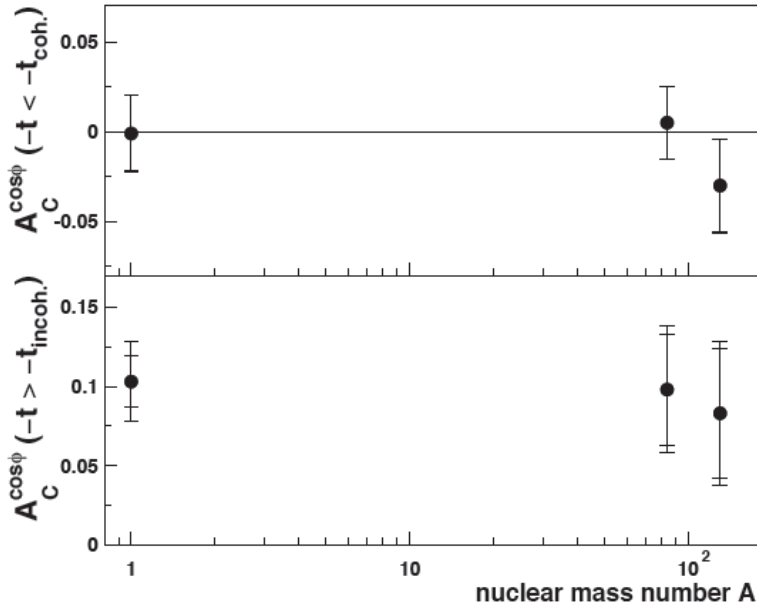


overall

- more data coming: COMPASS, JLab12 with transv. Target
- more models: Goloskokov, Kroll

$A_C^{\cos\phi}$ vs. A

Phys. Rev. C 81 (2010) 035202

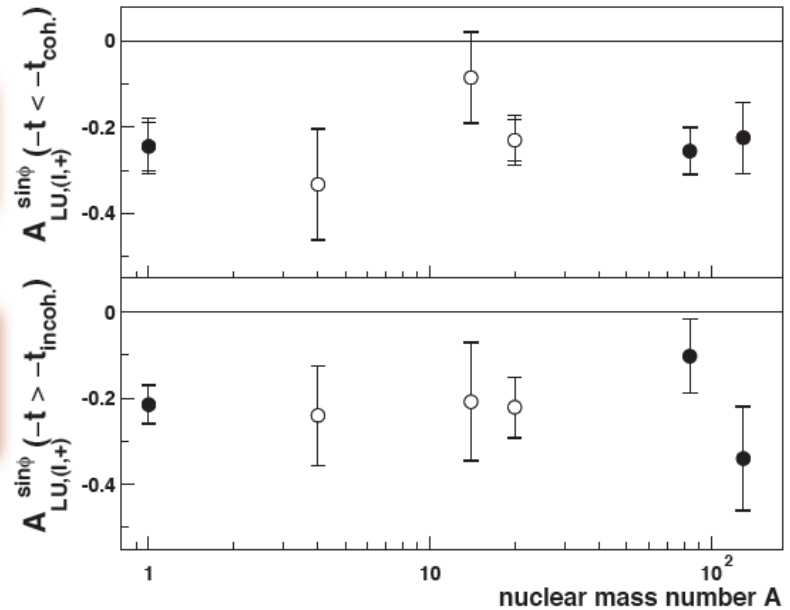


coherent
enriched

incoherent
enriched

Beam-charge asymmetry

$A_{LU}^{\sin\phi}$ vs. A



Beam-helicity asymmetry

- ❖ How does the nuclear medium modify parton-parton correlations?
- ❖ How do nucleon properties change in the nuclear medium?
- ❖ Enhanced 'generalized EMC effect', rise of T_{DVCS} with A ?

Average
 A_{LU}^A / A_{LU}^H :

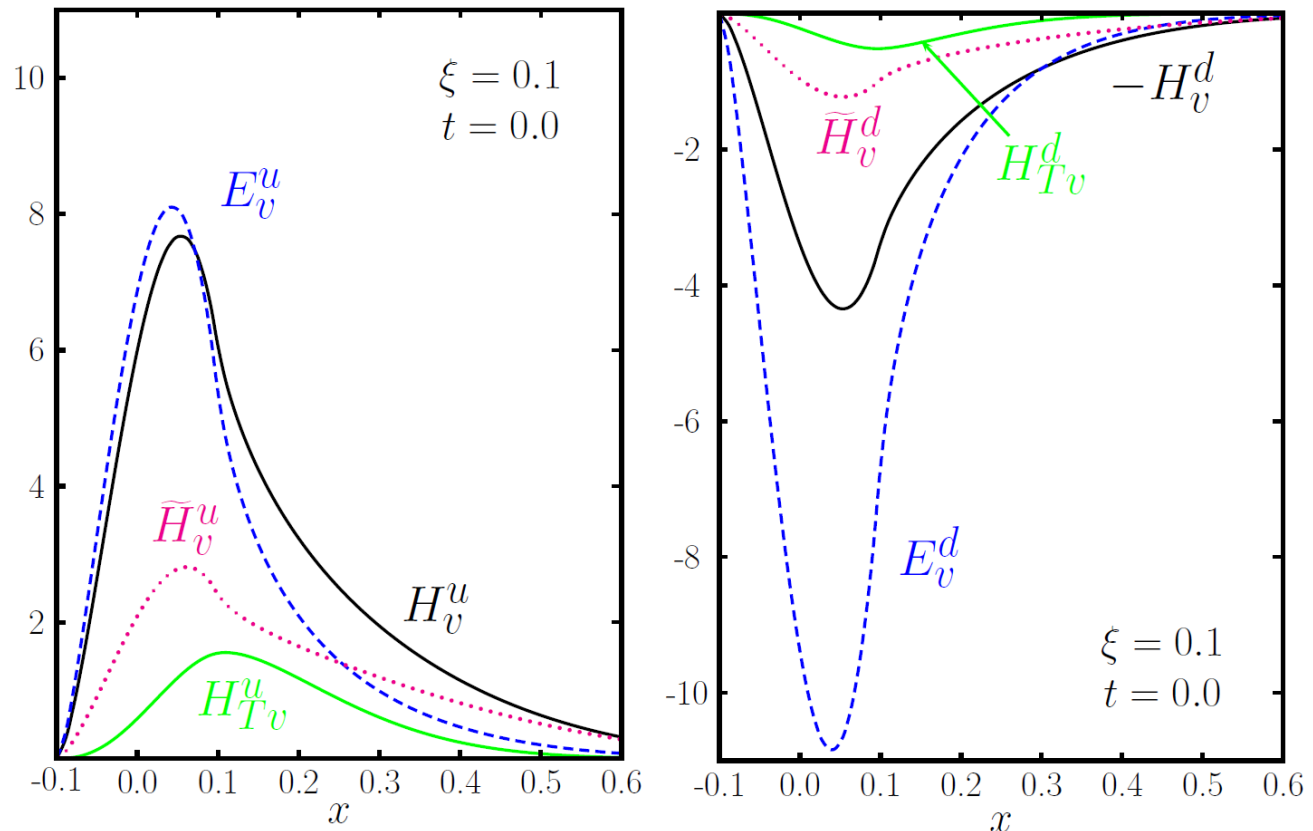
0.91 ± 0.19

0.93 ± 0.23

towards GPDs

recent developments (beyond VGG(1999)...)

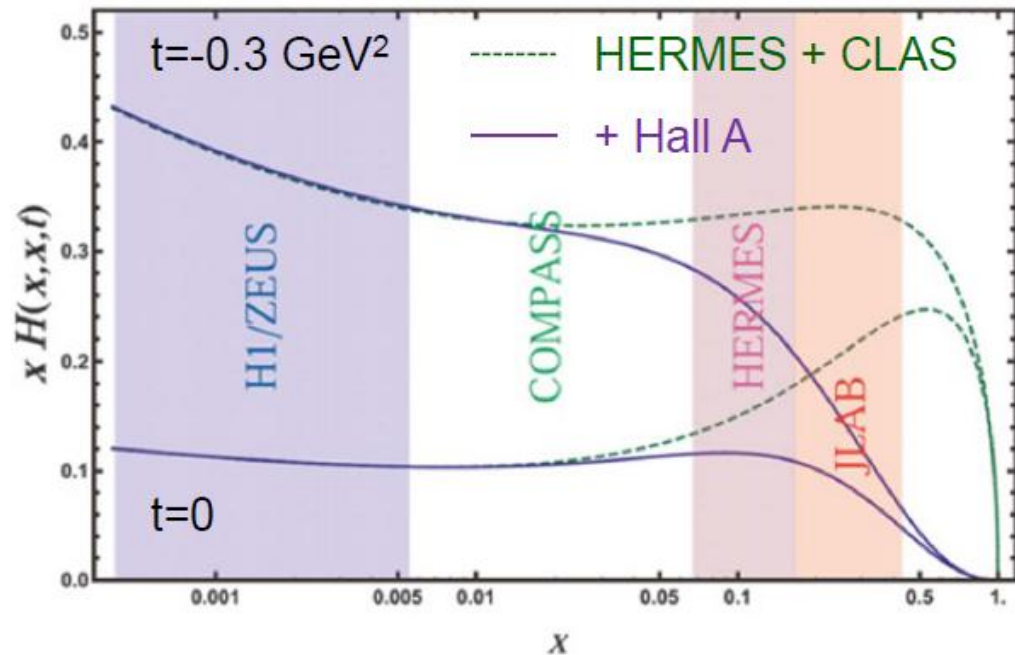
- Goloskokov, Kroll (2007):
 - LO GPD model using *DD, regge t dep., power corrections*
 - fit to **exclusive meson production data**



towards GPDs

recent developments (beyond VGG(1999)...)

- Goloskokov, Kroll (2007):
 - LO GPD model using *DD*, *regge t dep.*, *power corrections*
 - fit to **exclusive meson production** data
- Kumericki, Müller (2010):
 - partial wave expansion of GPDs, *regge t dep.*, *dispersion relations*
 - fit to **DVCS** data



towards GPDs

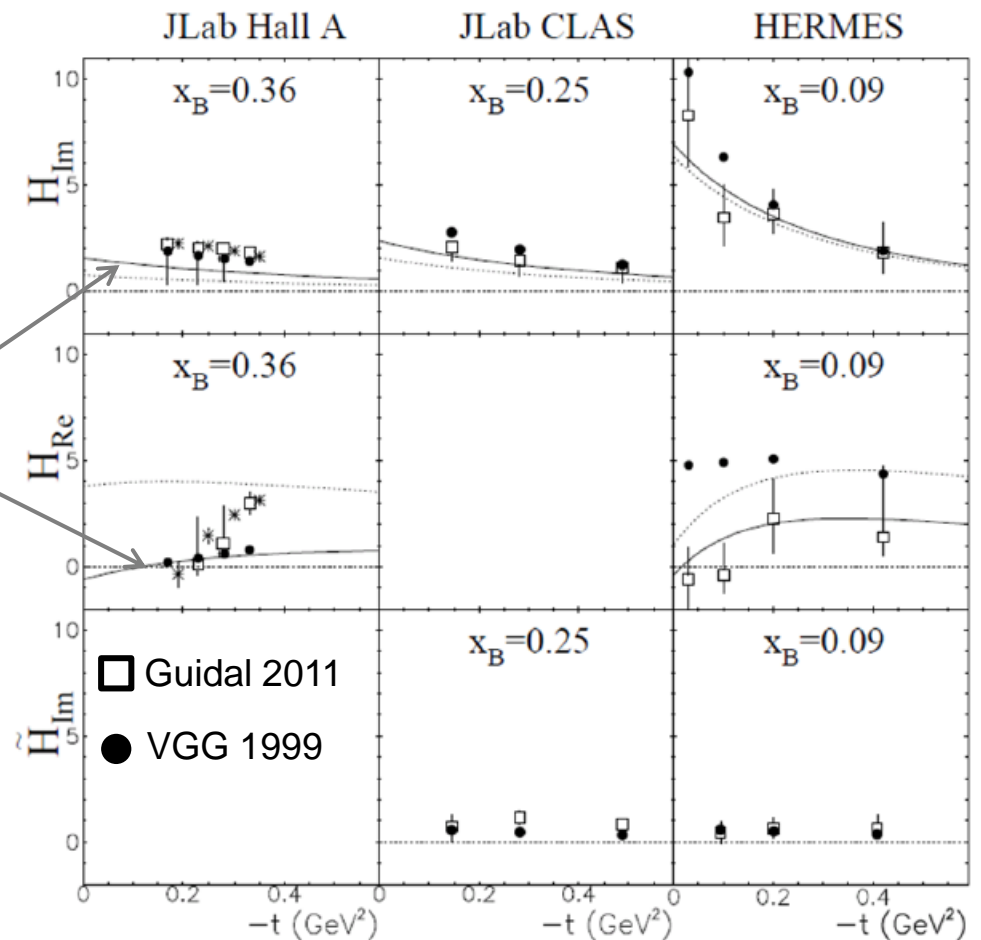
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 - fit to **exclusive meson production** data
- Kumericki, Müller (2010):
 - partial wave expansion of GPDs, *regge t dep.*, *dispersion relations*
 - fit to **DVCS** data
- Goldstein, Hernandez, Liuti (2010):
 - quark-diquark model of GPDs, *Regge ansatz for low x region & t dep.*
 - fit to **DVCS** data

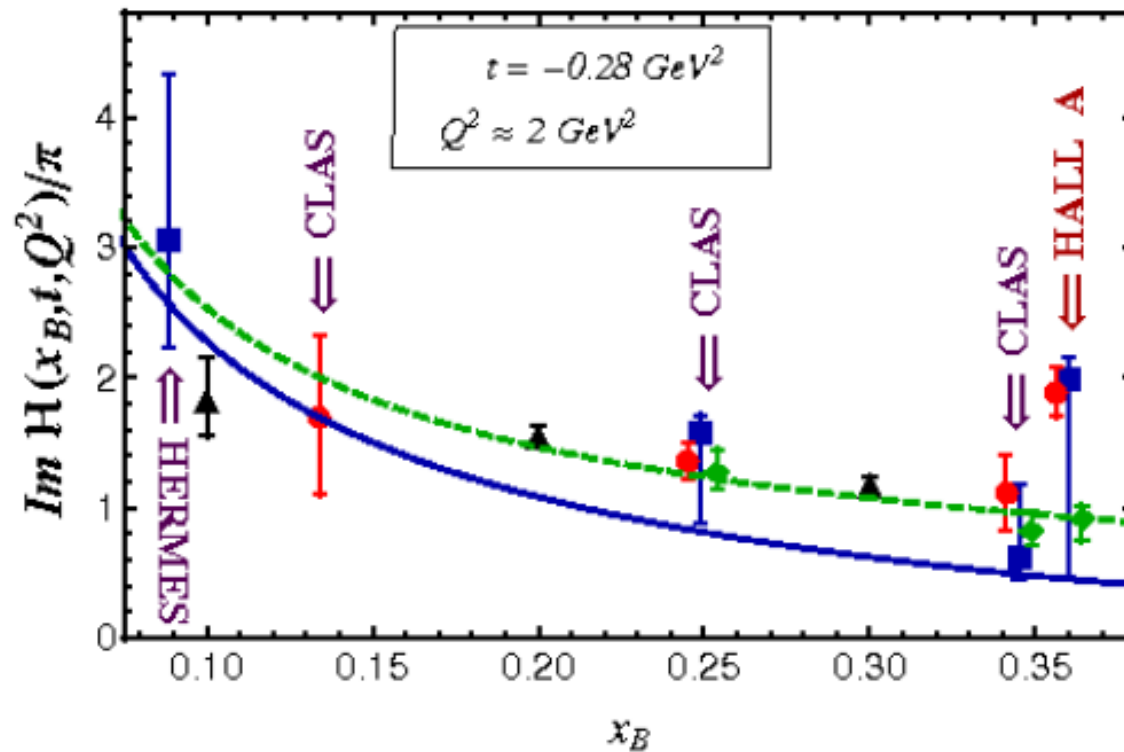
towards GPDs

recent developments (beyond VGG)

- Goloskokov, Kroll (2007):
 - LO GPD model using D
 - fit to **exclusive meson p**
- Kumericki, Müller (2010):
 - partial wave expansion
 - fit to **DVCS** data
- Goldstein, Hernandez, Liuti (2011):
 - quark-diquark model of ρ
 - fit to **DVCS** data
- Guidal (2011):
 - *model independent* extraction of **CFF** (GPD extr. requires model ansatz)
 - kinematic fitting of **DVCS** data (per experiment)



towards global analysis of GPDs



[Guidal '08, Guidal and Moutarde '09], seven CFF fit (blue squares), [Guidal '10] $\mathcal{H}, \tilde{\mathcal{H}}$ CFF fit (green diamonds), [Moutarde '09] H GPD fit (red circles)

(slide from K. Kumericki, Photons11)

towards global analysis of GPDs

-- employ all available exclusive data (DVCS & meson production) --

